

PROBONITE : PRivate One-Branch-Only Non Interactive decision Tree Evaluation

Sofiane Azogagh, Victor Delfour, Sébastien Gambs and Marc-Olivier Killijian - UQÀM

Summary

- Introduction
- State-of-the-art
- Preliminaries
 - Functional Bootstrapping
 - Private Information Retrieval
- Our proposal
- Conclusion and perspectives

Introduction

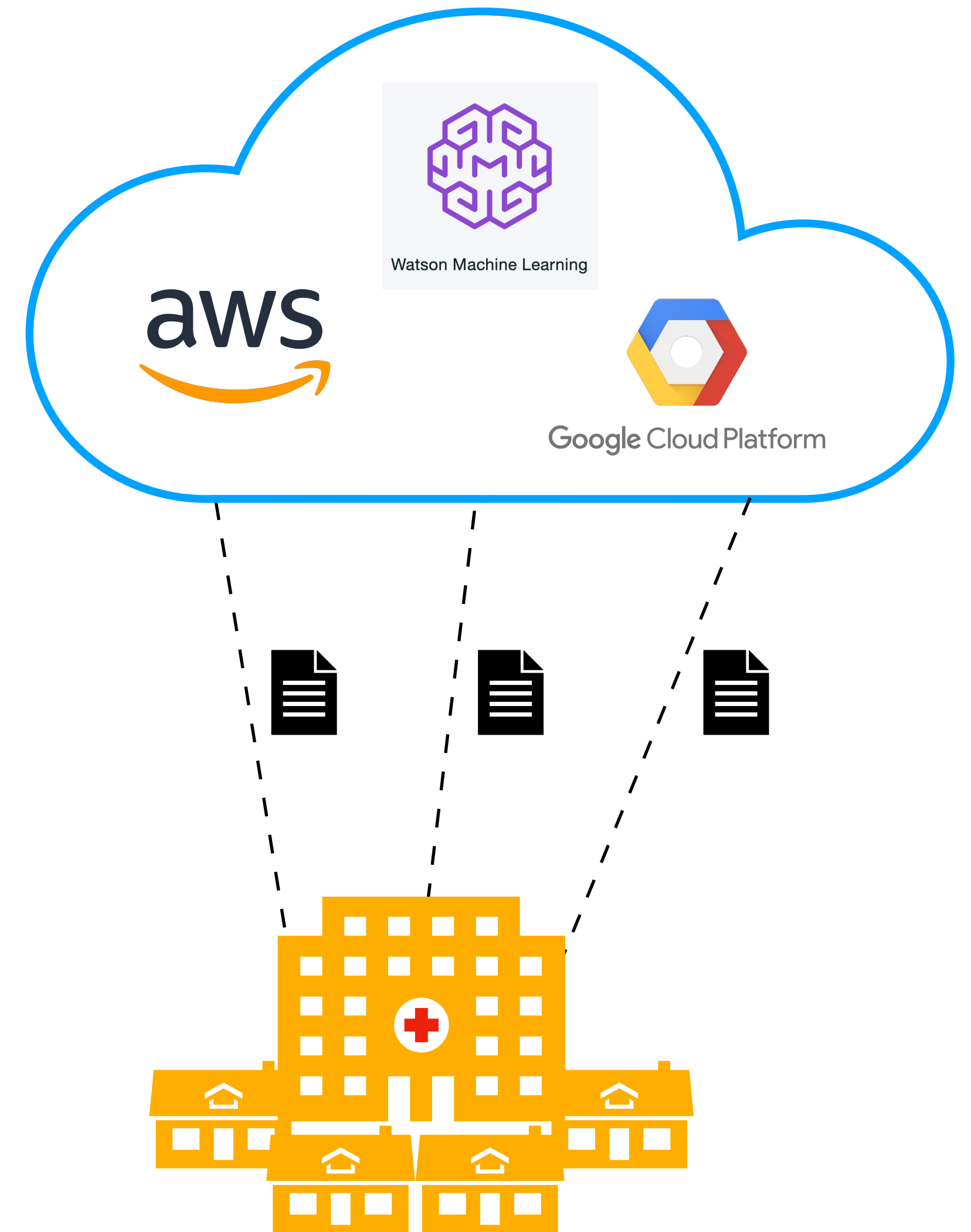
Introduction

Machine Learning as a Service (MLaaS)

Exists in many platforms

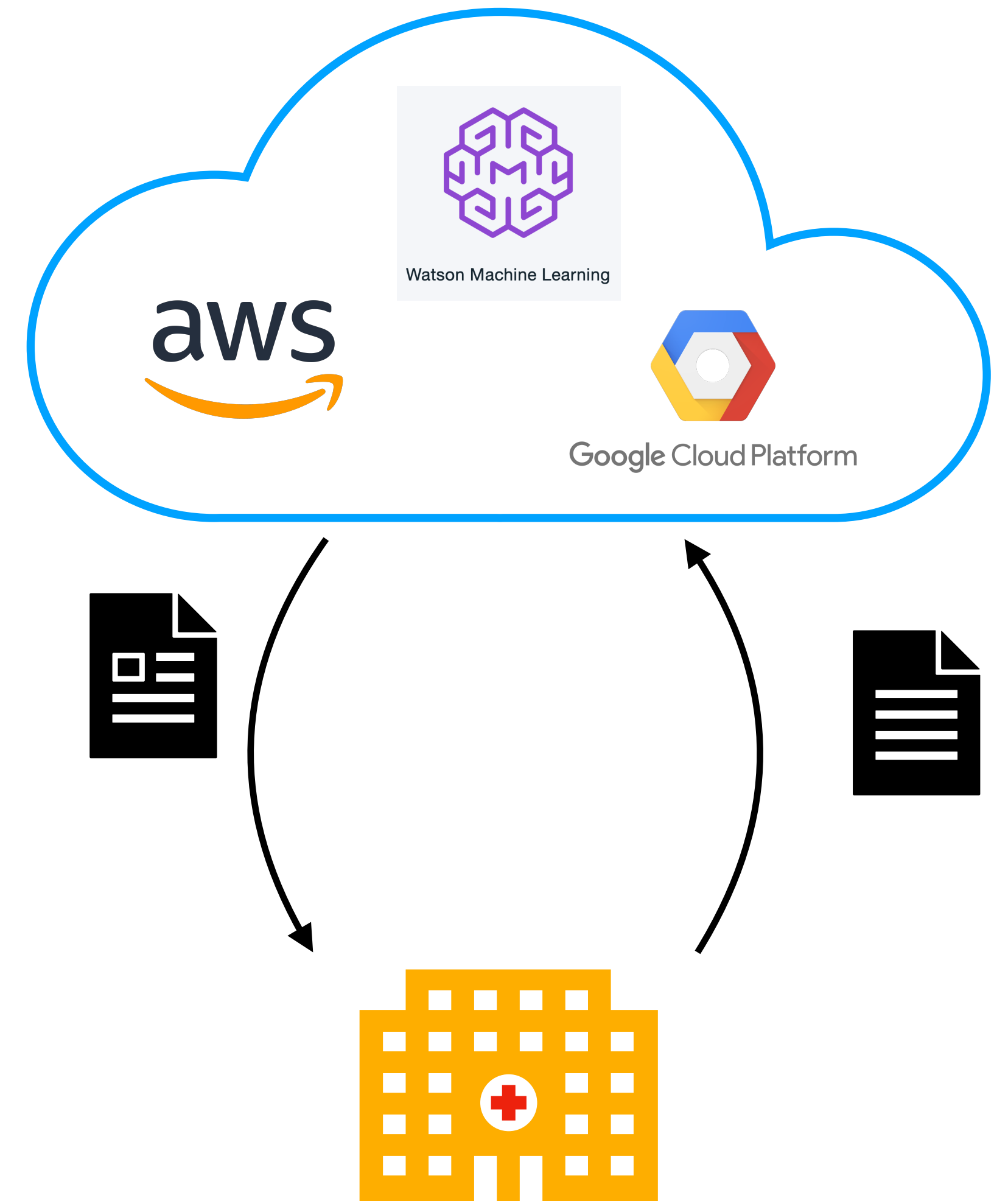
Uses private or personal information

During the training phase or at inference time



Introduction

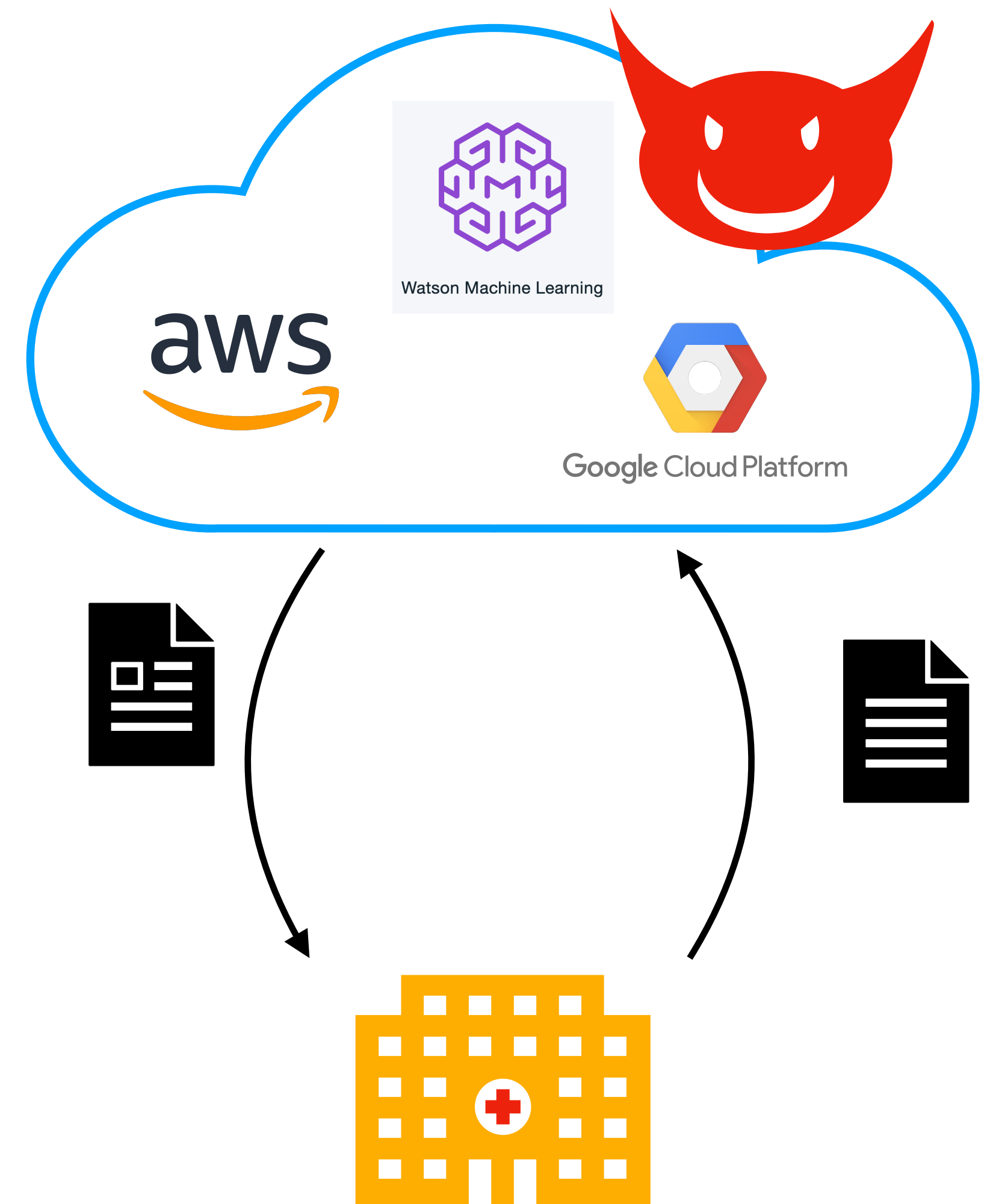
Motivation



Introduction

Motivation

If the cloud is compromised, some private information of the client will leak

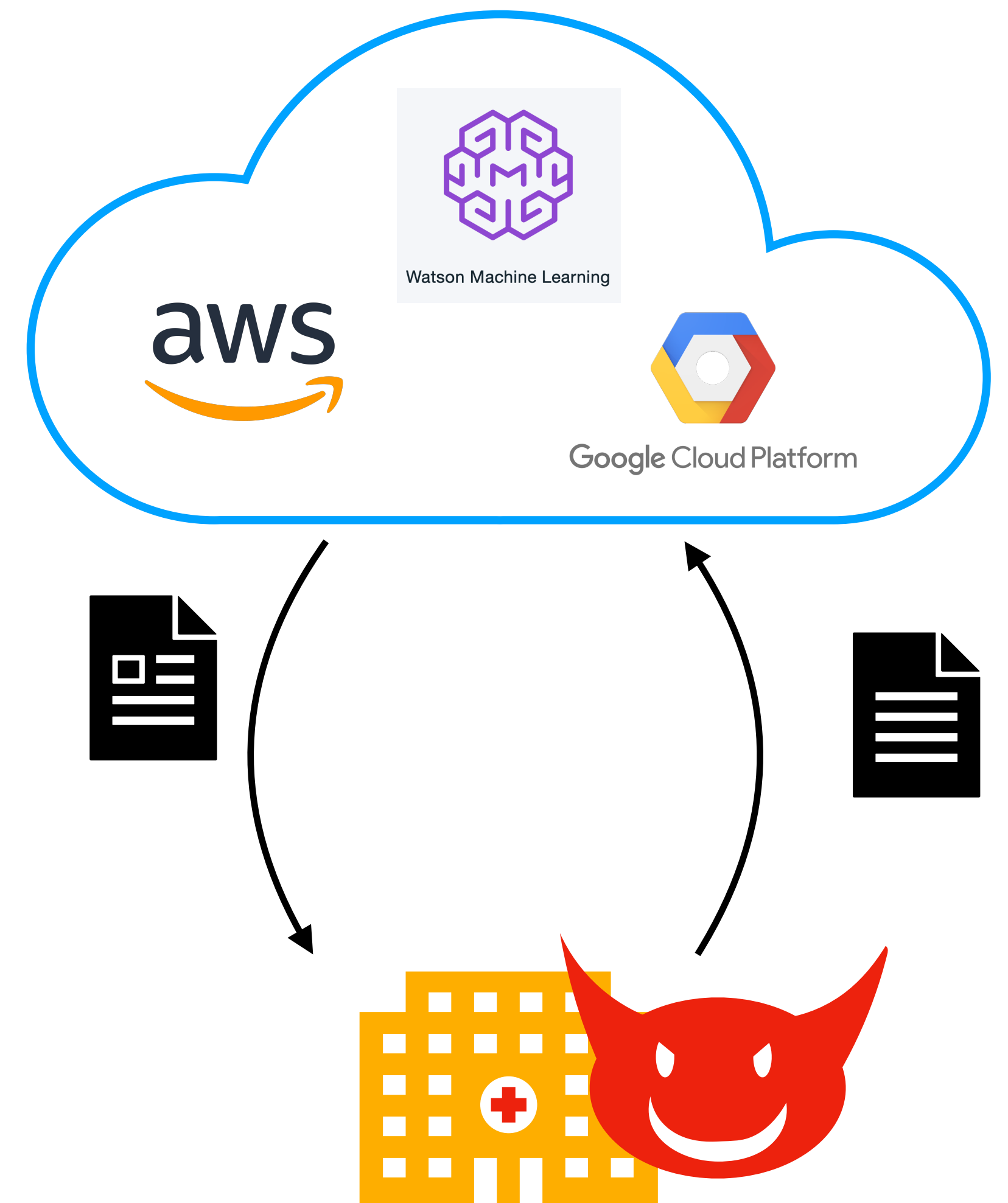


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If the cloud is compromised, some private information of the client will leak

If the client is malicious, he might recover information about the model



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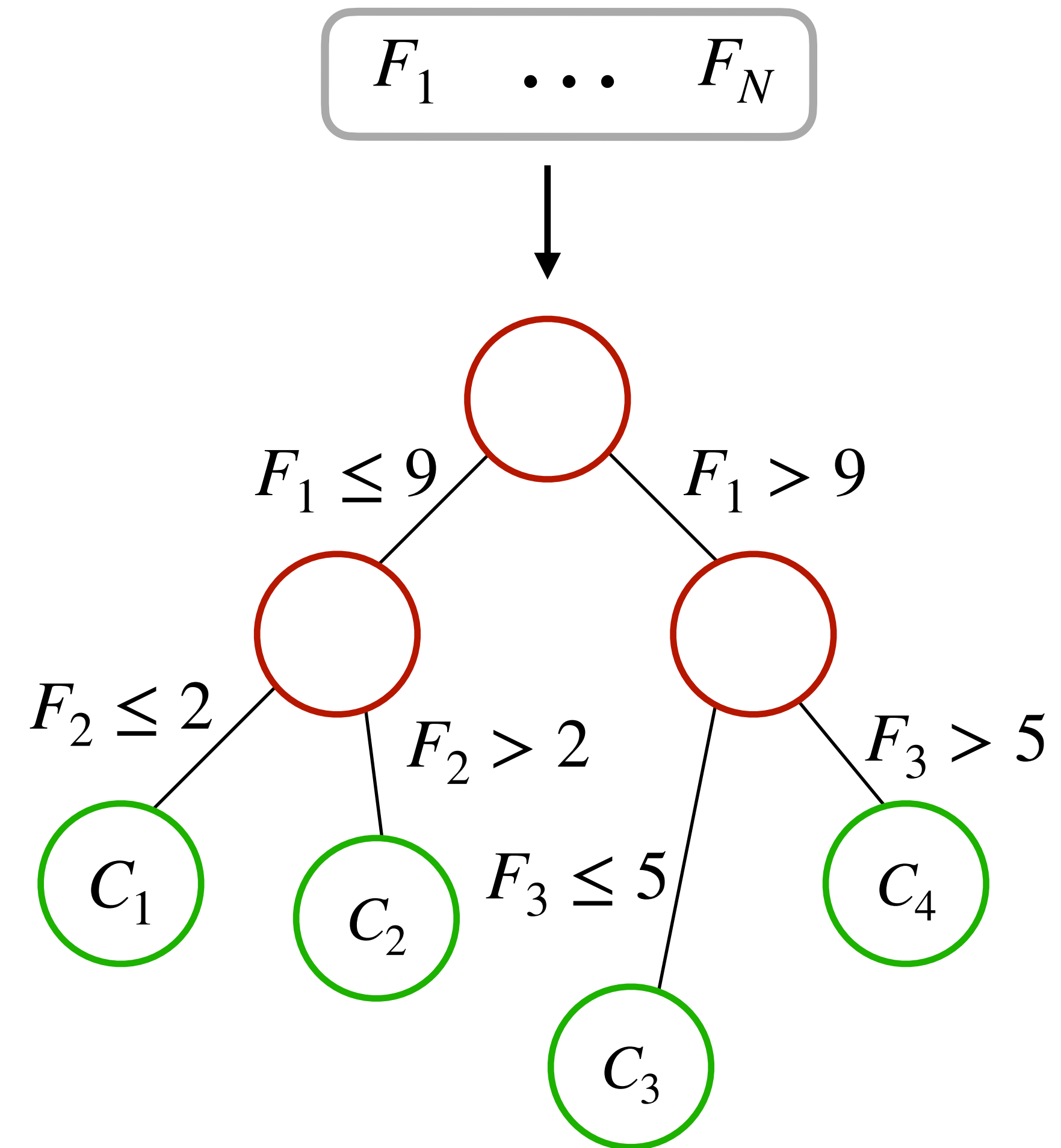
Decision trees are :

- Simpler to train

- Interpretable

- Used in post hoc explanation

- Building block for random forest



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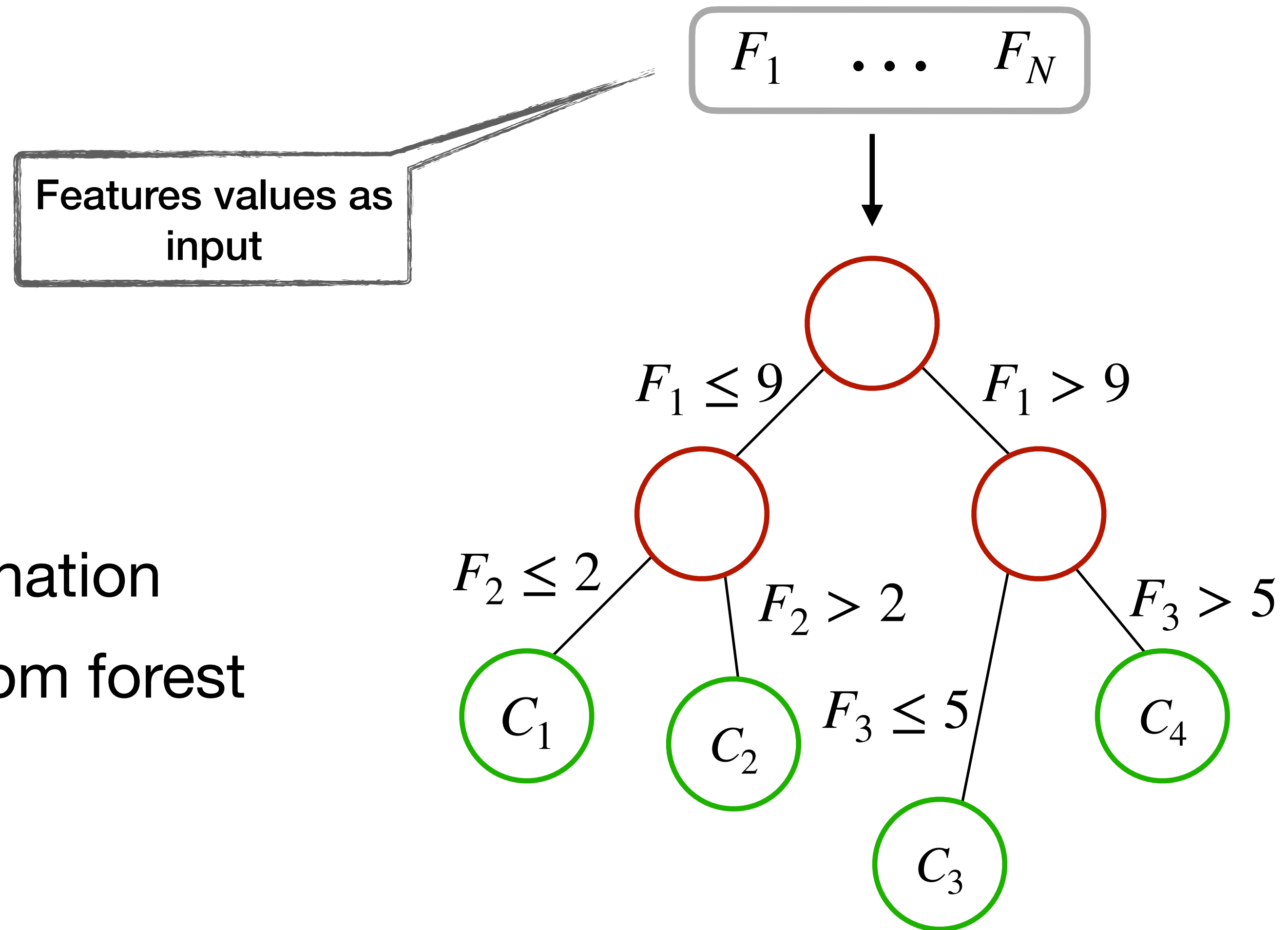
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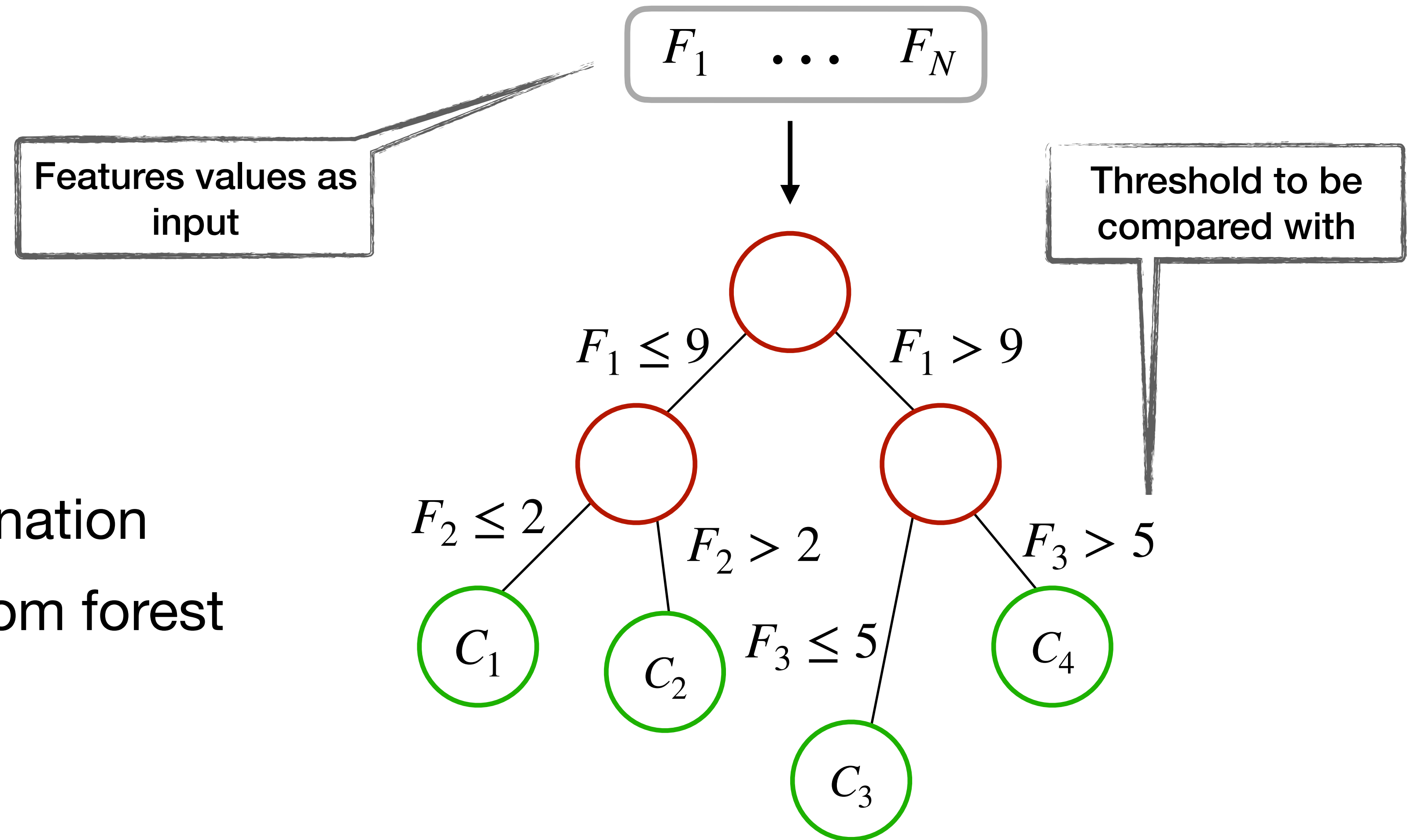
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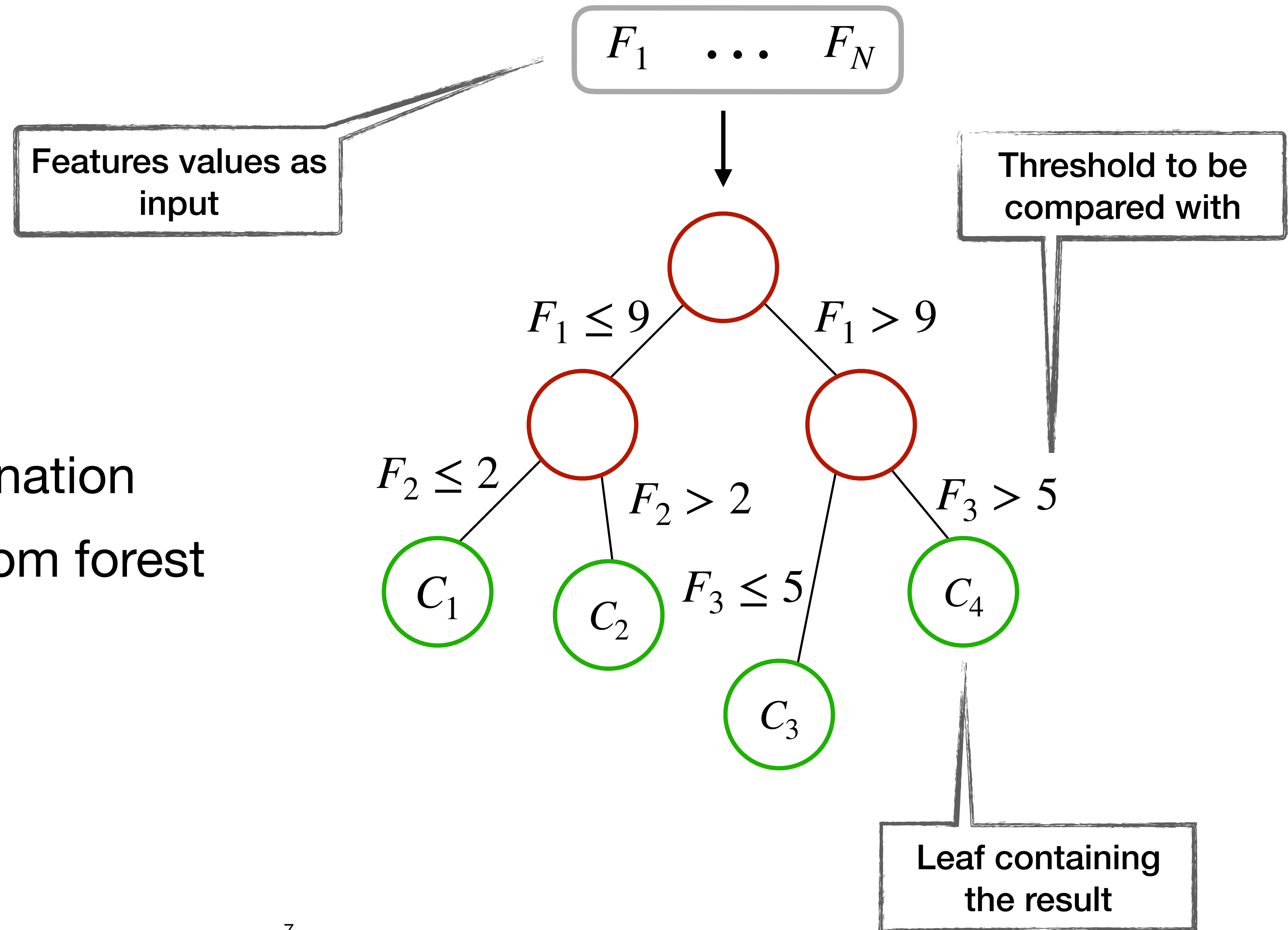
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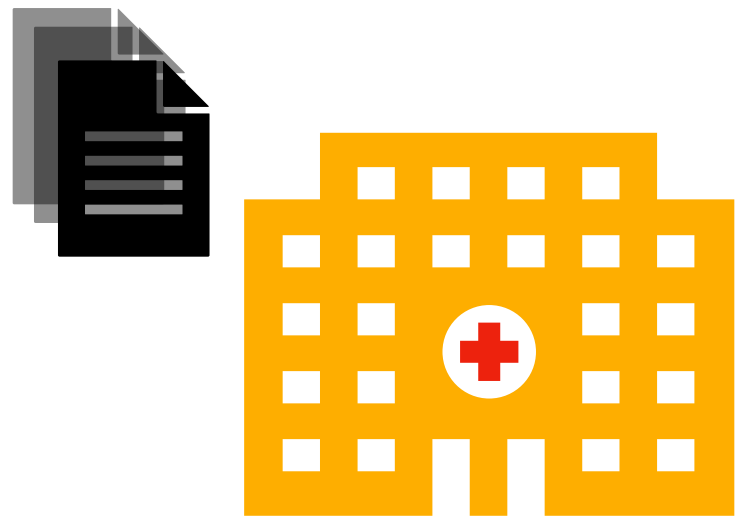
How to evaluate a decision tree on private data ?

Introduction

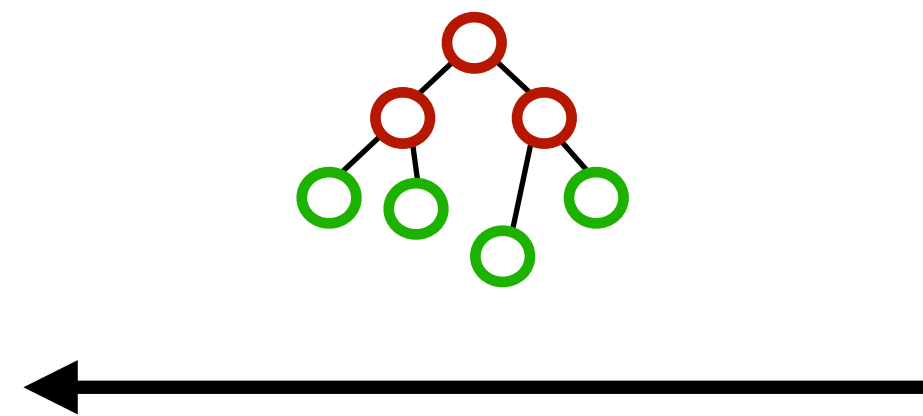
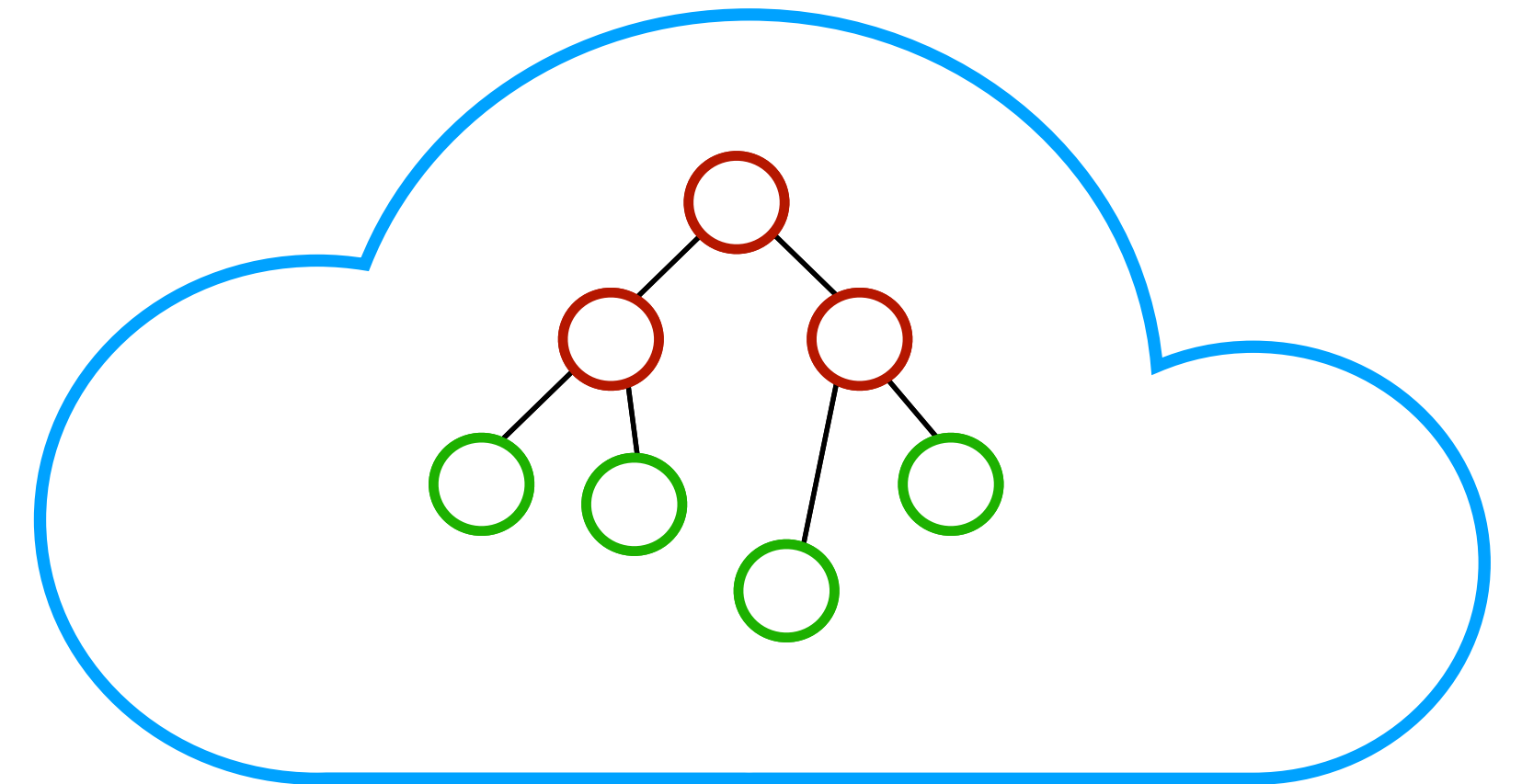
How to evaluate a decision tree on private data ?

The naïve way

Client



Server



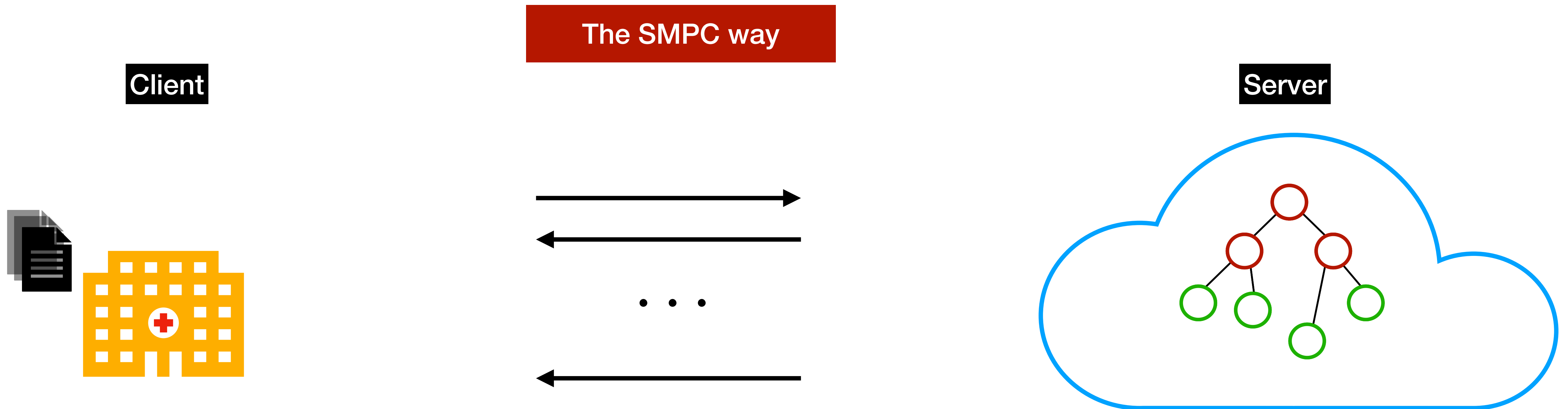
Preserves privacy of the client's data ✓

Preserves privacy of the server's model ✗

Needs one round of communication ✓

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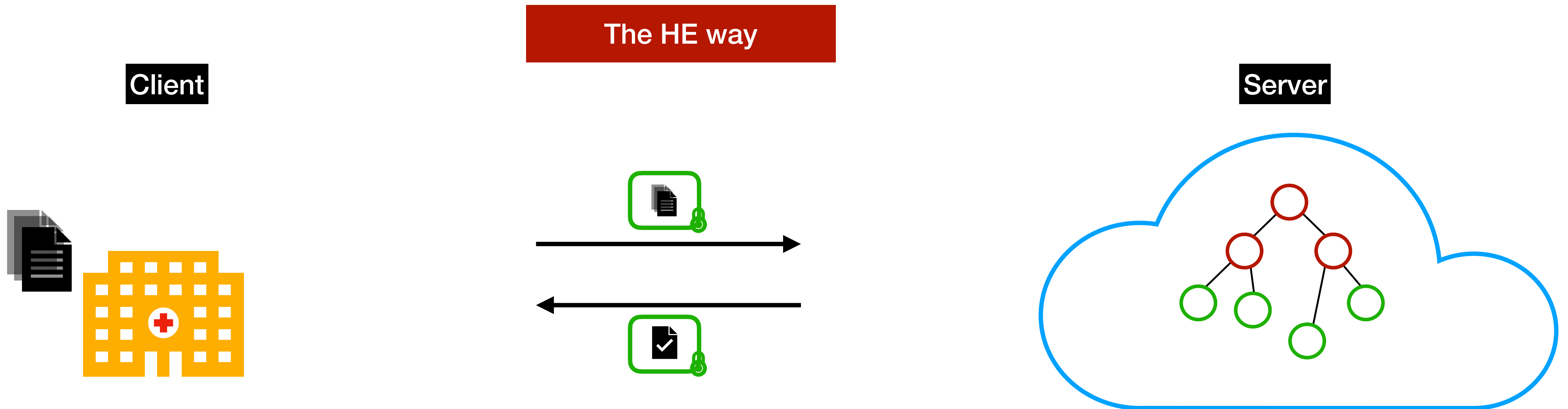
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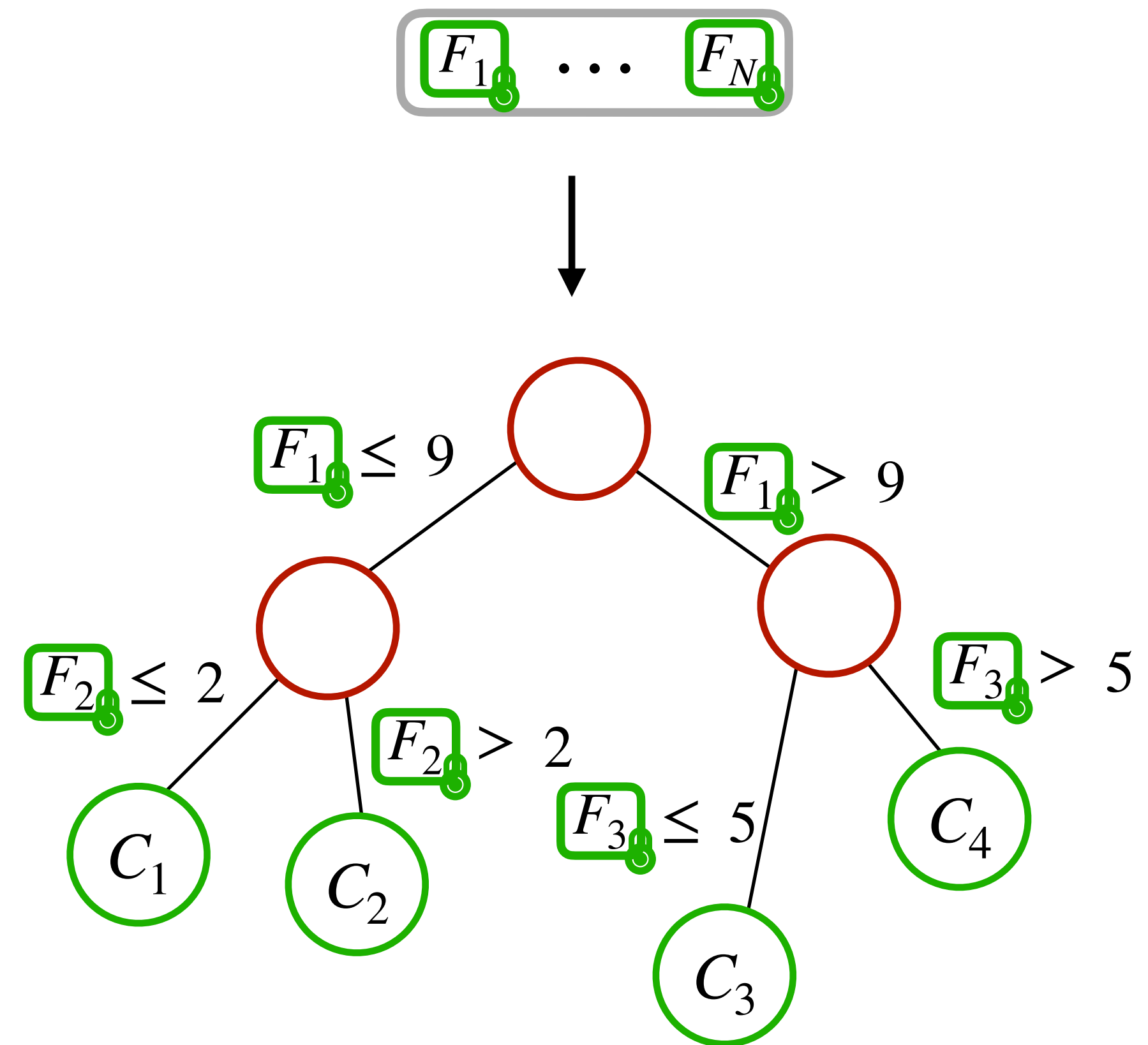
Introduction

How to evaluate a decision tree on private data ?

The client's features are encrypted

Server has to consider all the nodes
($\mathcal{O}(2^d)$)

Private comparison is the most expensive operation and there is one per node

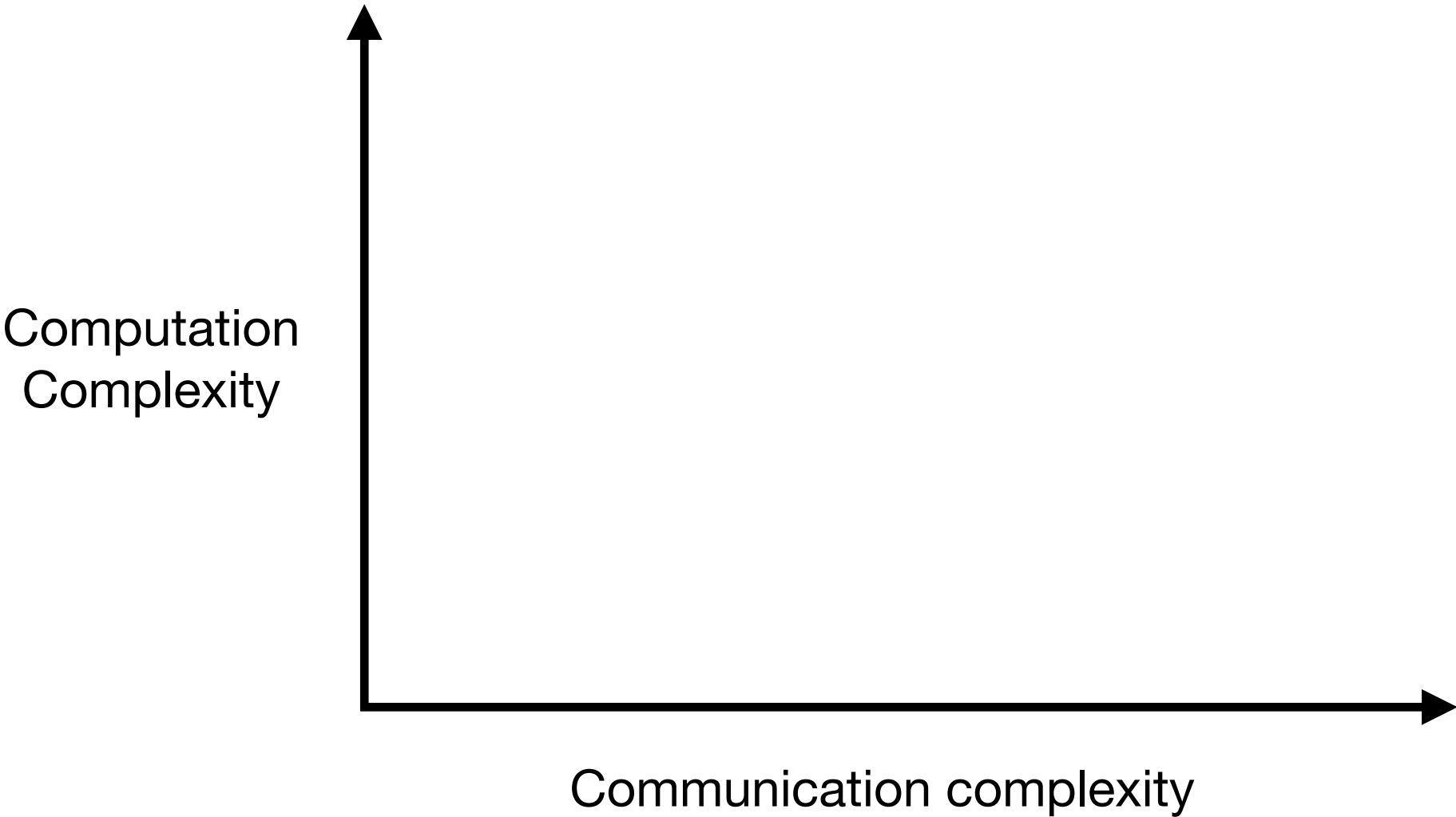


State-of-the-art

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Comparisons of approaches

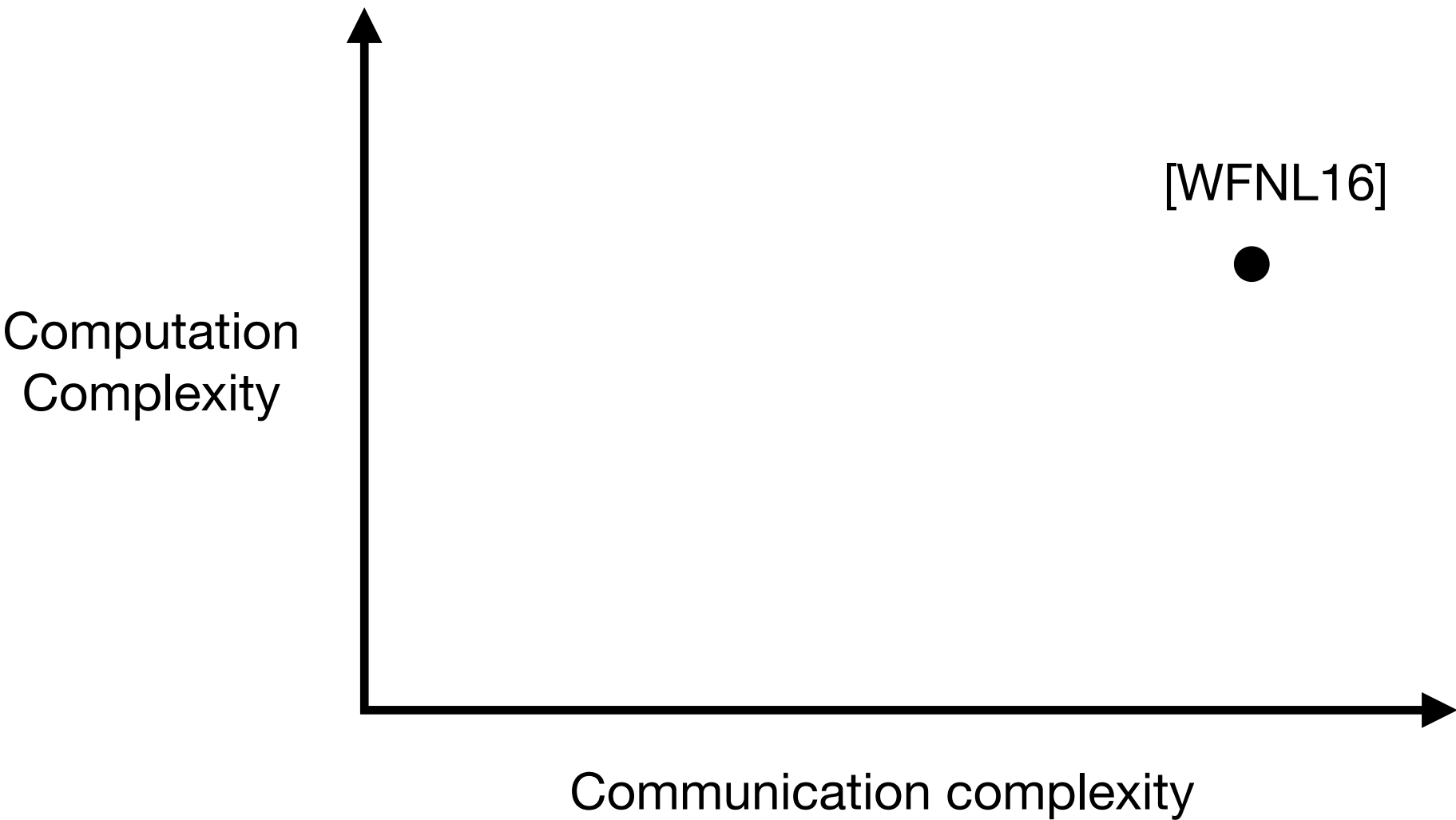
Non-interactive				
One branch				
Techniques used				



State-of-the-art

Comparisons of approaches

	[WFNL16]			
Non-interactive	✗			
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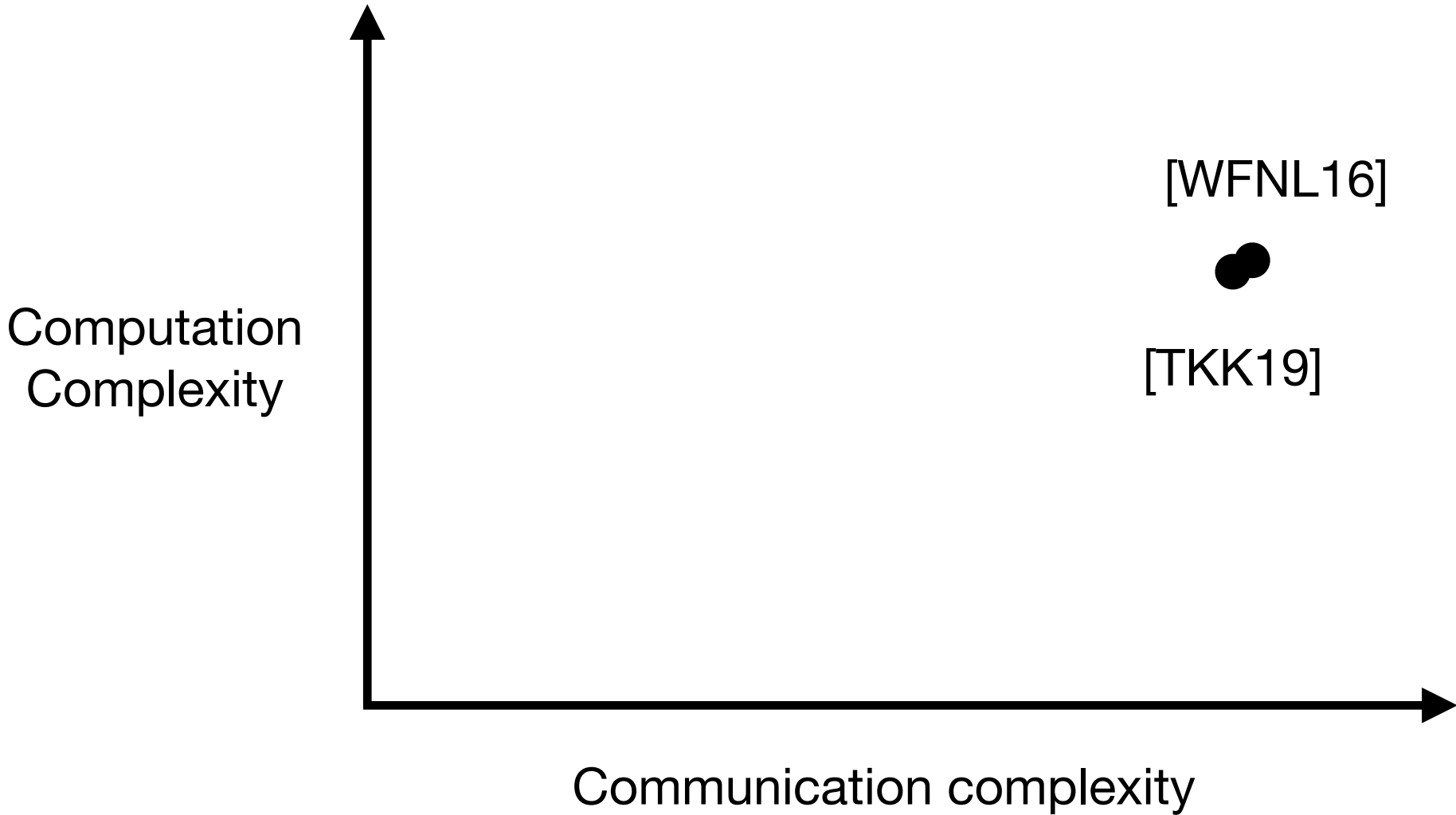


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State-of-the-art

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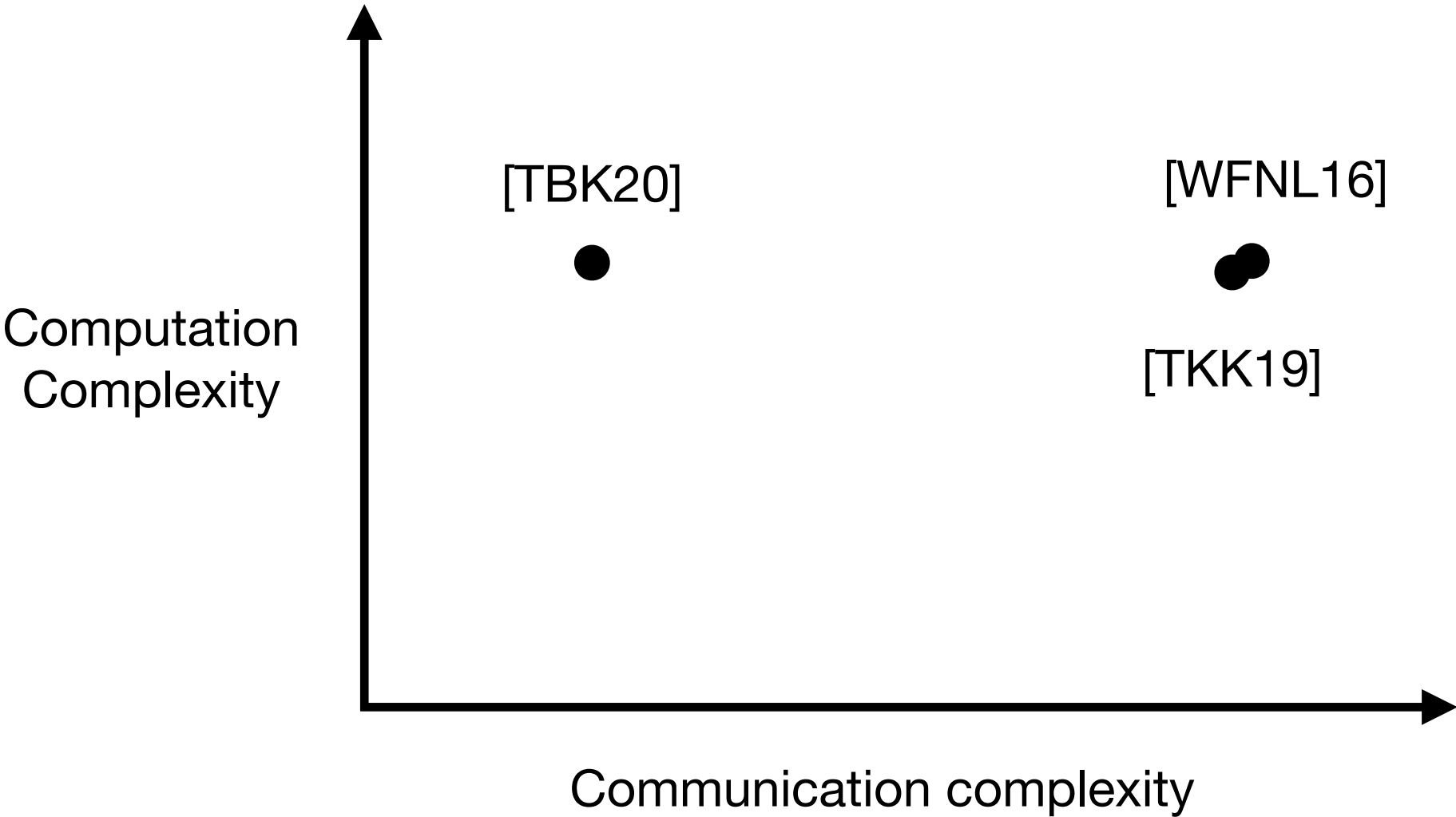


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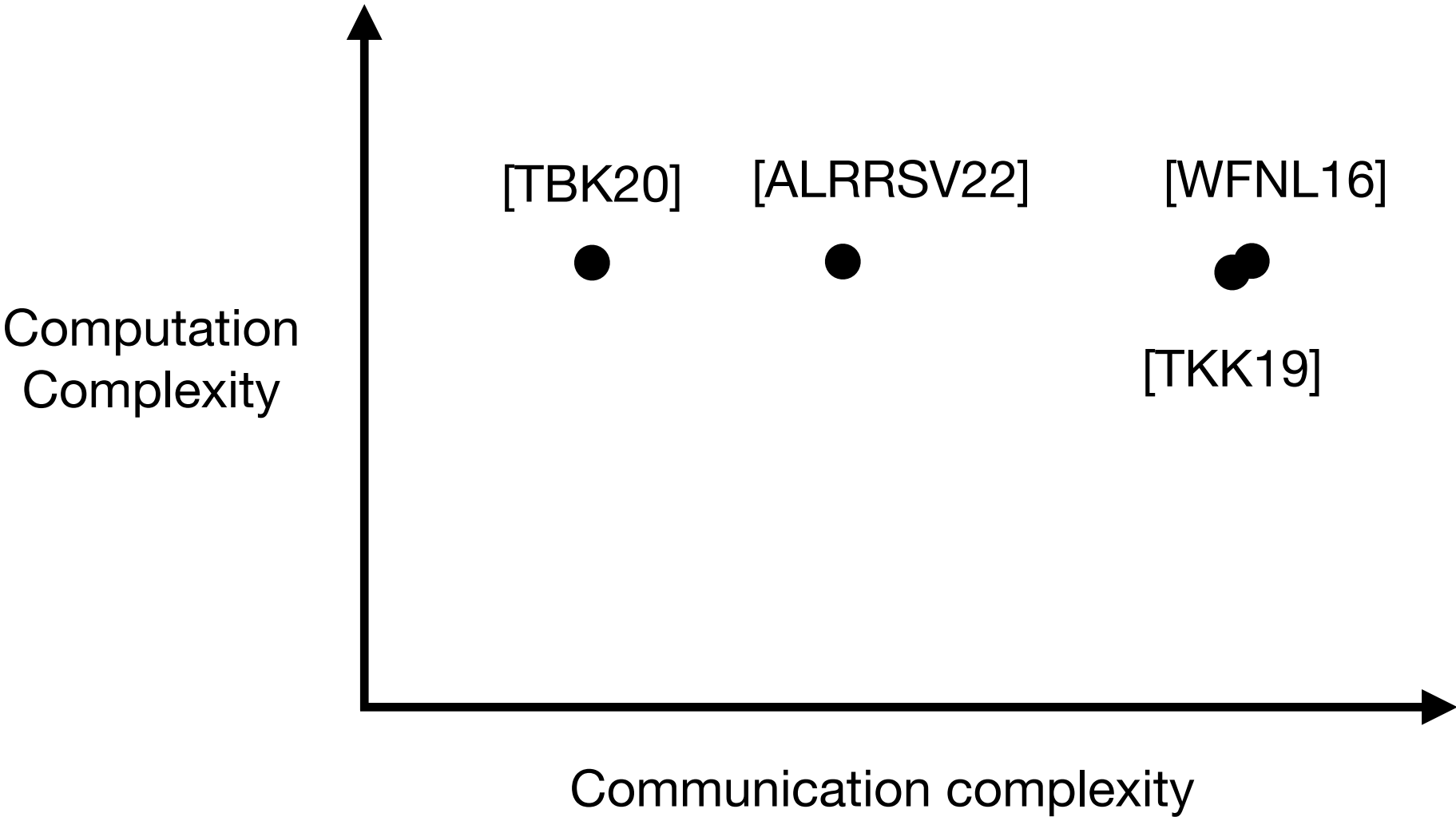


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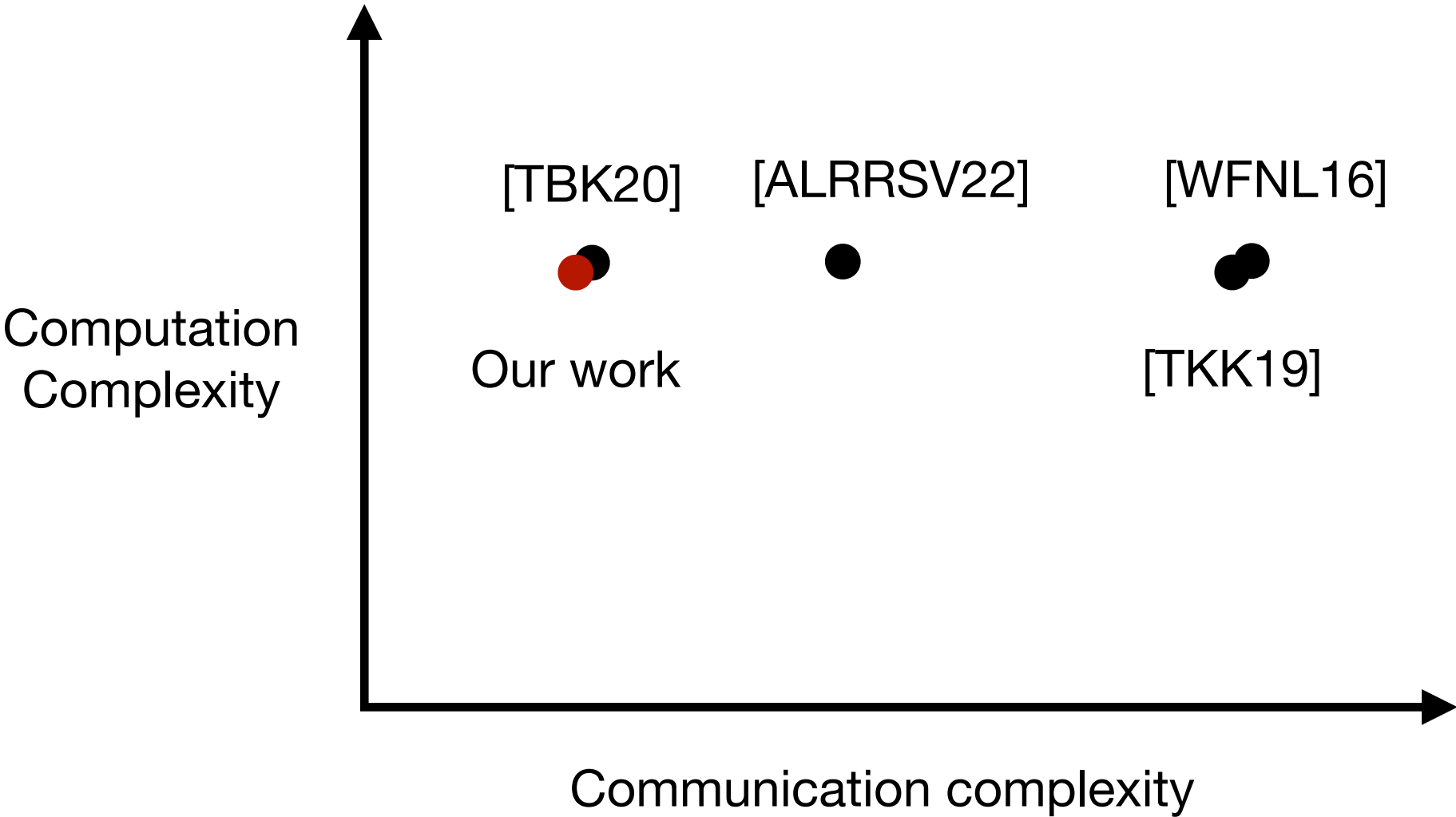
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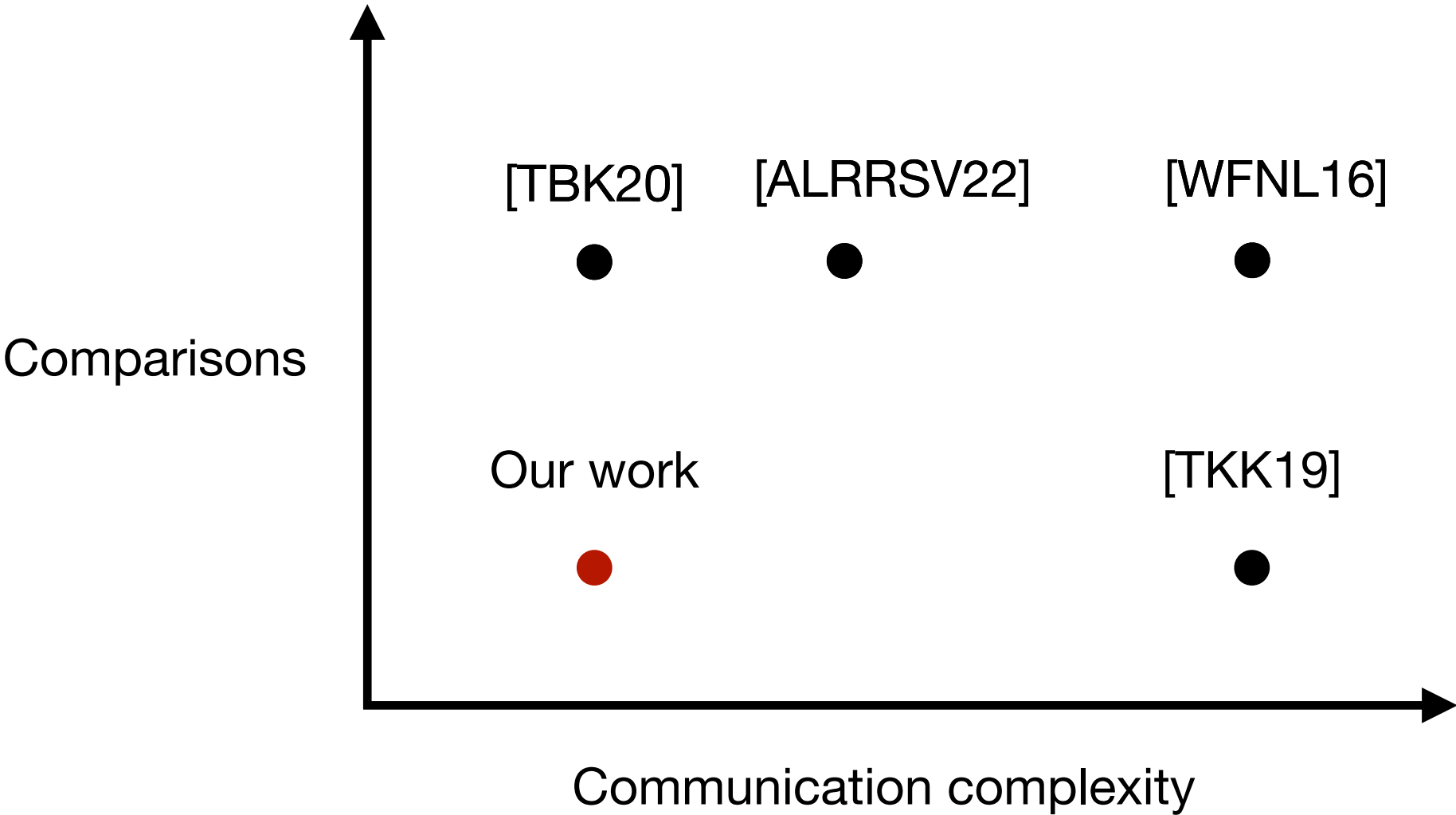
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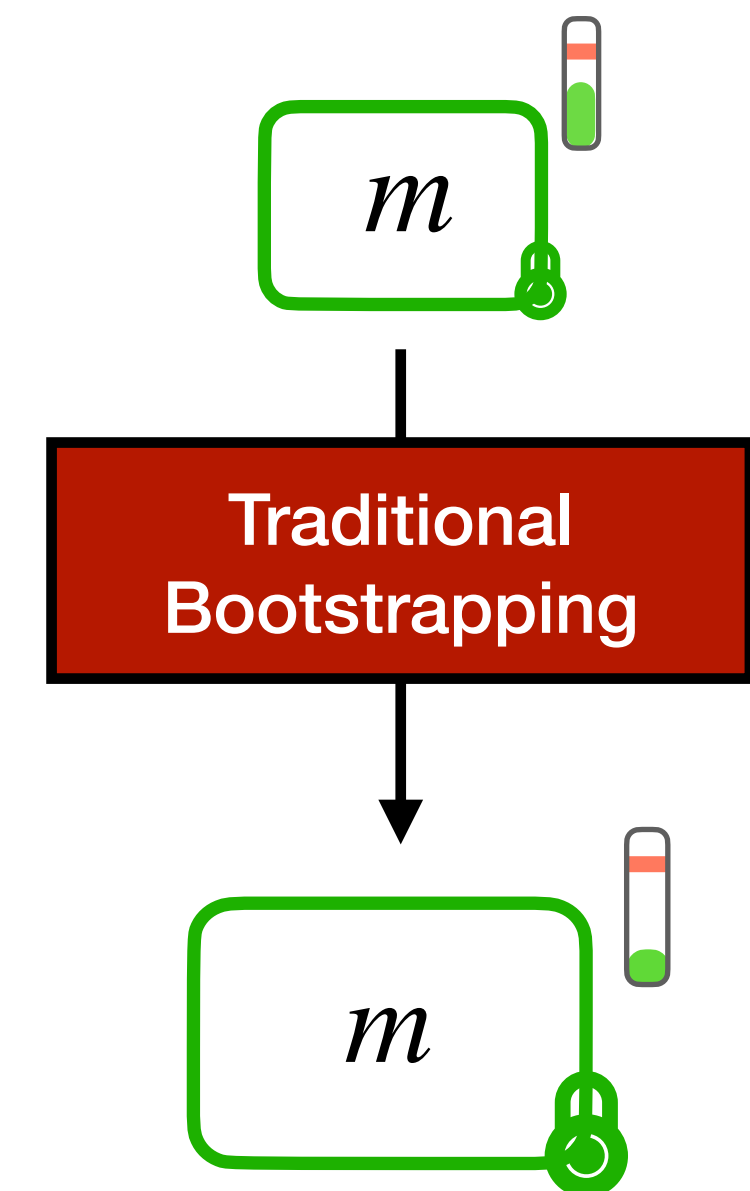
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Preliminaries

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Functional Bootstrapping

Traditional bootstrapping allows to refresh the noise of a ciphertext

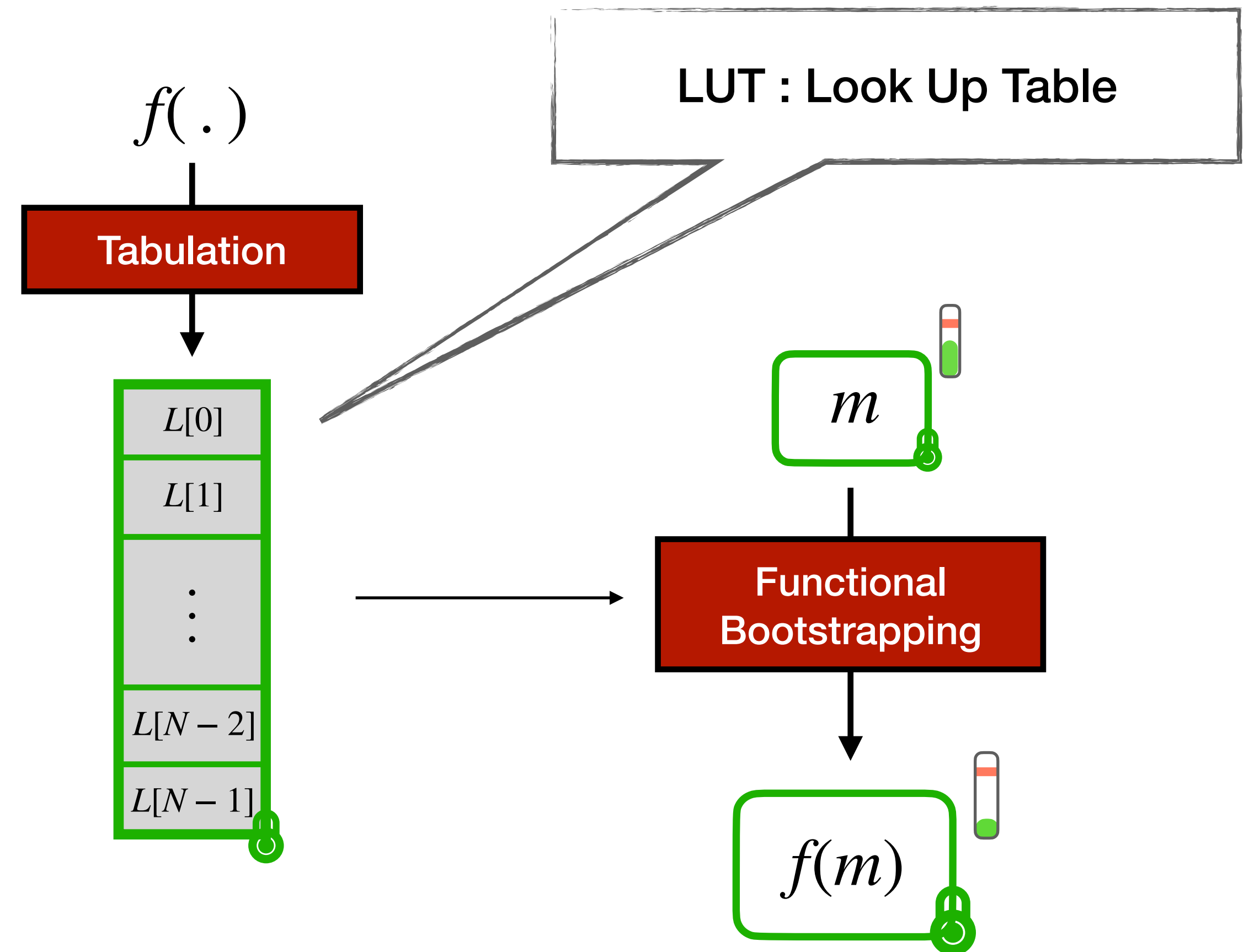


Preliminaries

Functional Bootstrapping

Traditional bootstrapping allows to refresh the noise of a ciphertext

Functional bootstrapping exploit the traditional one to compute arbitrary function



Preliminaries

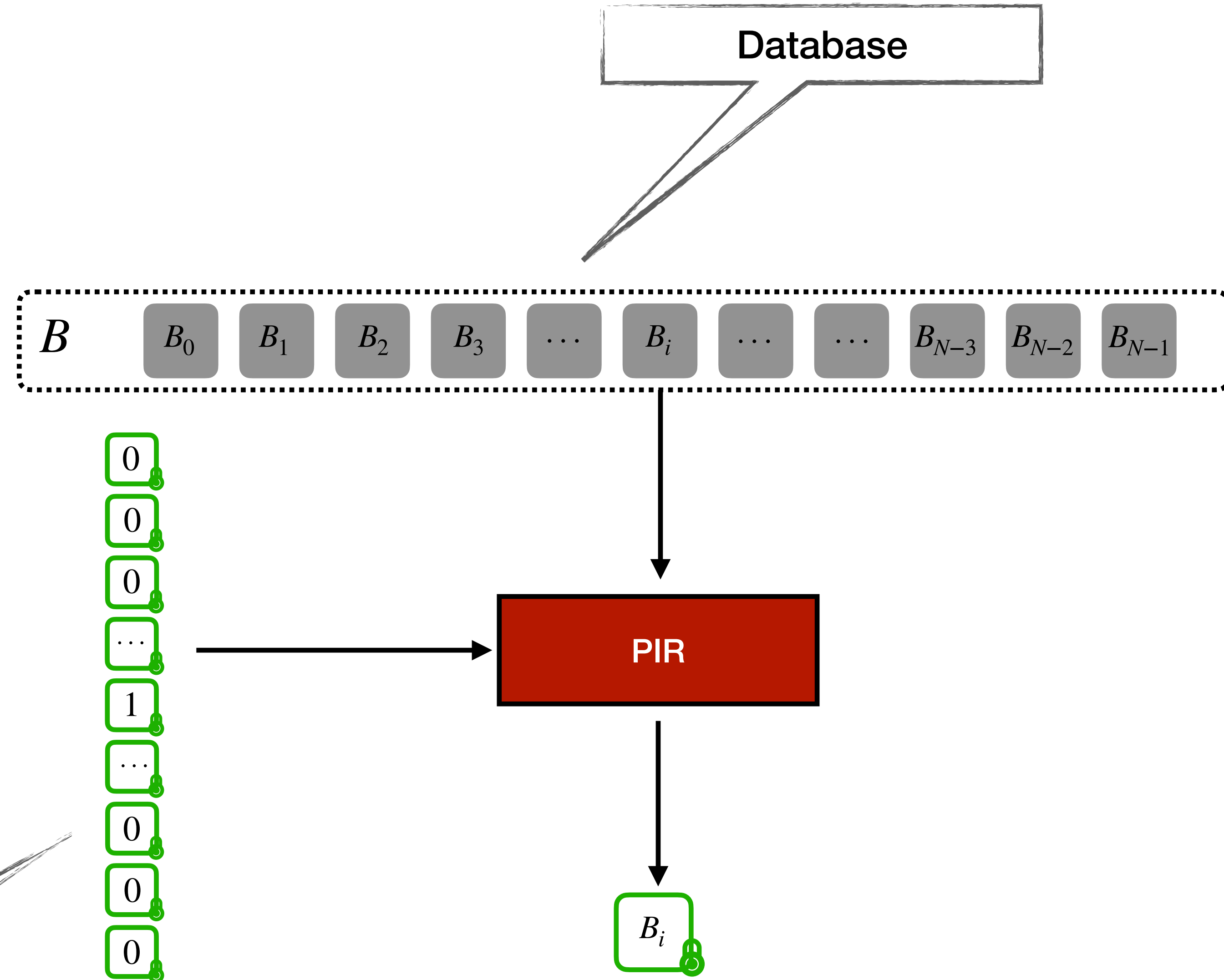
Private Information Retrieval

A PIR can be done by an absorption between the encrypted request and the database

Homomorphic absorption :

$$\boxed{1} \cdot B_i = \boxed{B_i}$$

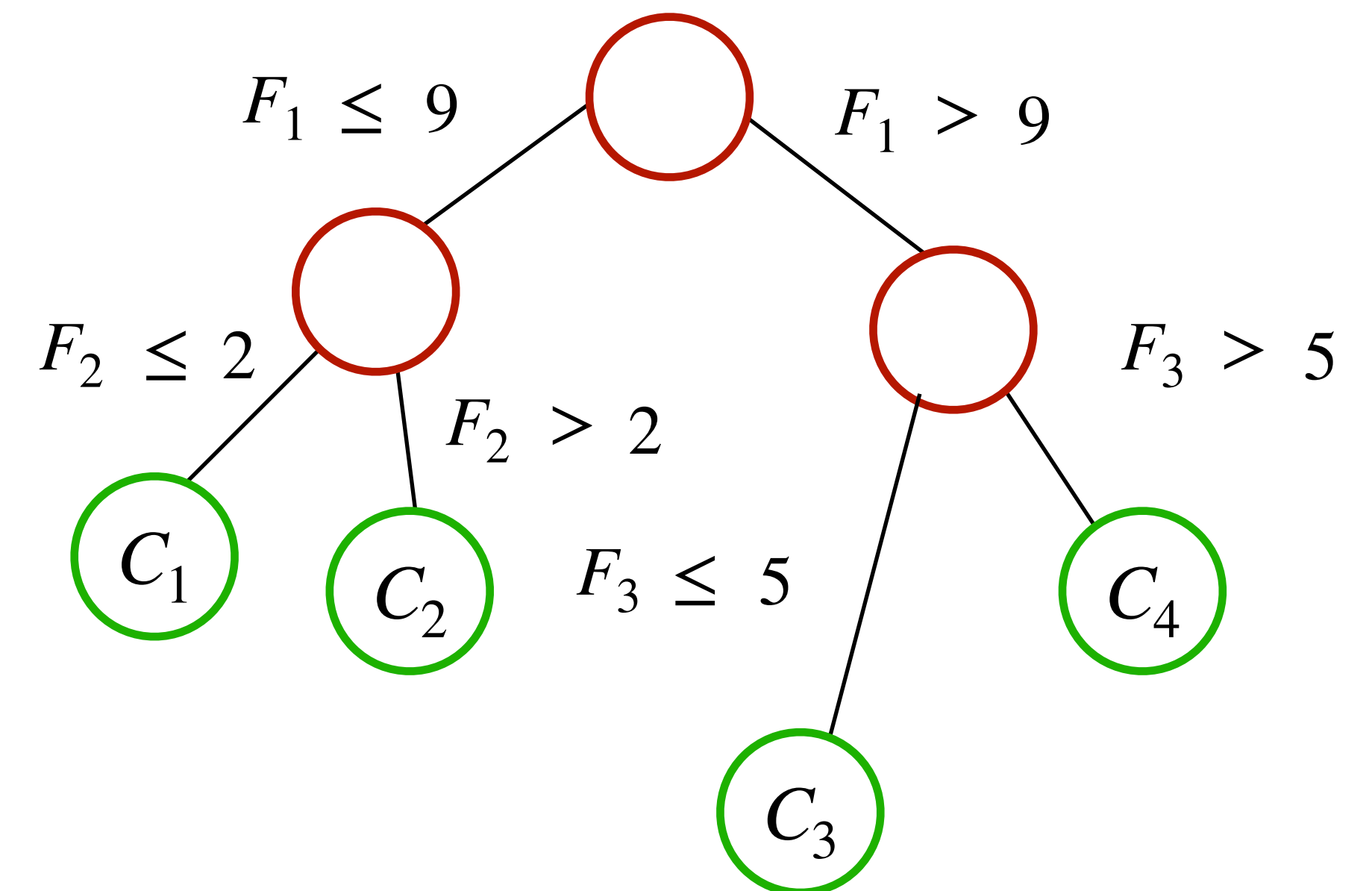
PIR request



Our proposal

Our proposal

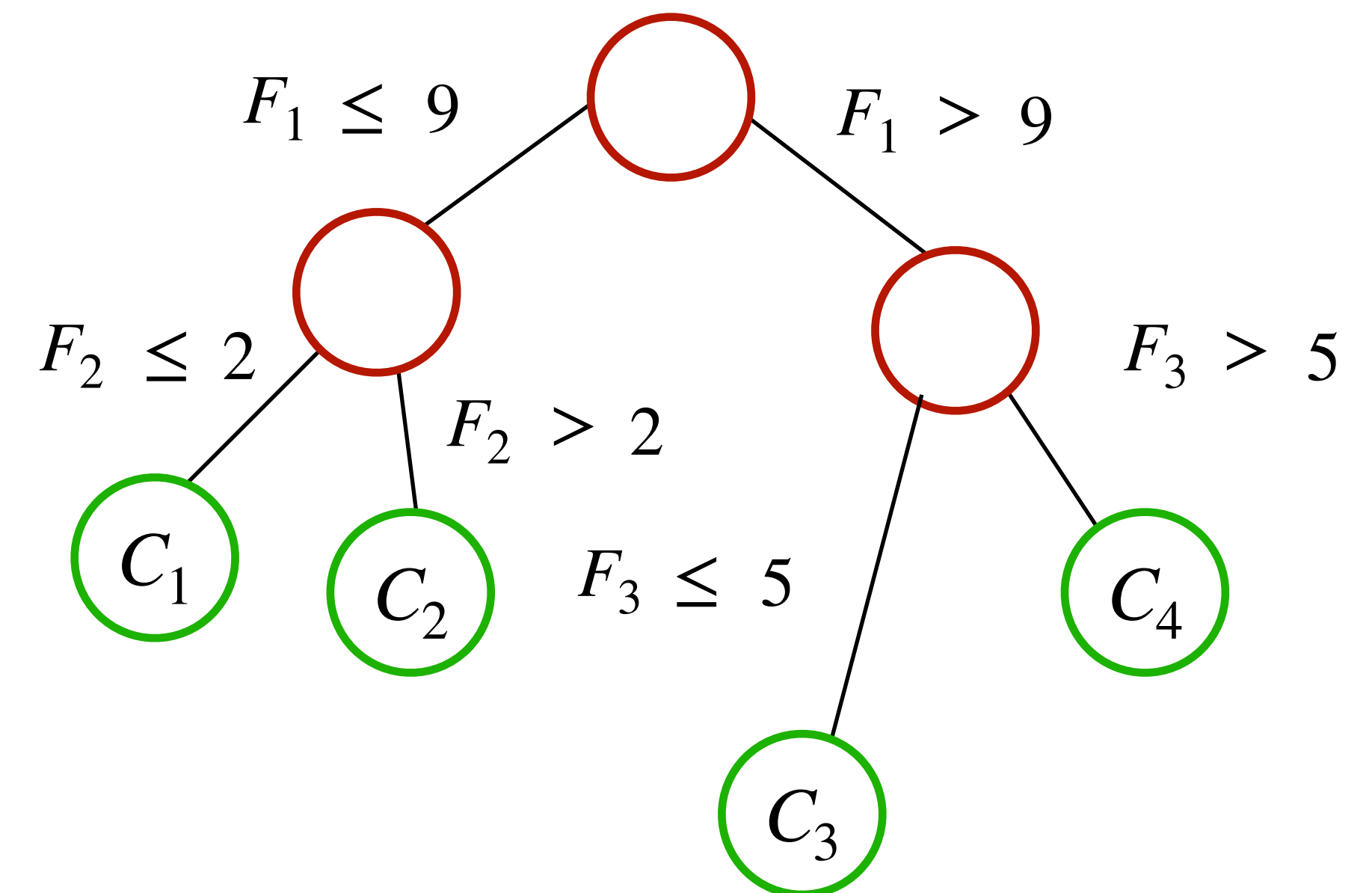
Challenge : reducing the number of comparisons



Our proposal

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To address this challenge, the server has to accomplish two tasks :

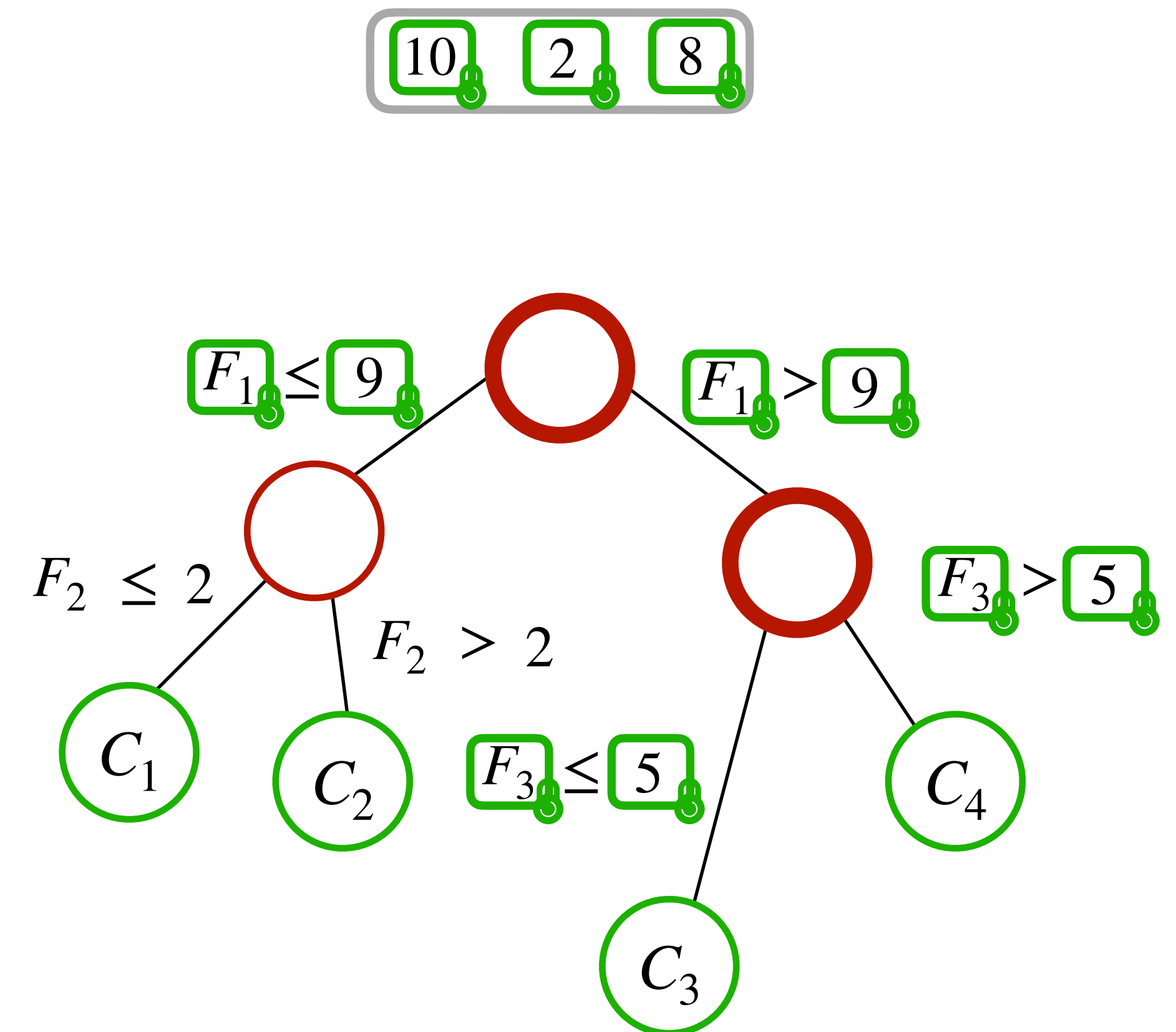


Our proposal

Challenge : reducing the number of comparisons

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1. Blindly select the node to evaluate

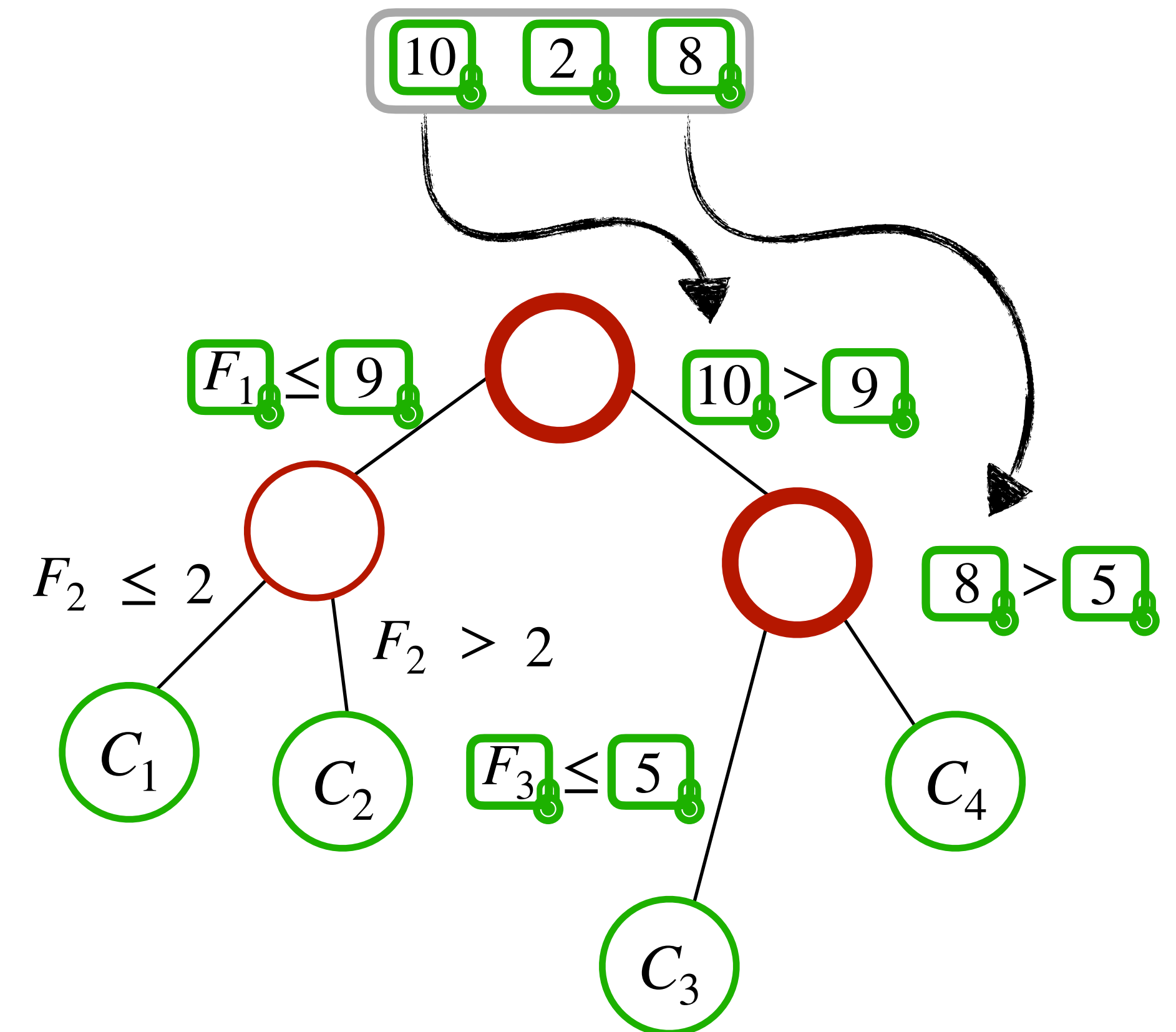


Our proposal

Challenge : reducing the number of comparisons

To address this challenge, the server has to accomplish two tasks :

1. Blindly select the node to evaluate
2. Blindly select the attribute without getting any knowledge



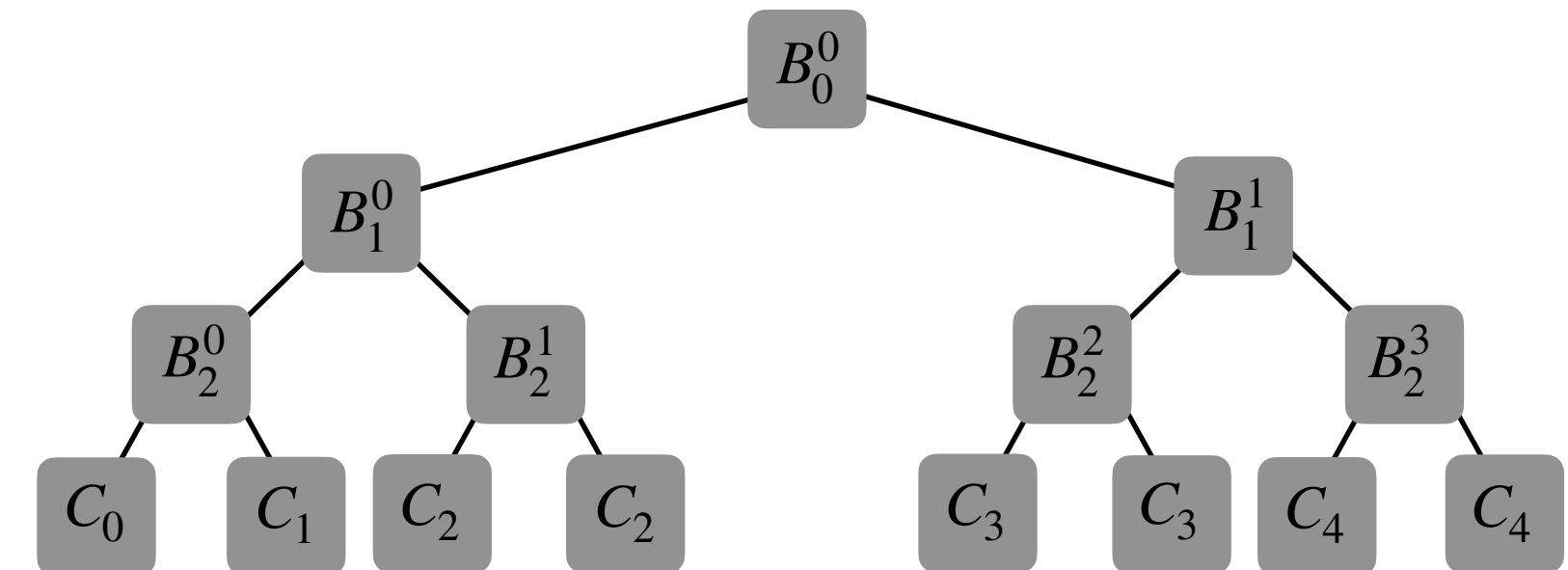
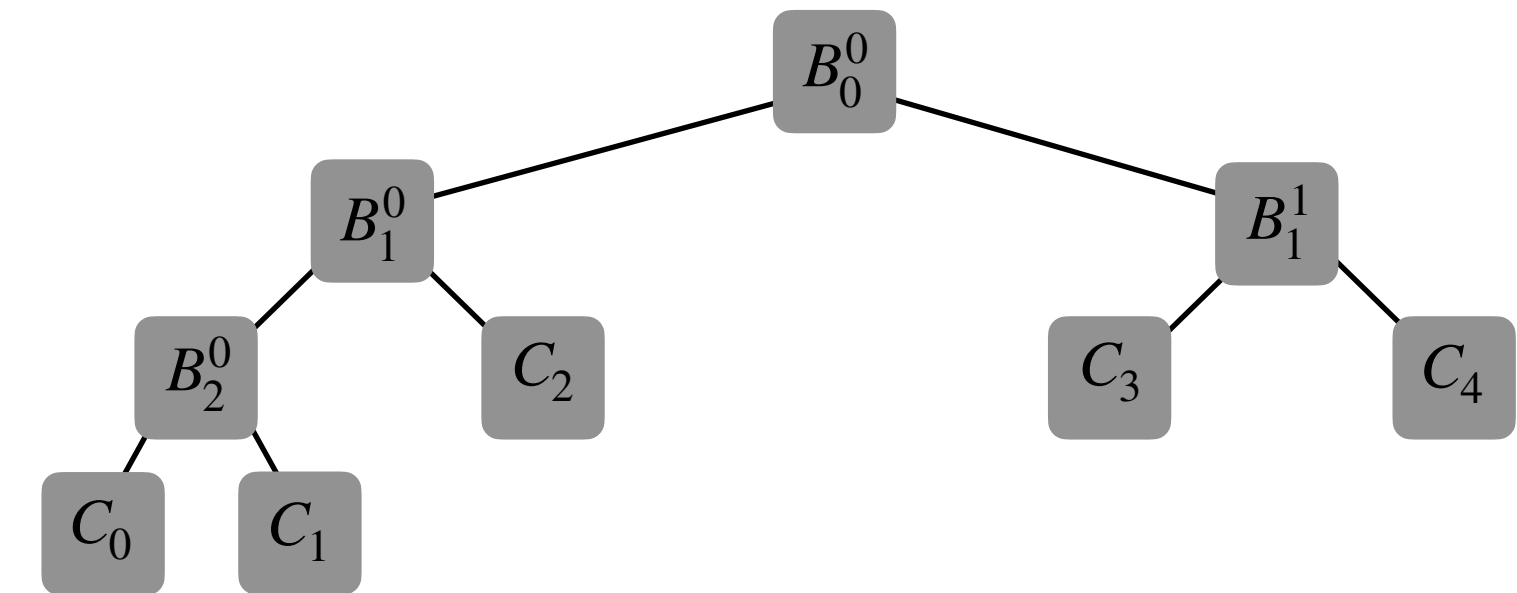
Our proposal

Impact on data structure

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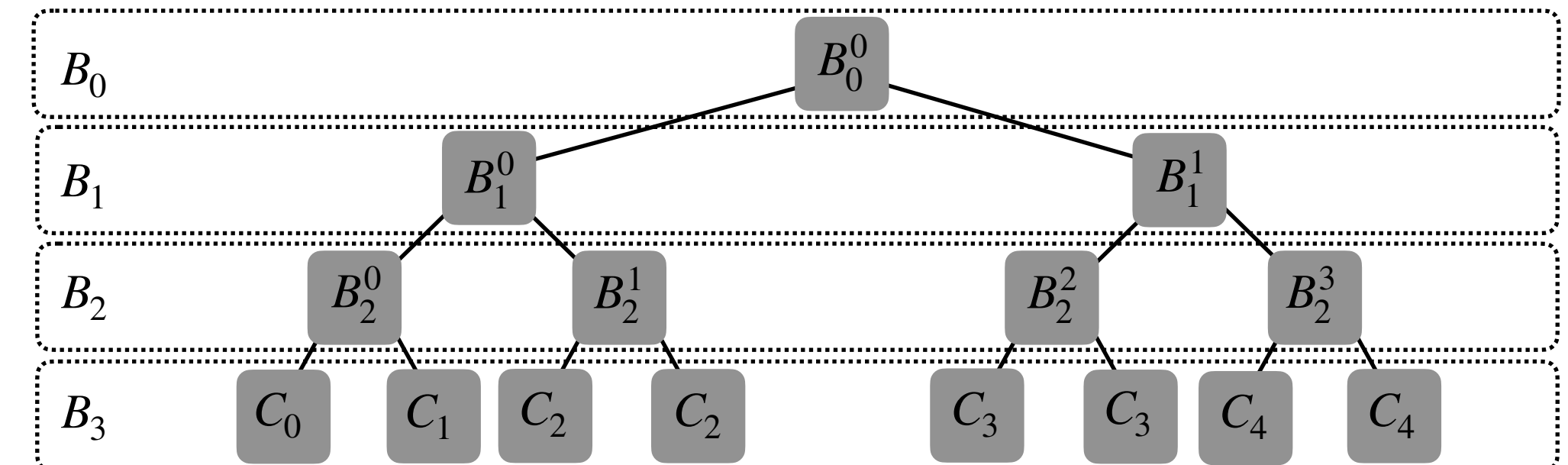
1. We complete the decision tree by adding some dummy nodes if necessary



Our proposal

Impact on data structure

1. We complete the decision tree by adding some dummy nodes if necessary
2. We consider the tree as a database composed by d sub-databases called « levels »



Our proposal

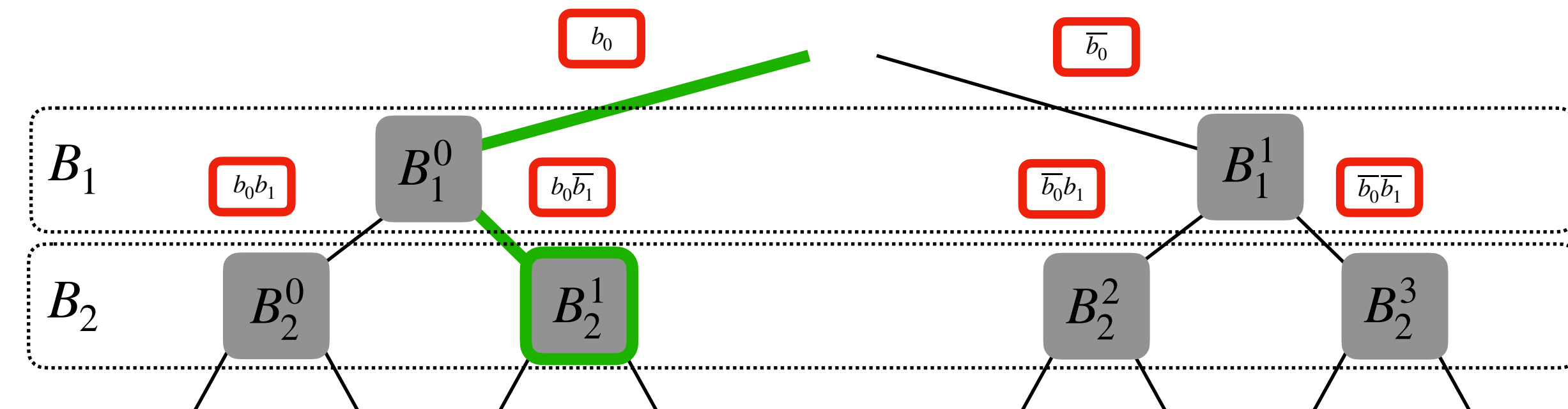
New primitive : Blind Node Selection

Each level, except the root, is associated to a new encrypted bit b_j

This bit is used to build an accumulator bit associated to each node

Only one of this accumulator bit is set

Finally, we get the correct node a-la-PIR



$$B_2^1 = b_0 b_1 \cdot B_2^0 + b_0 \bar{b}_1 \cdot B_2^1 + \bar{b}_0 b_1 \cdot B_2^2 + \bar{b}_0 \bar{b}_1 \cdot B_2^3$$

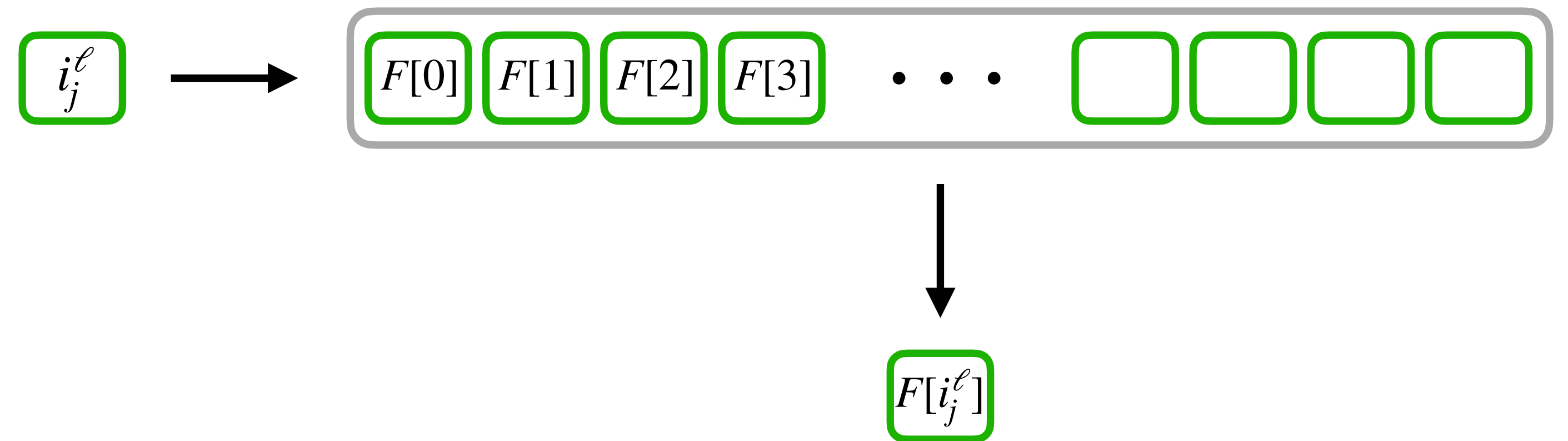
Our proposal

New primitive : Blind Array Access

The idea : use the feature vector as a LUT in the functional bootstrapping

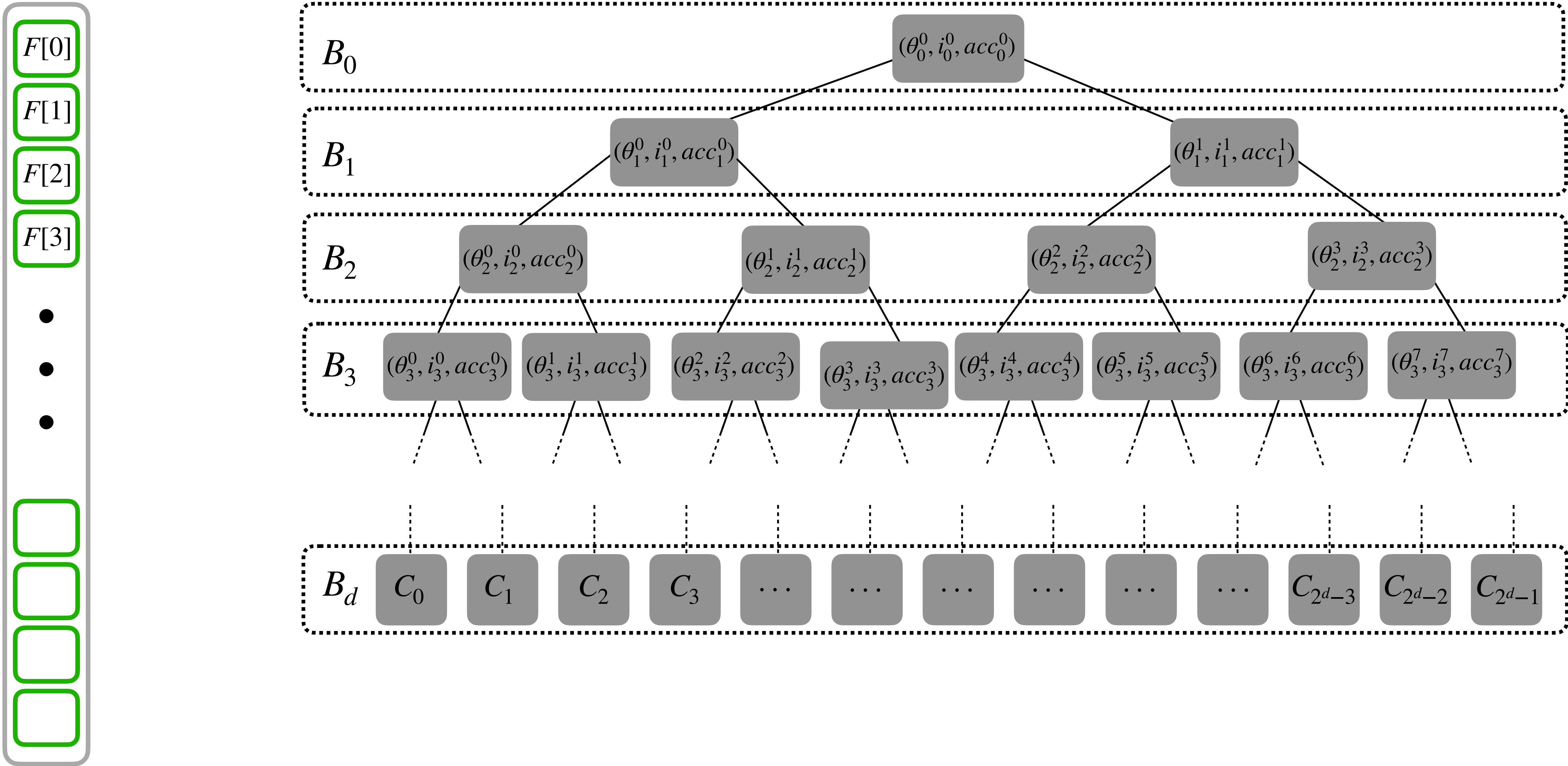
The message to be bootstrapped is the index encrypted

Improvement : use the binary decomposition of the index as a bootstrapping key



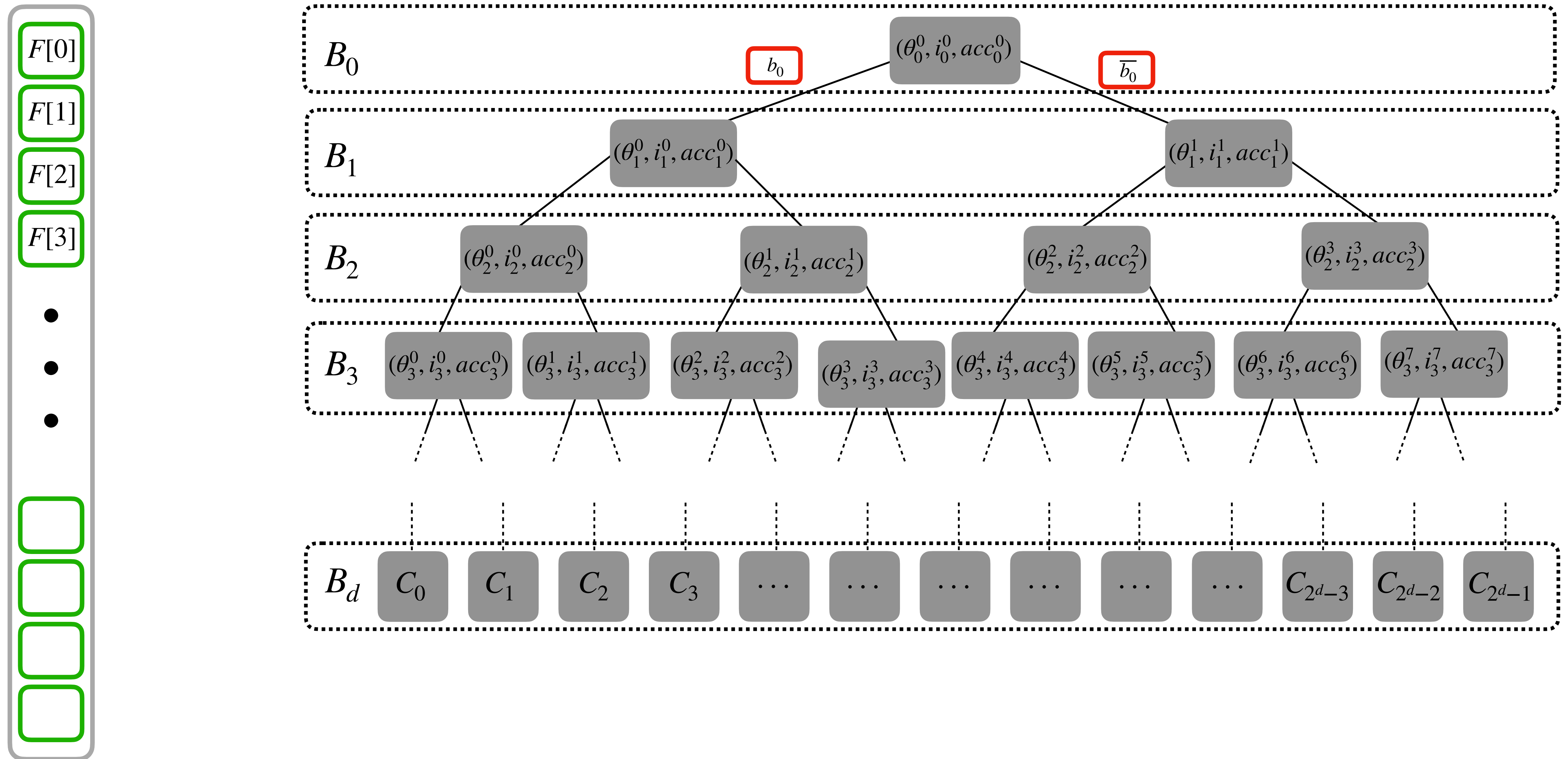
Client's Features

Server's Decision Tree



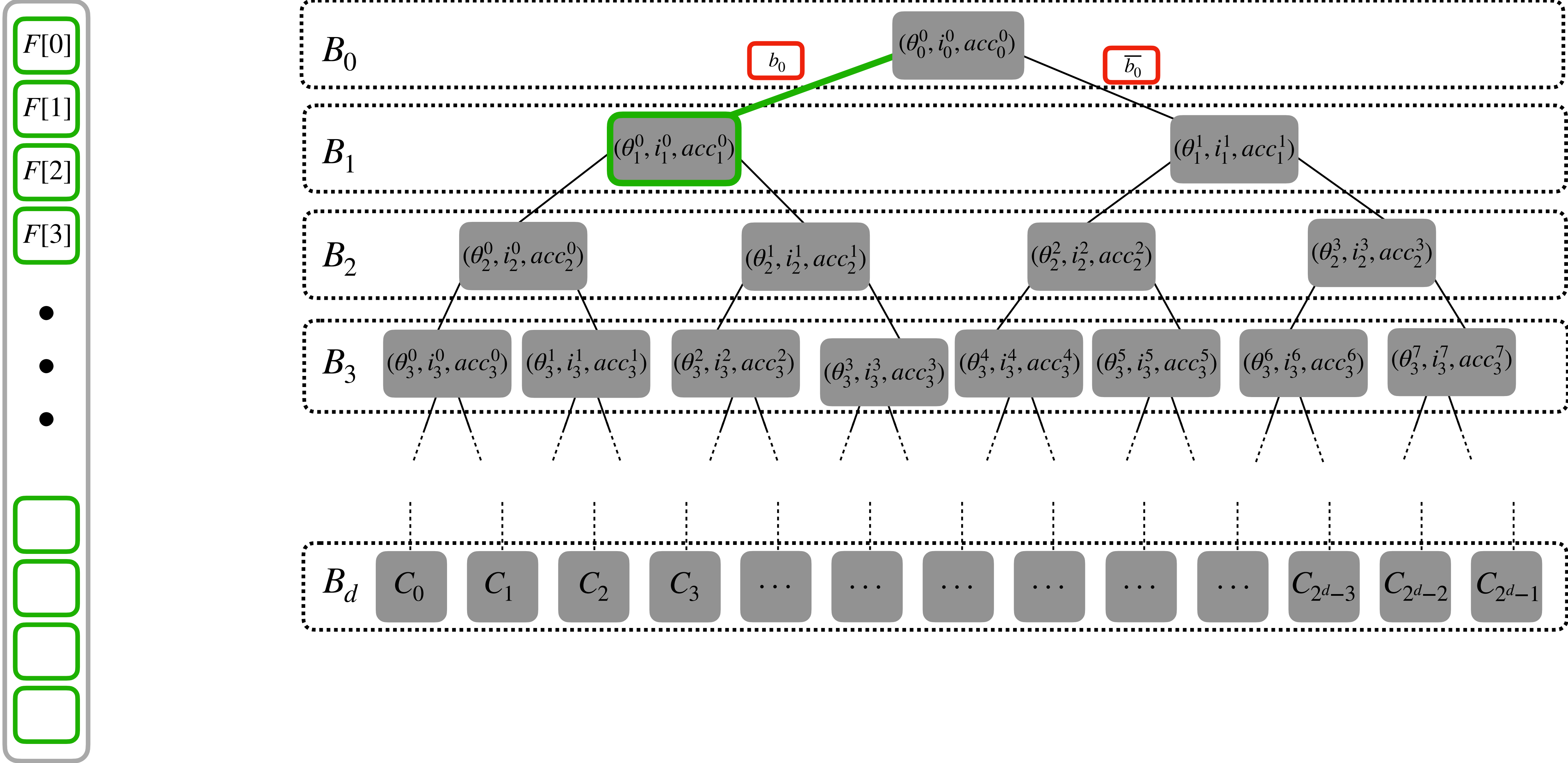
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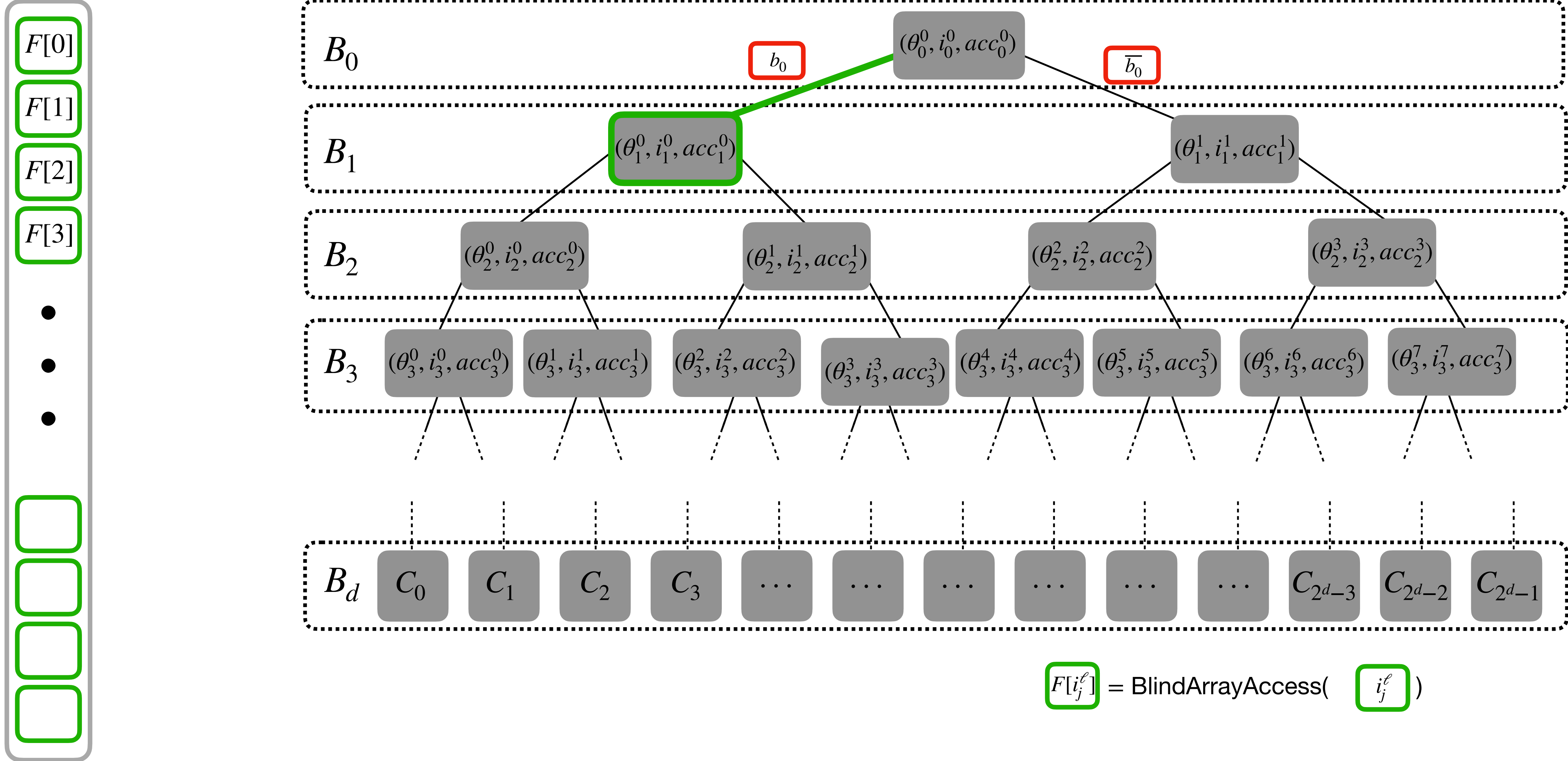
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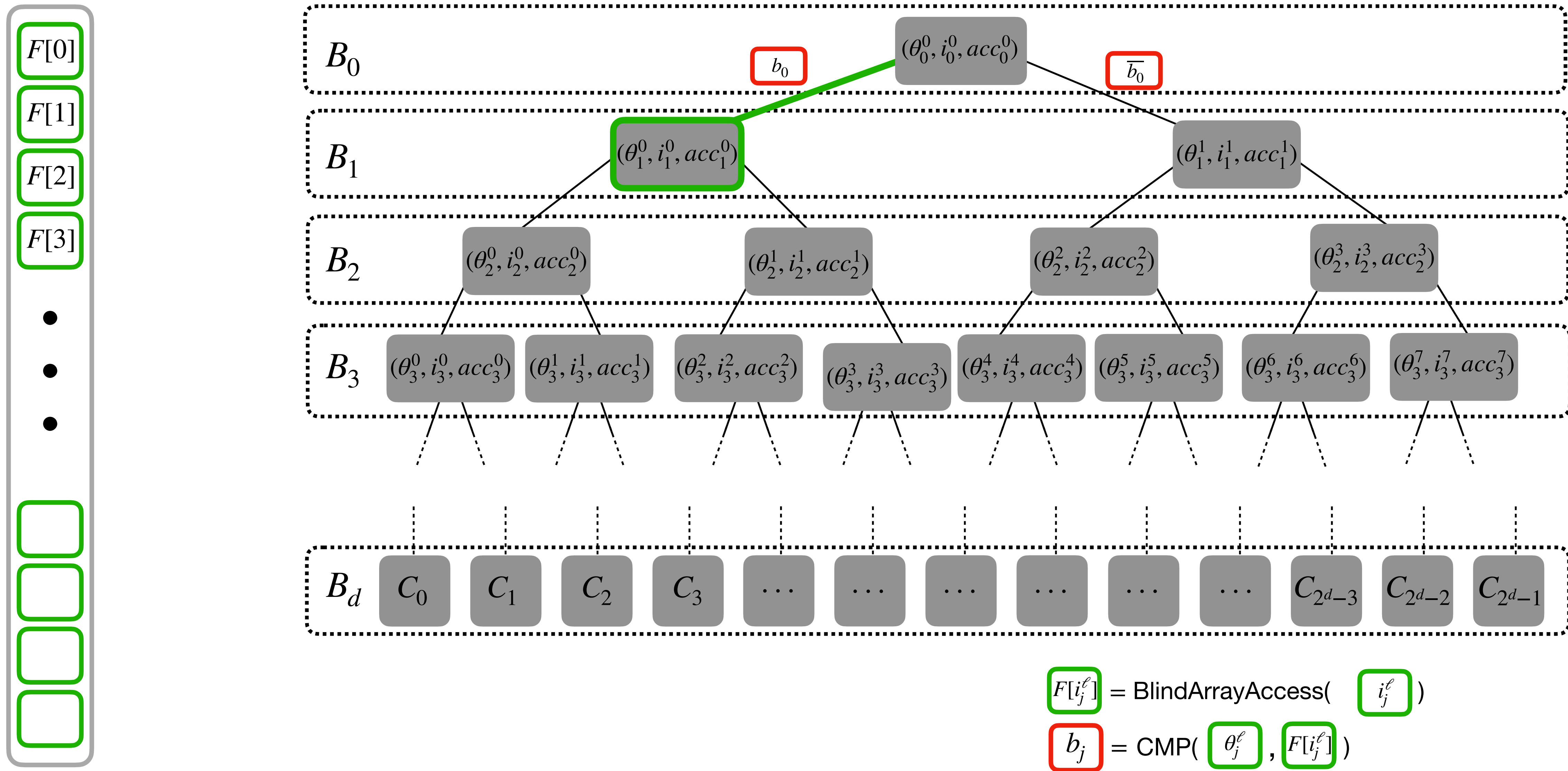
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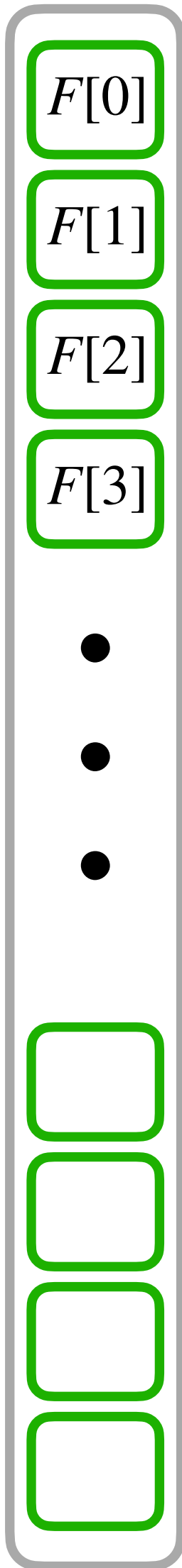


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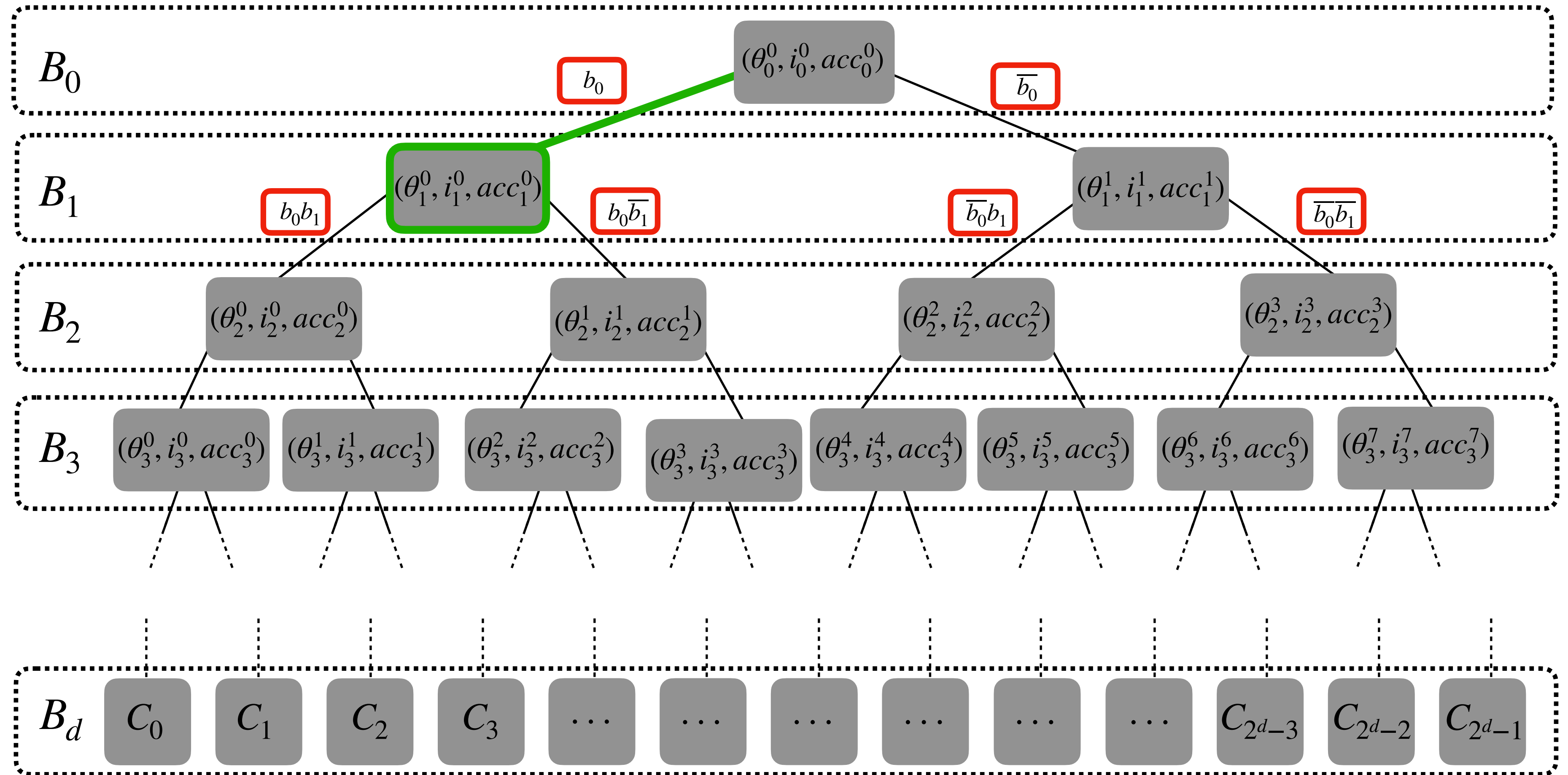
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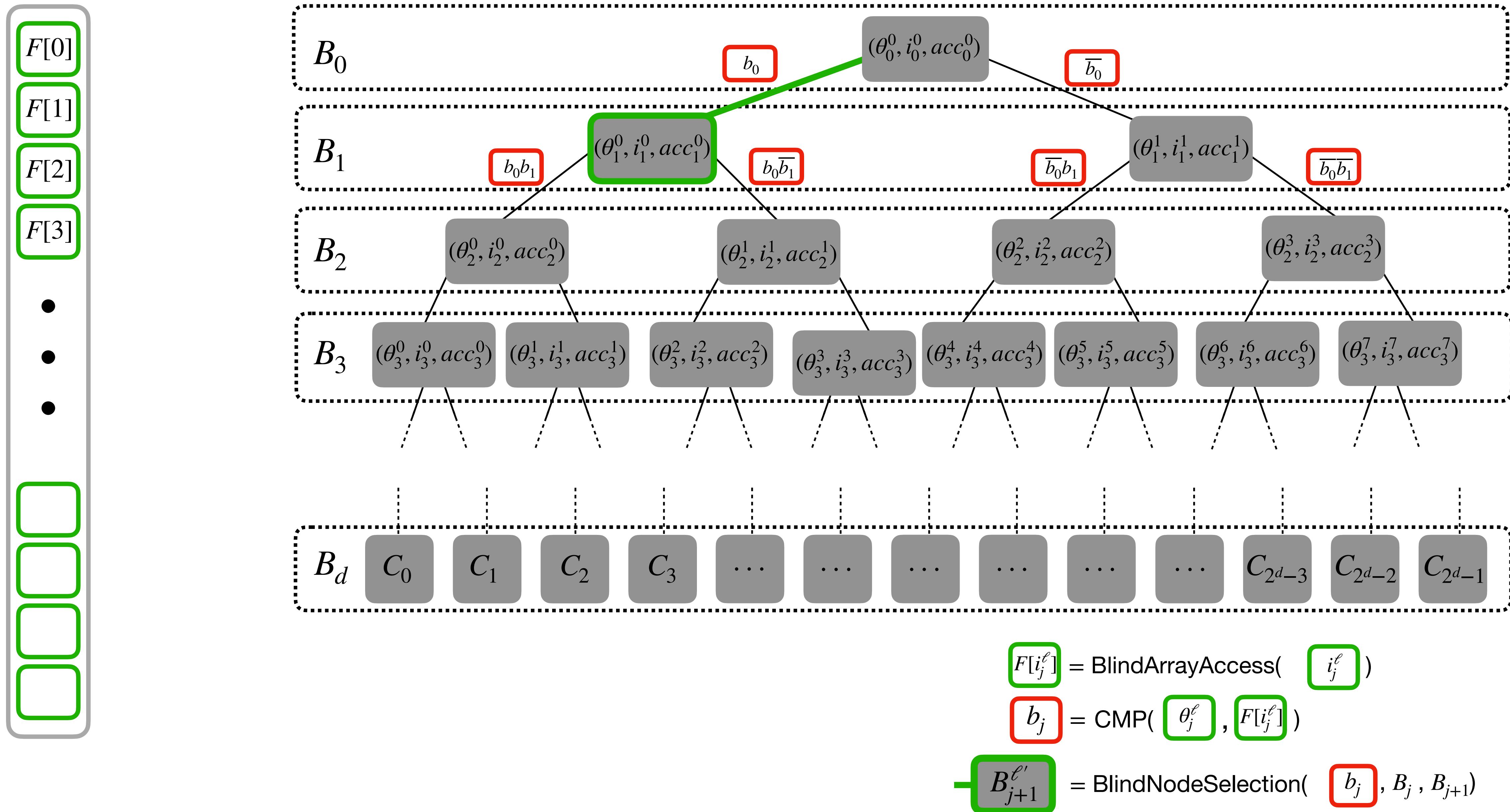


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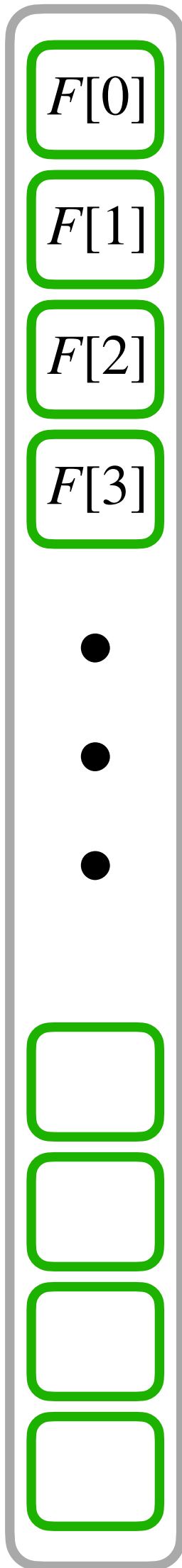
$$b_j = \text{CMP}(\theta_j^\ell, F[i_j^\ell])$$

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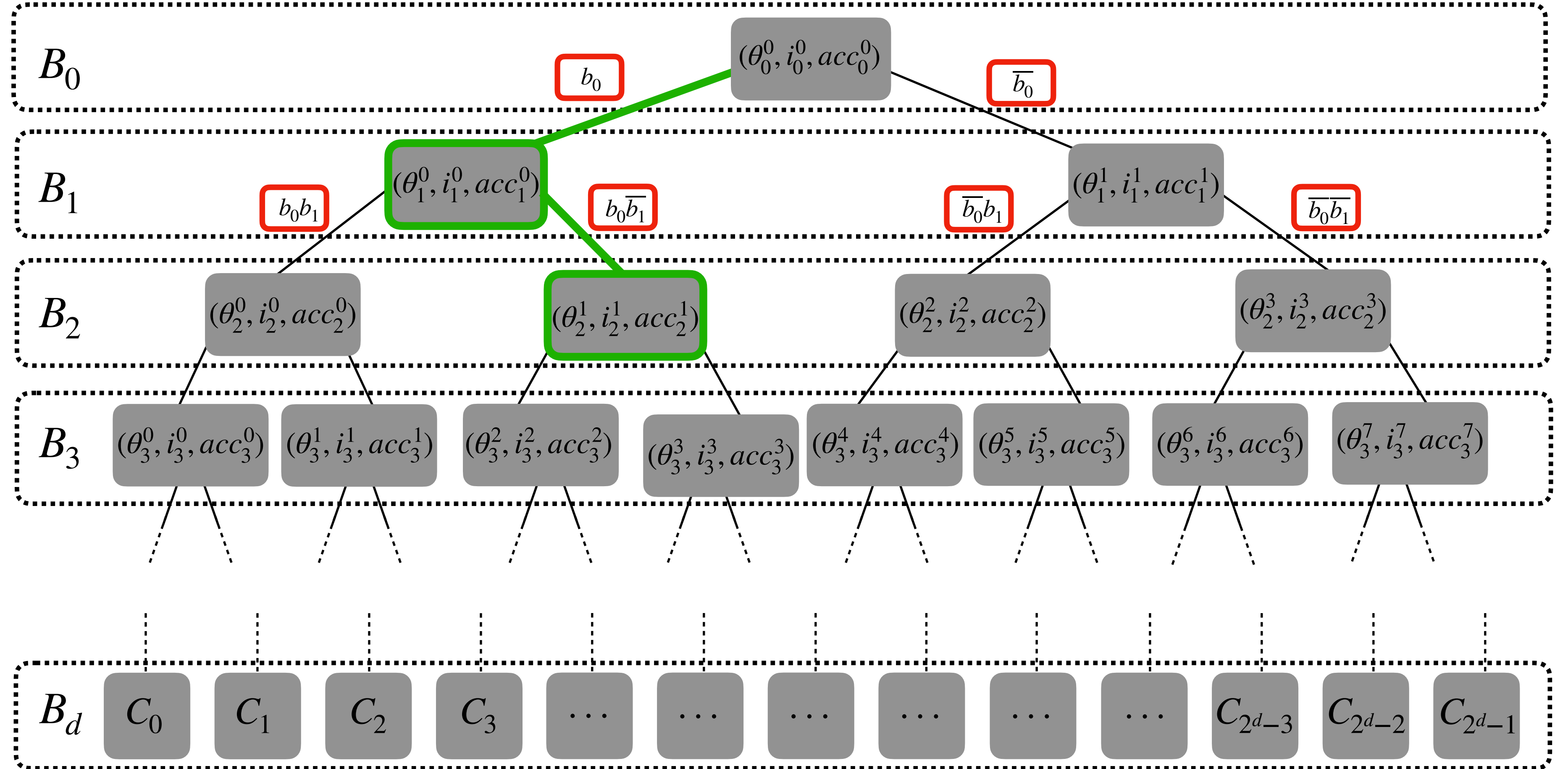
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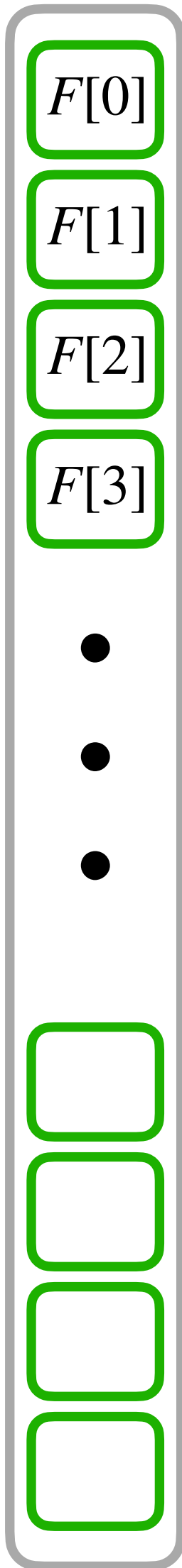


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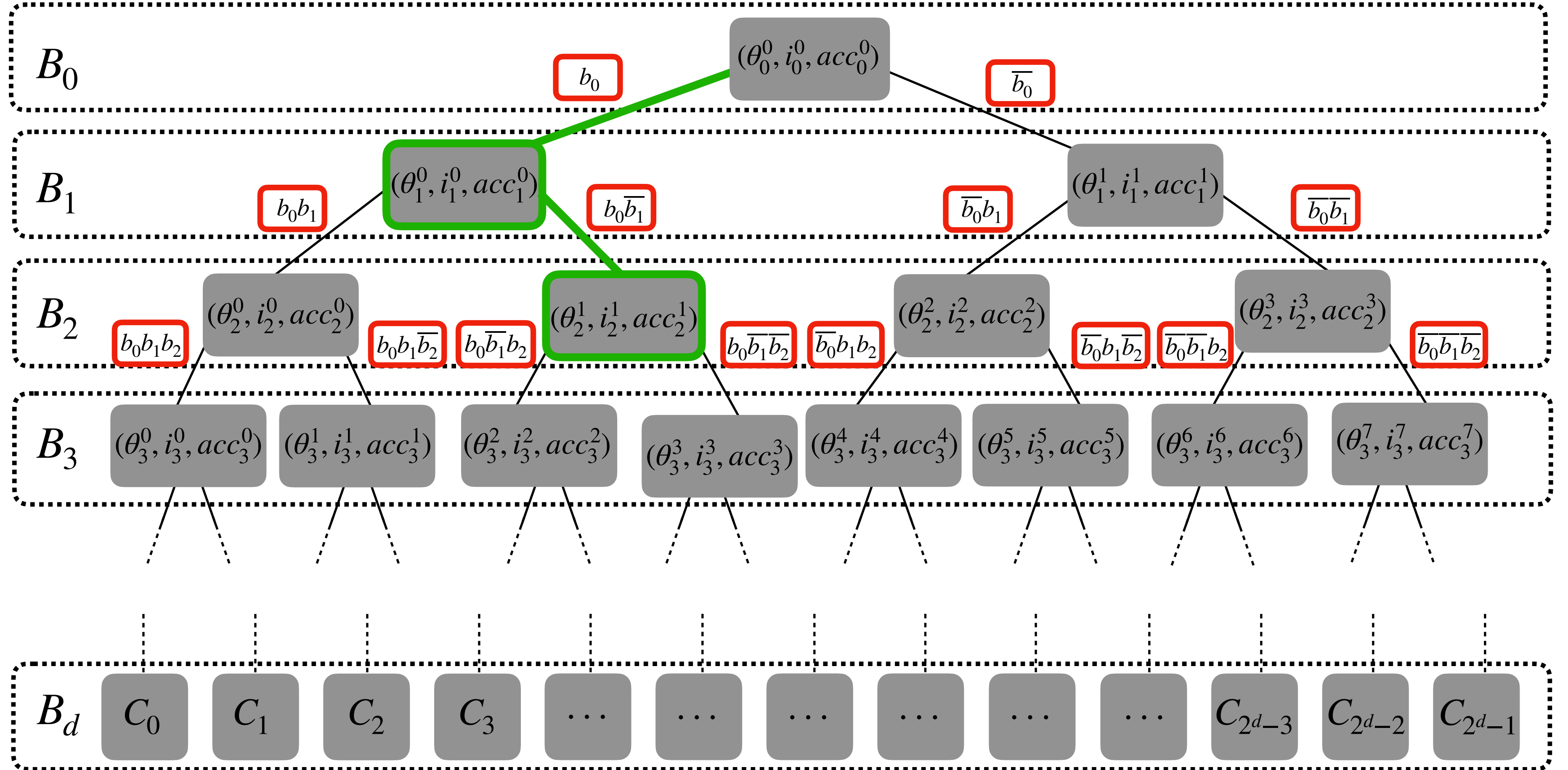


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Client's Features



Server's Decision Tree

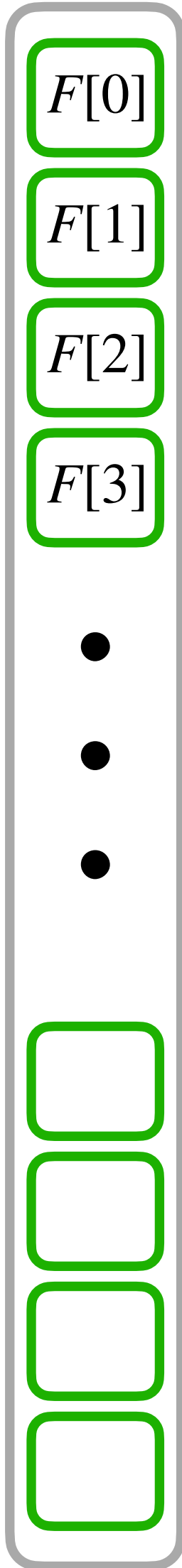


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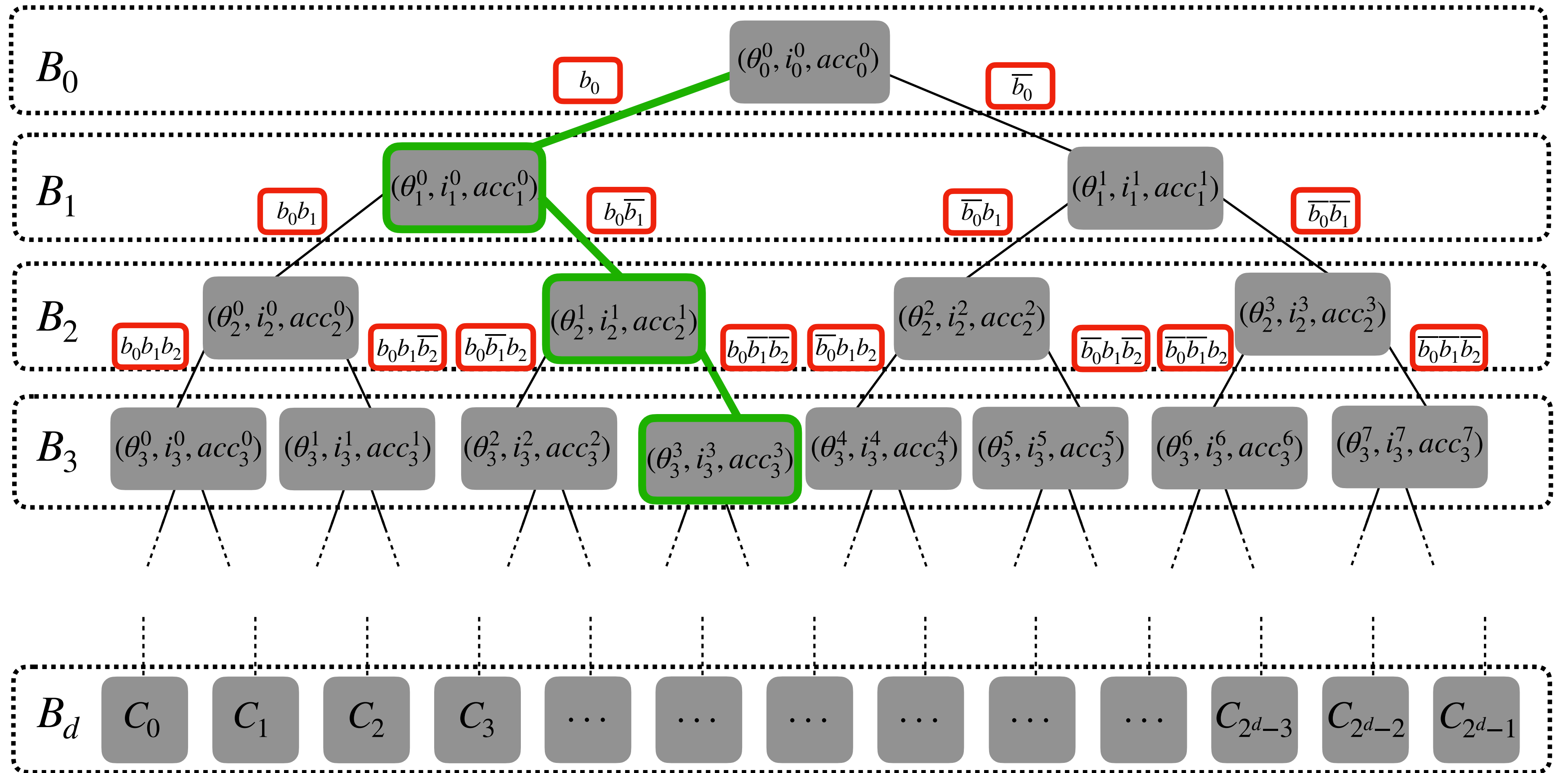
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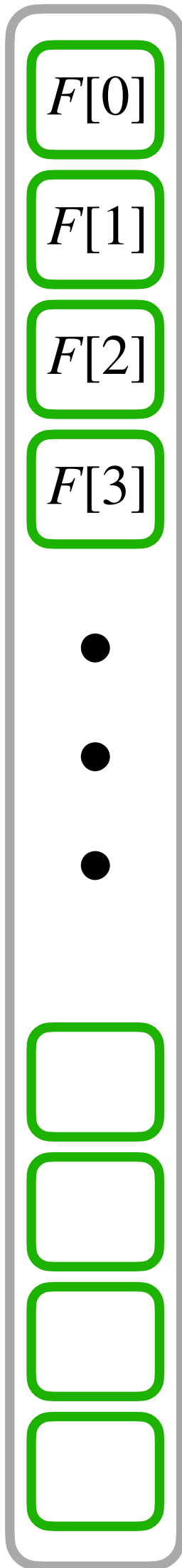


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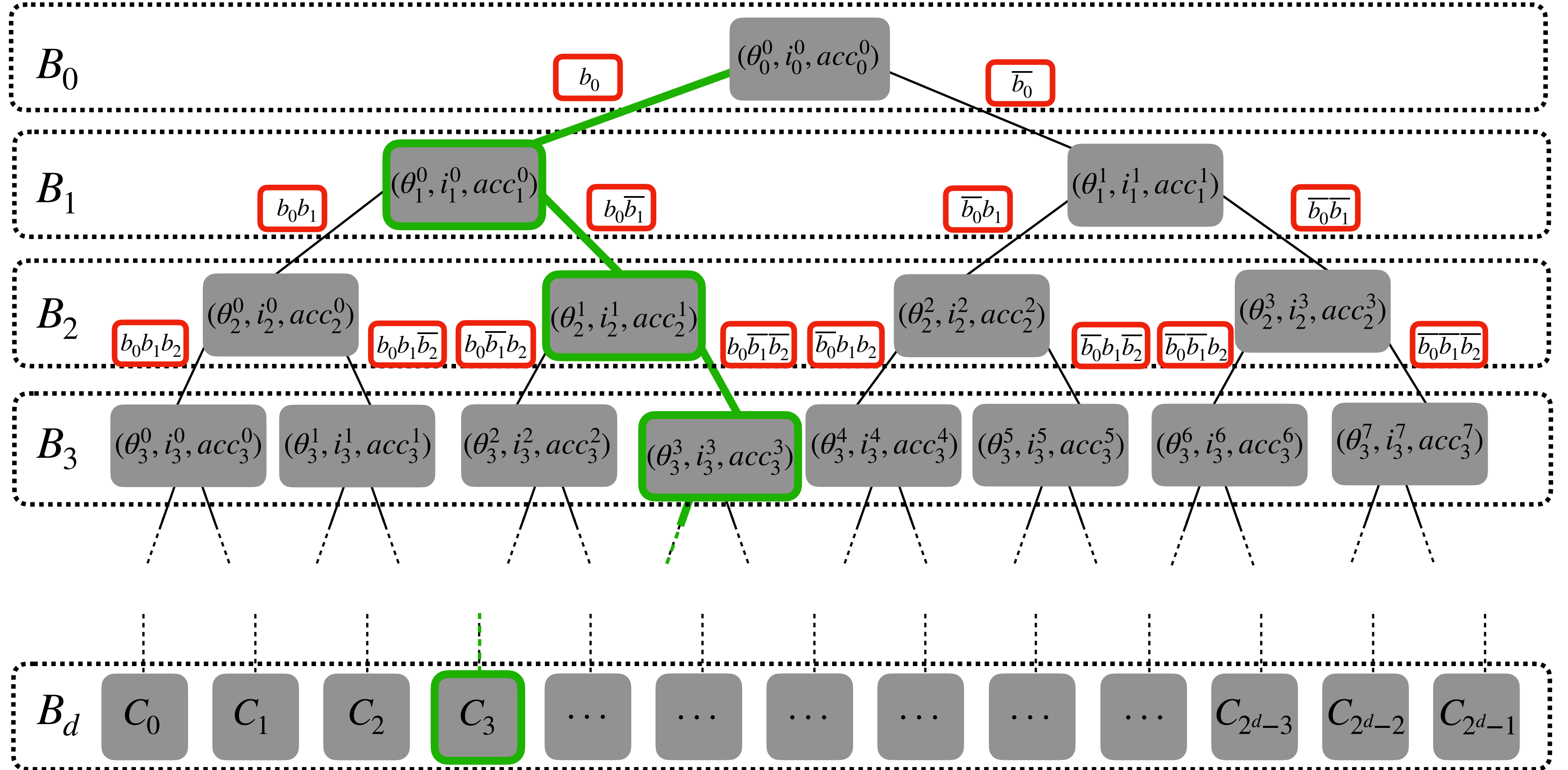
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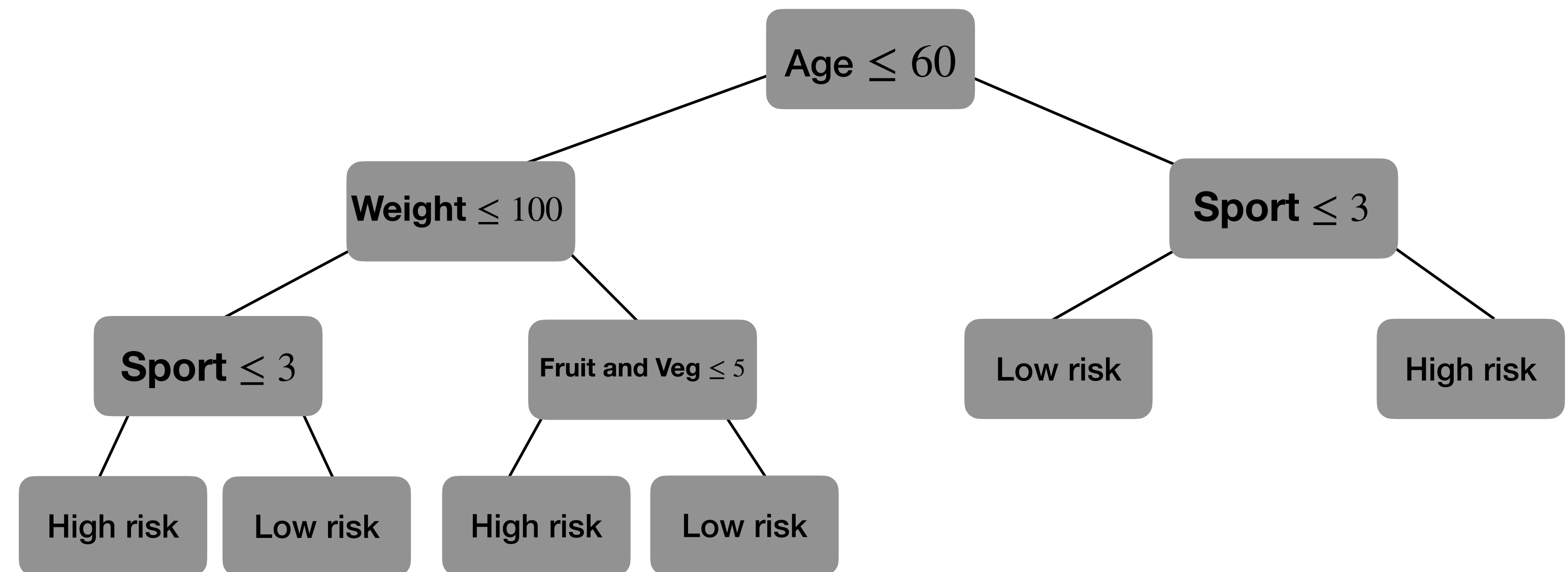
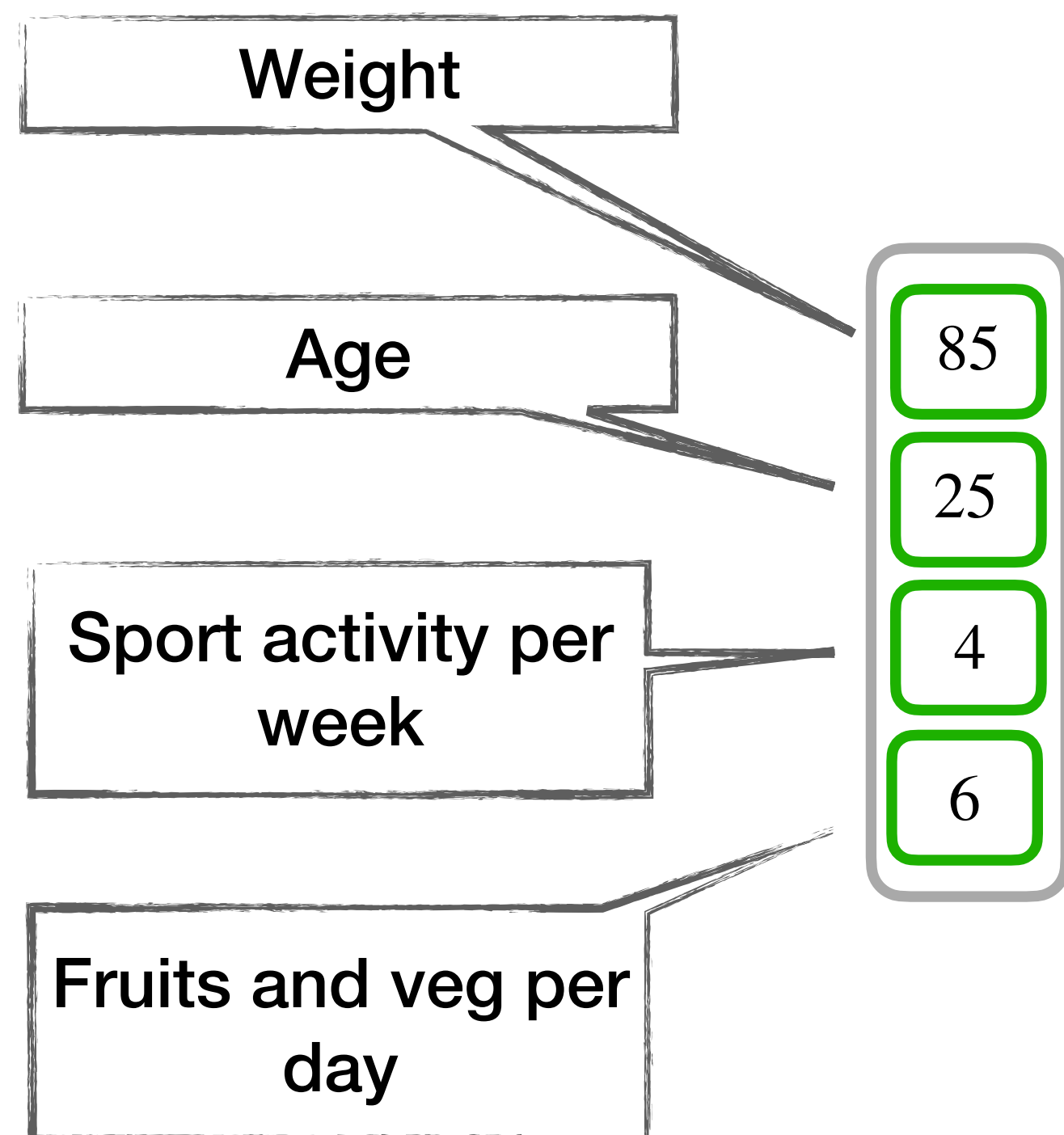
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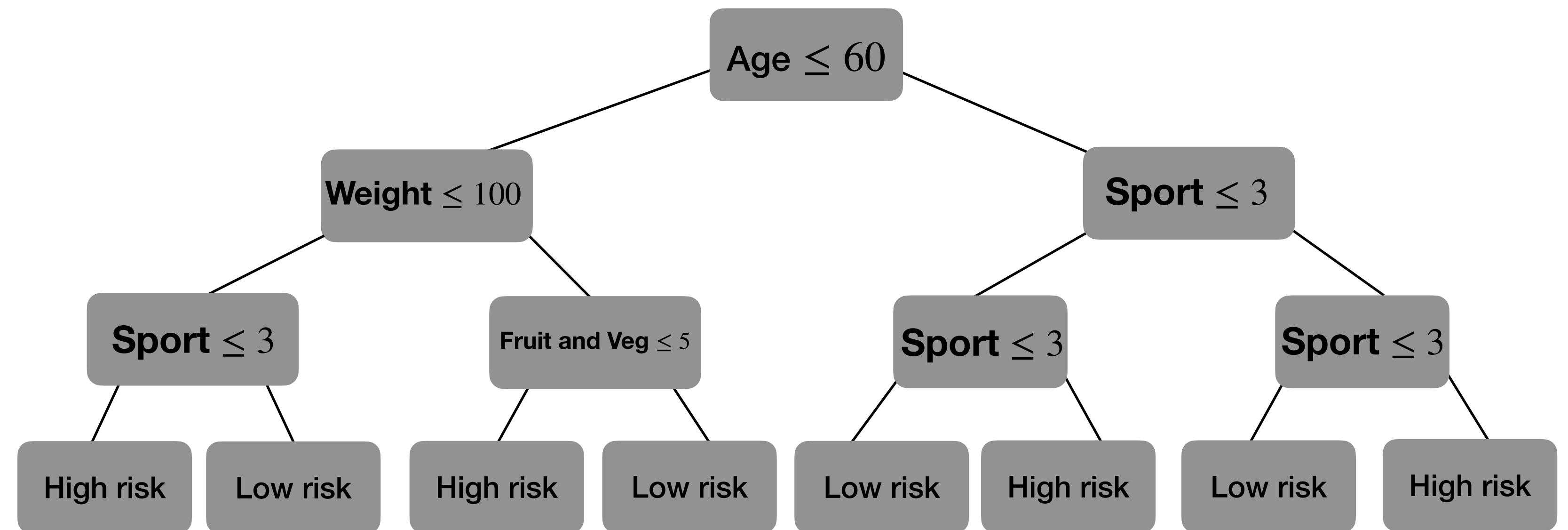
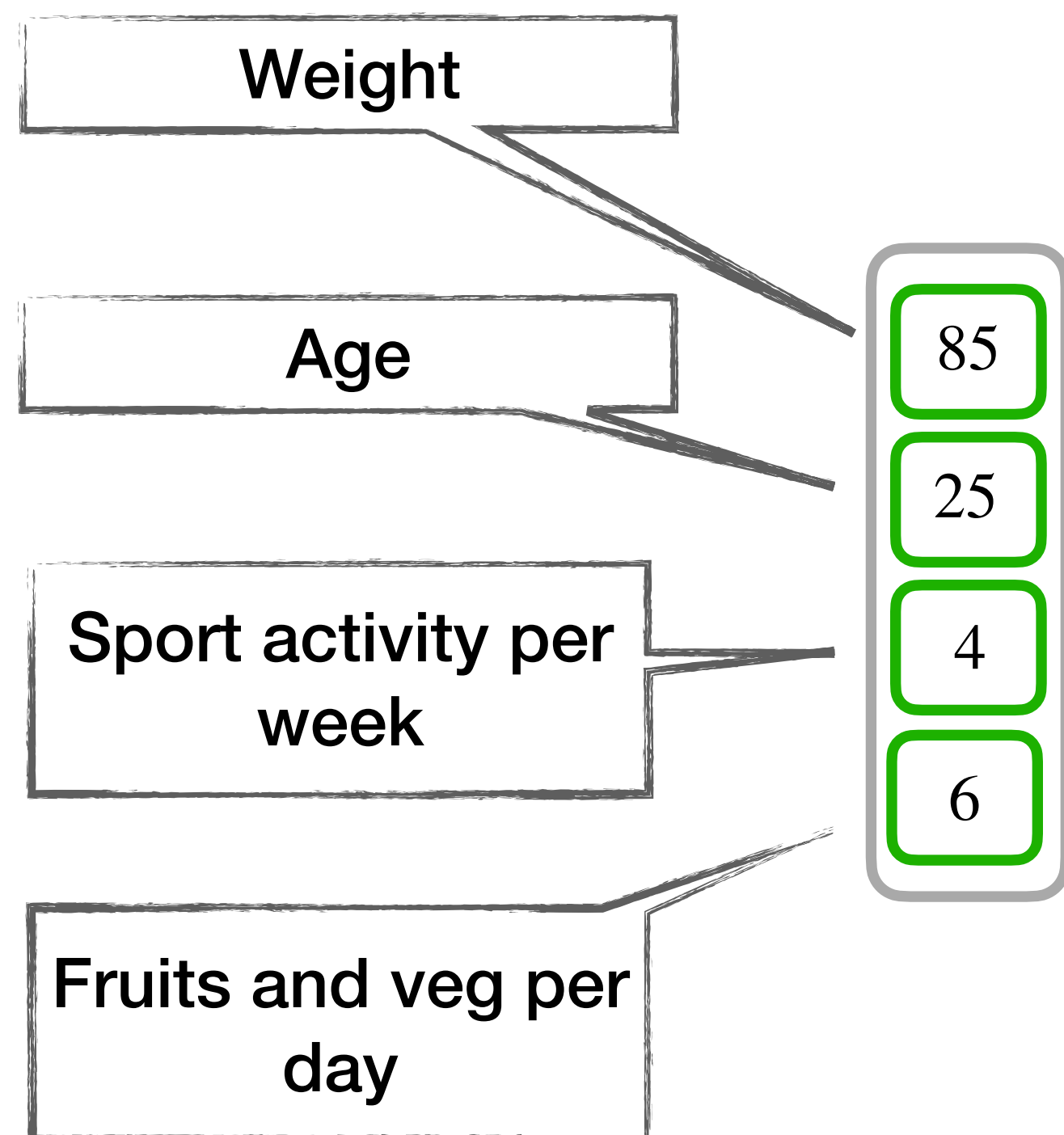
Our proposal

Toy example



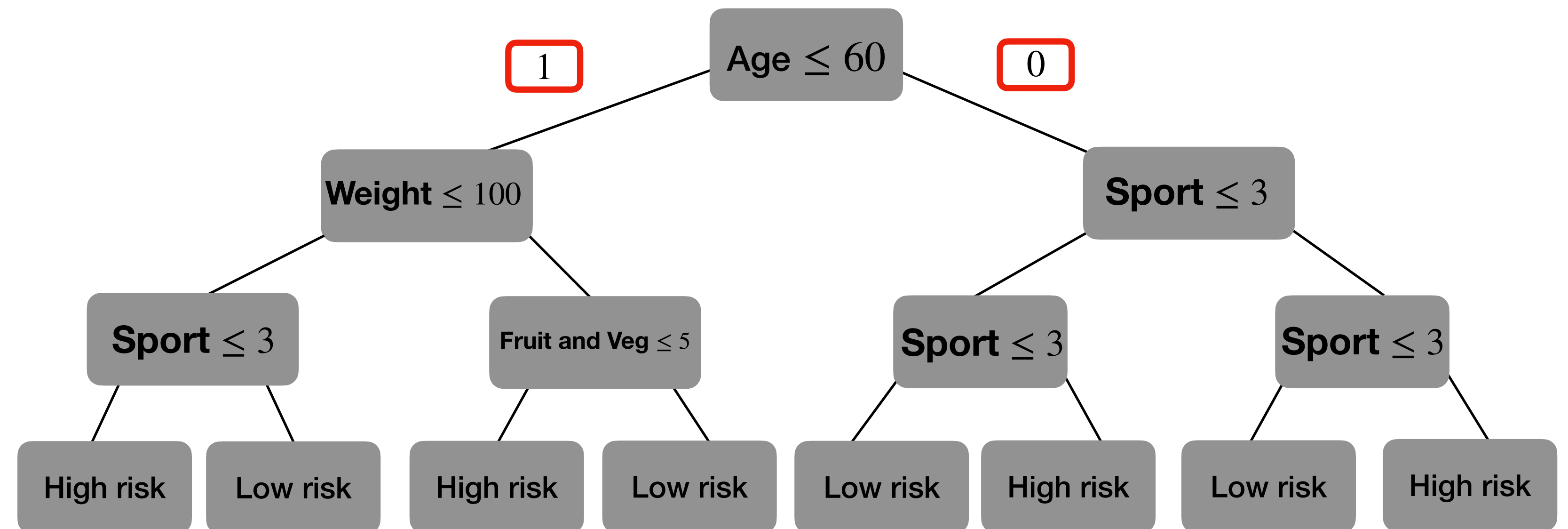
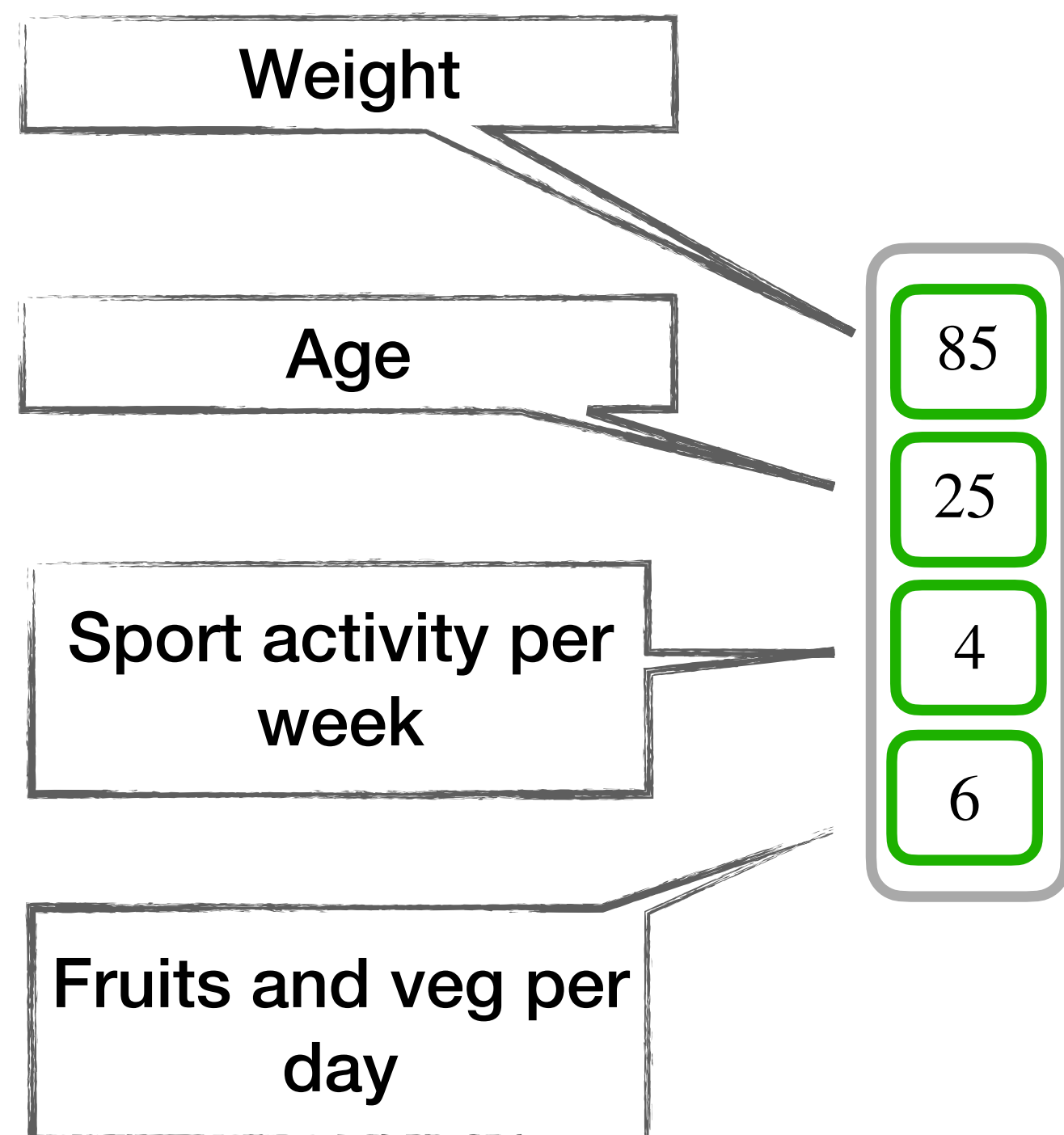
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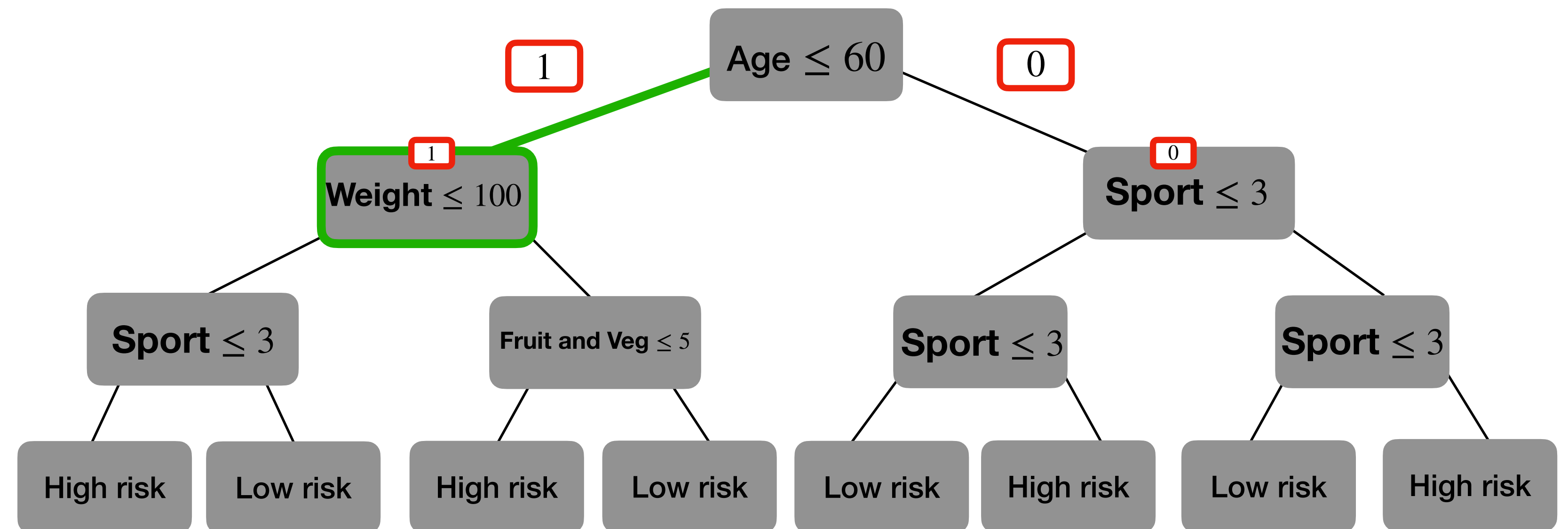
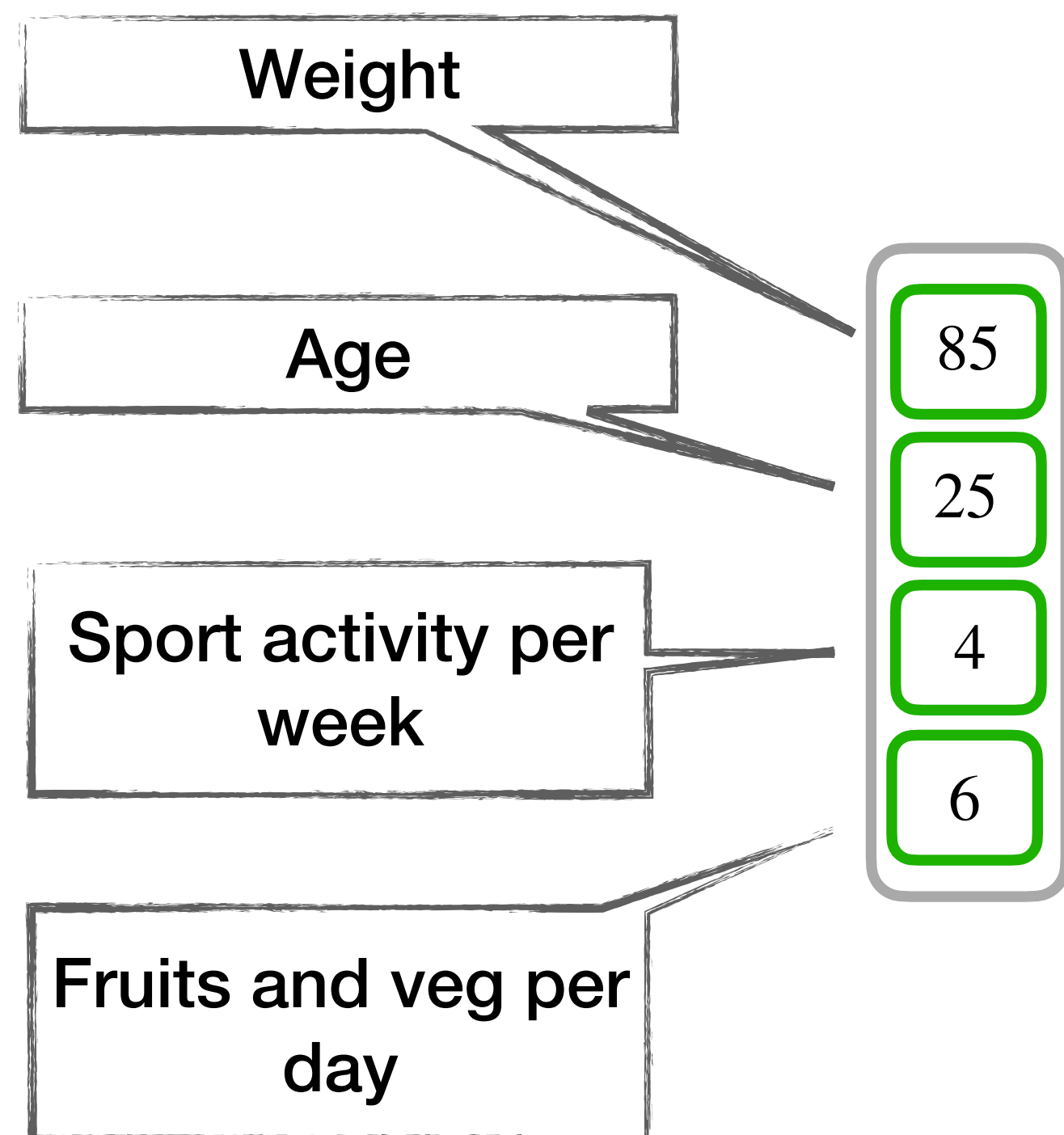
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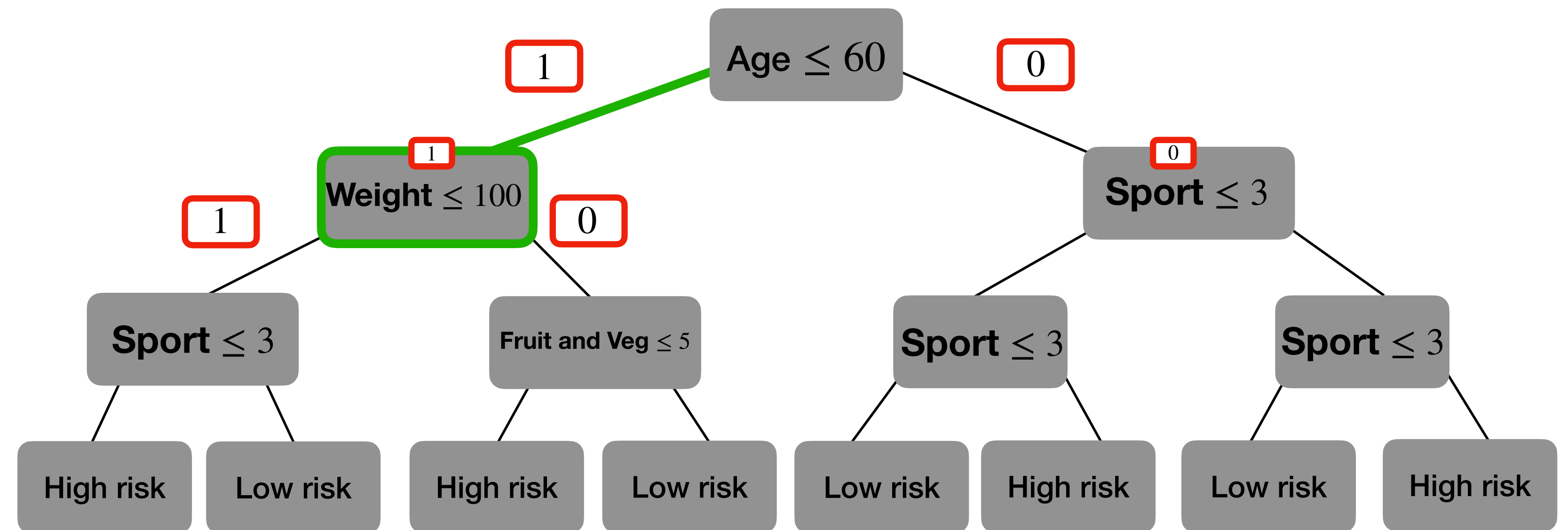
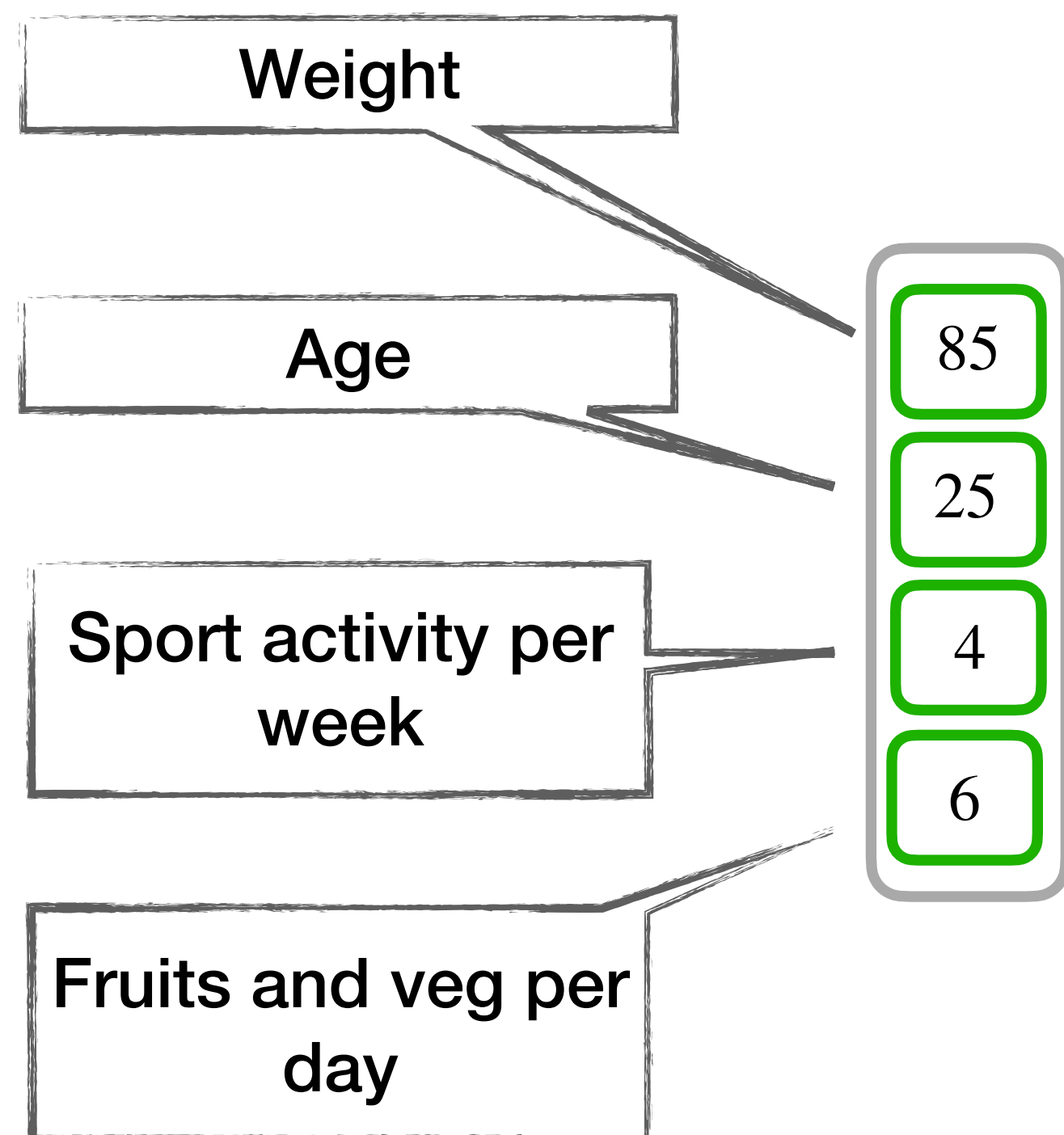
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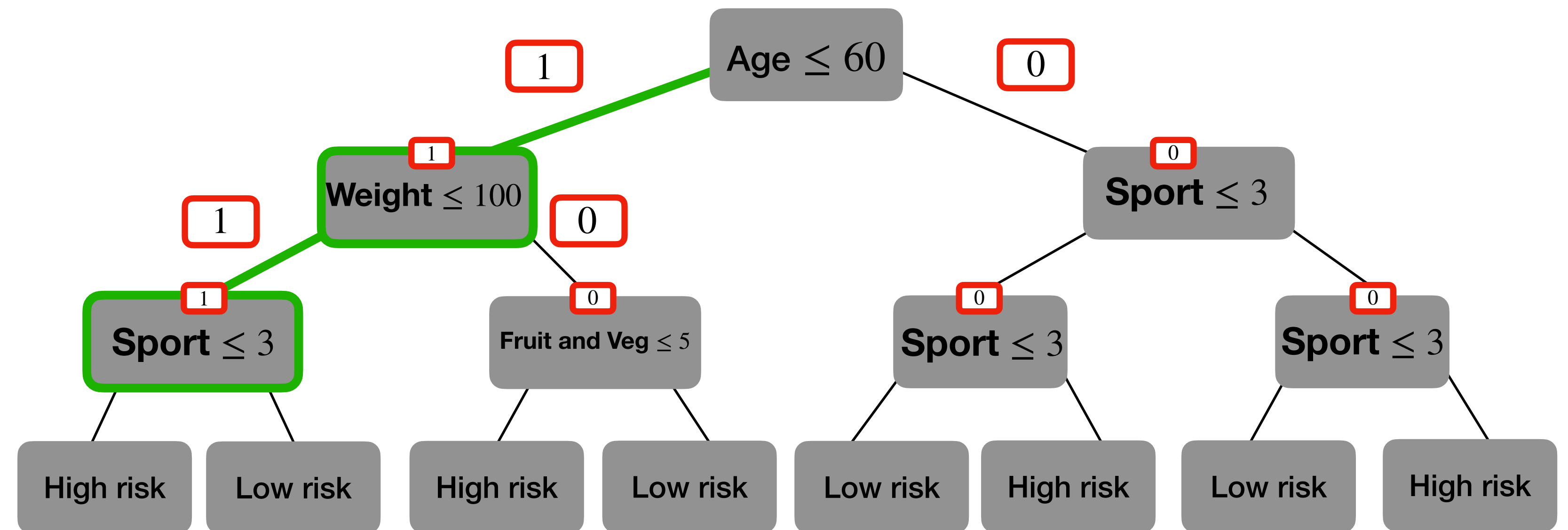
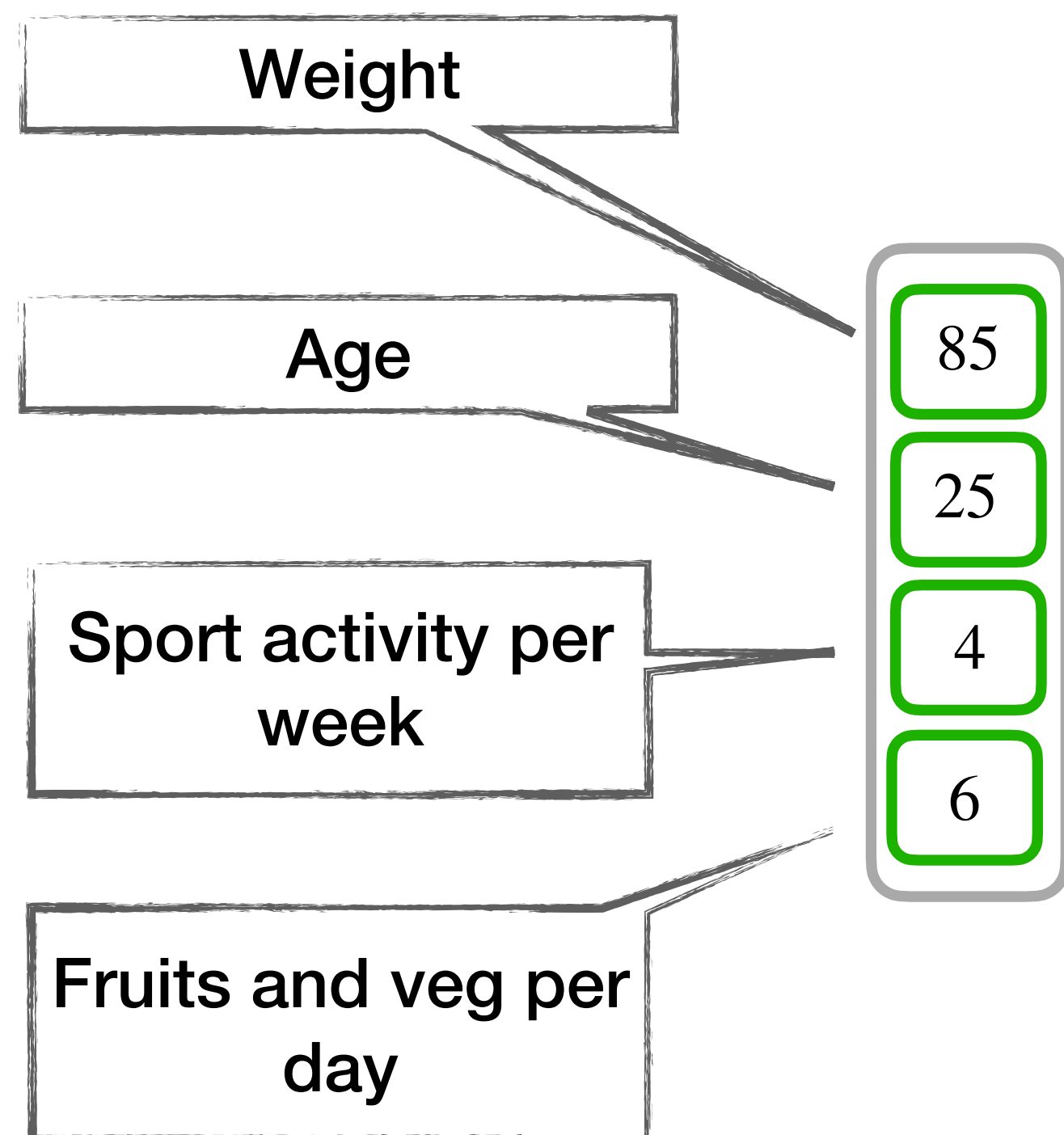
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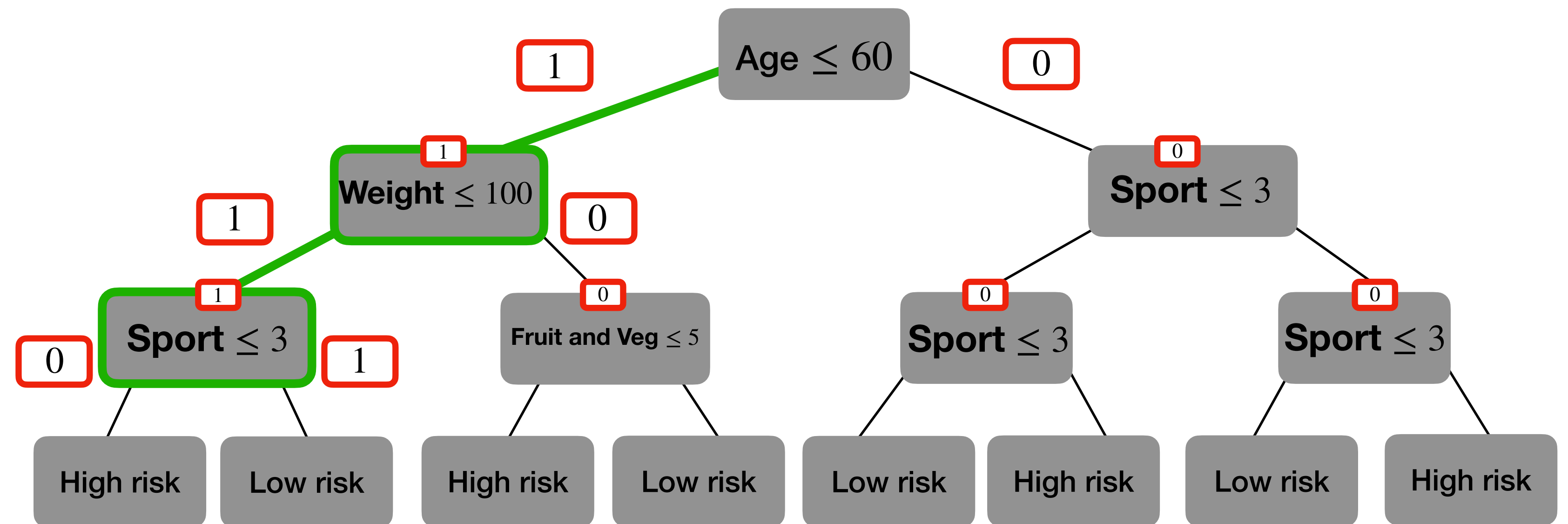
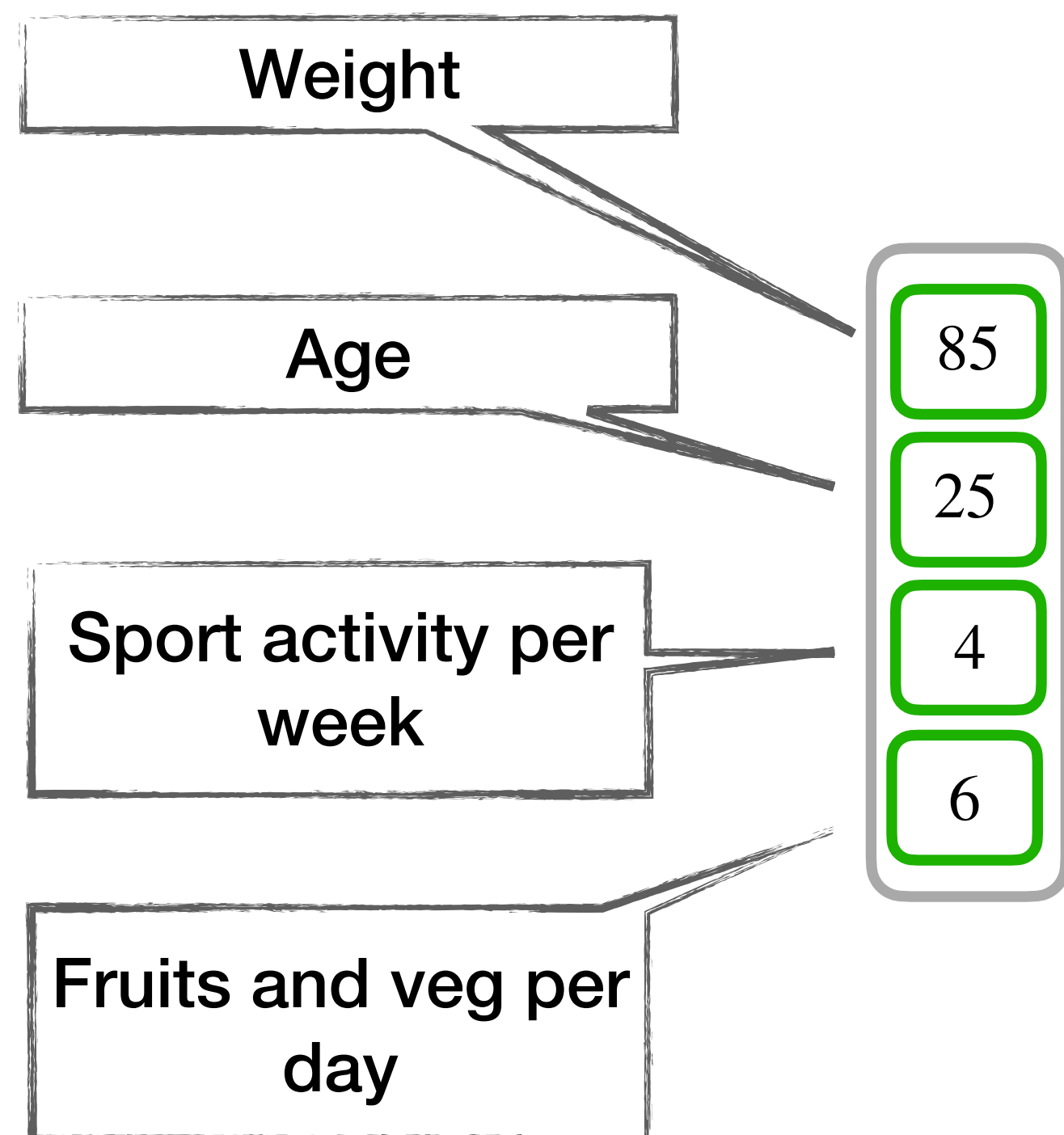
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Toy example



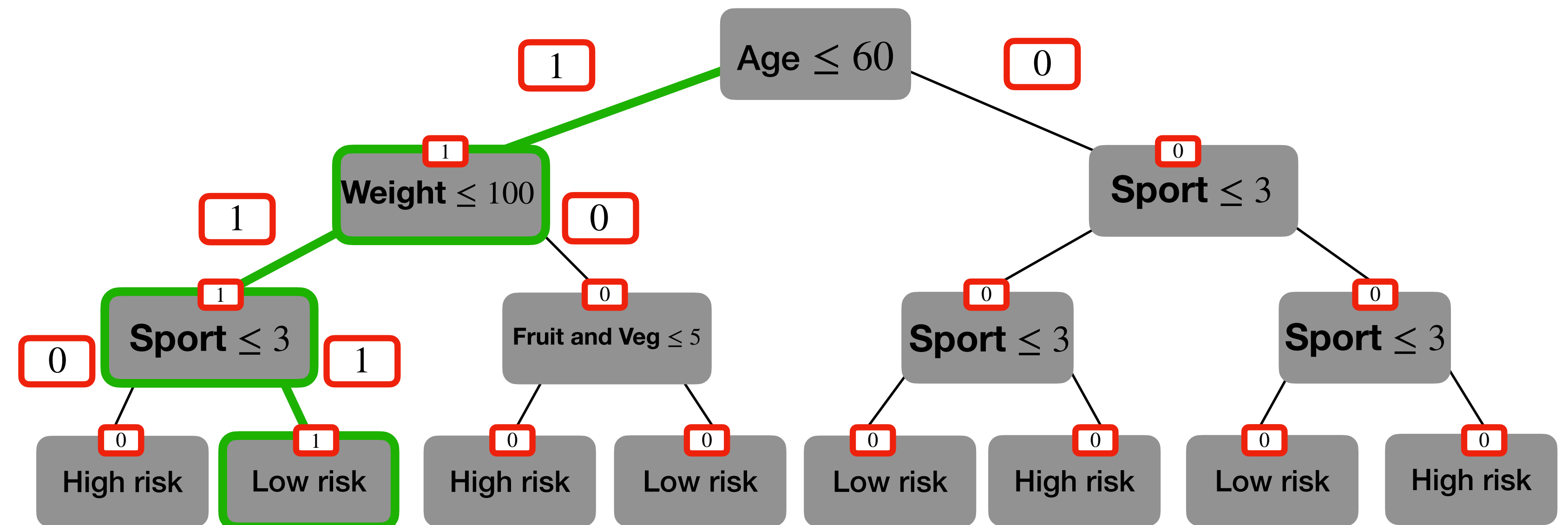
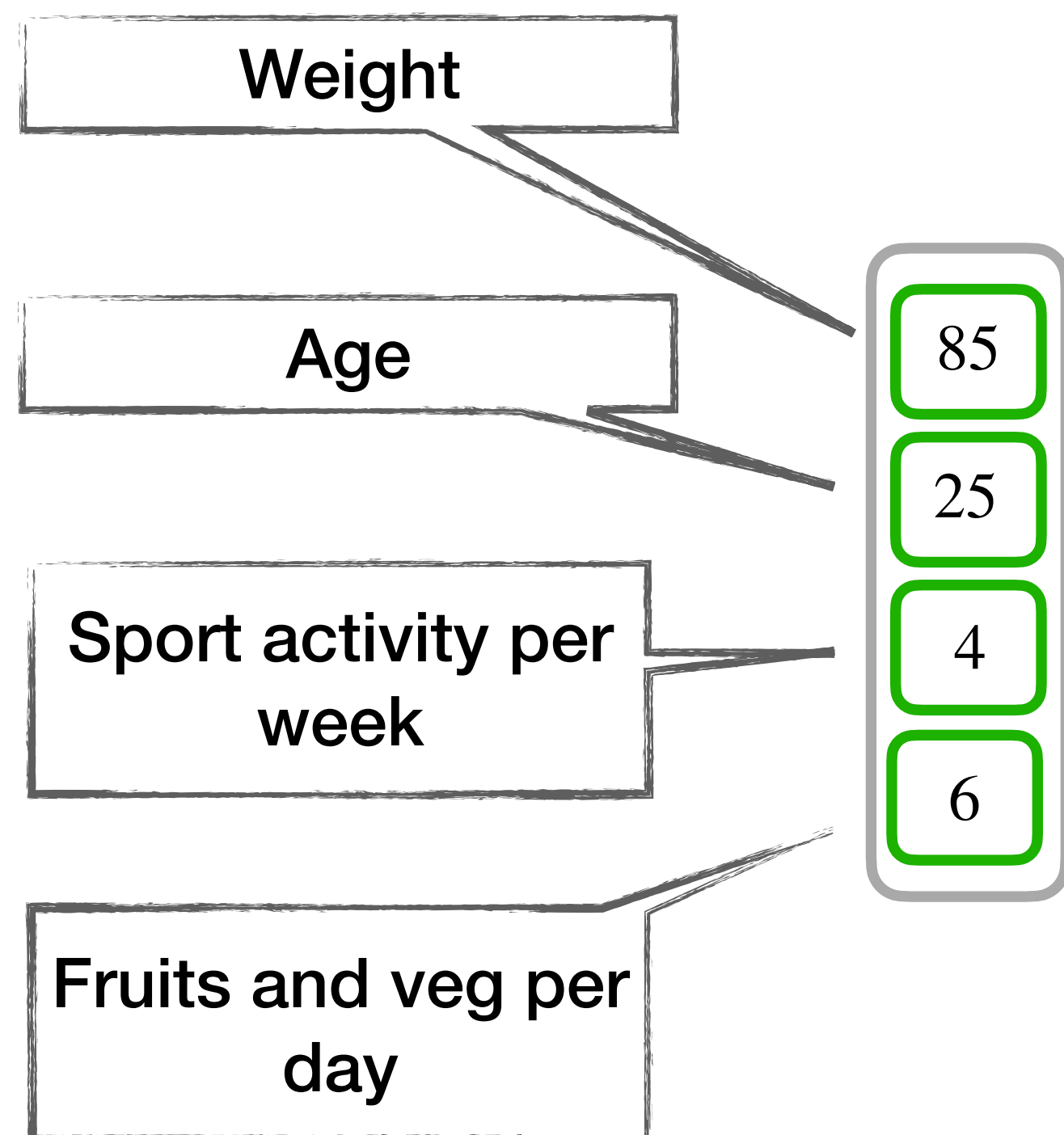
Our proposal

Toy example



Our proposal

Toy example



I have a **lower risk** to contract a disease

Conclusions and Perspectives

PROBONITE :

- A simple yet effective protocol for decision tree evaluation
- Based on homomorphic encryption and non-interactive
- Reduces the number of comparisons to its bare minimum
- Two new primitives : **Blind Array Access** and **Blind Node Selection**

Conclusions and Perspectives

Perspectives :

- Implementation with a FHE library
- Packing techniques
- Use efficient private comparison to improve the protocol

Thanks ! 

Any Questions ?

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