

UQÀM

DEEL

DEpendable & Explainable Learning

Oblivious Exact (Un)Learning of Extremely Randomized Trees

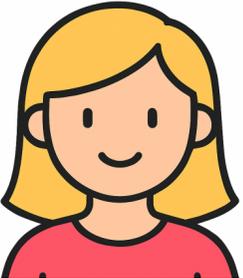
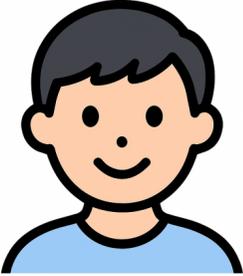
Sofiane Azogagh, Zelma Aubin Birba,
Sébastien Gambs and Marc-Olivier Killijian



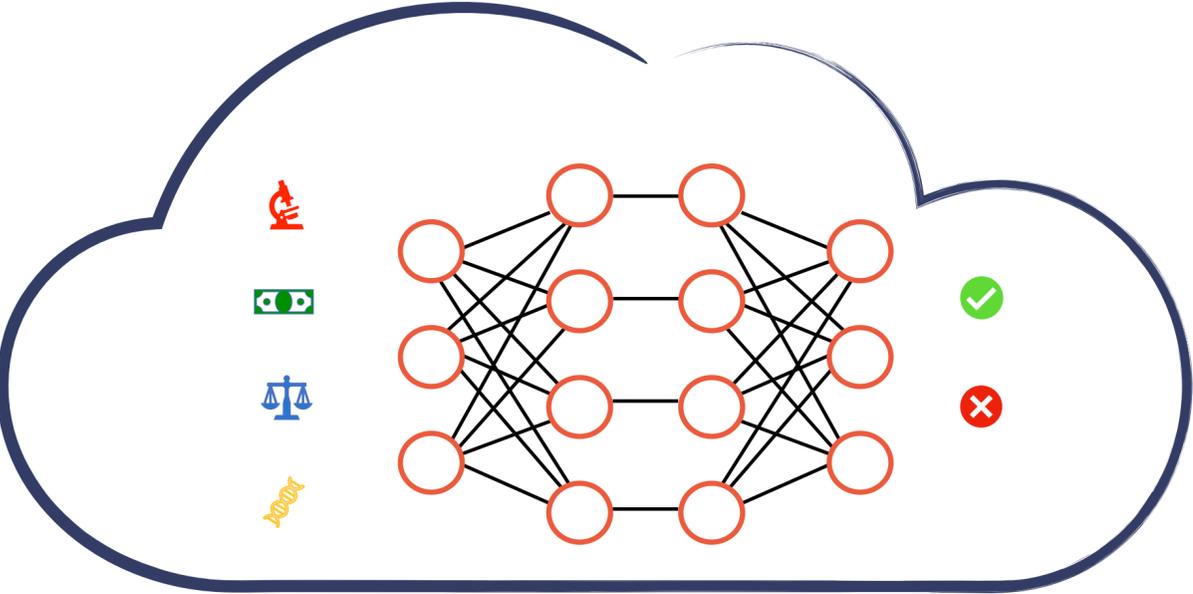
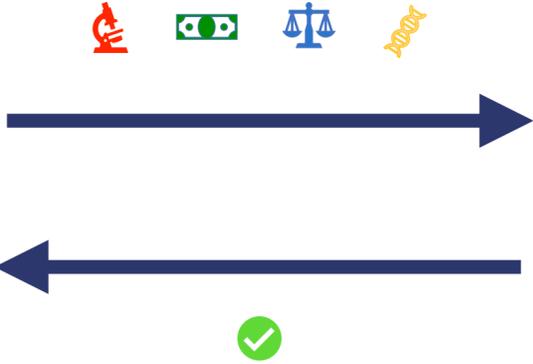
Slides



Outsourcing the computation

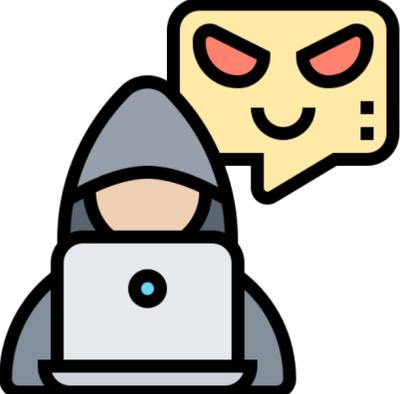


Client

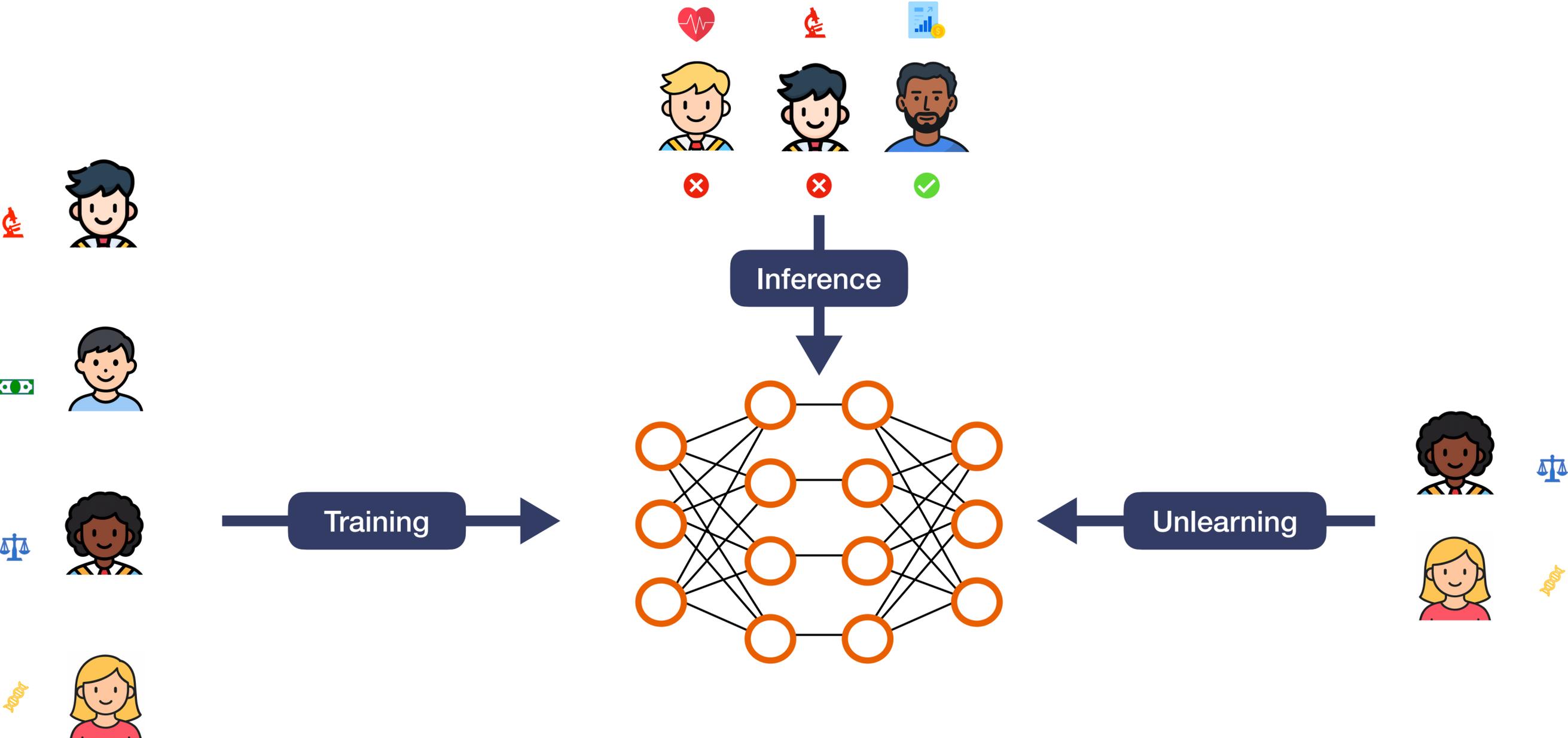


Server

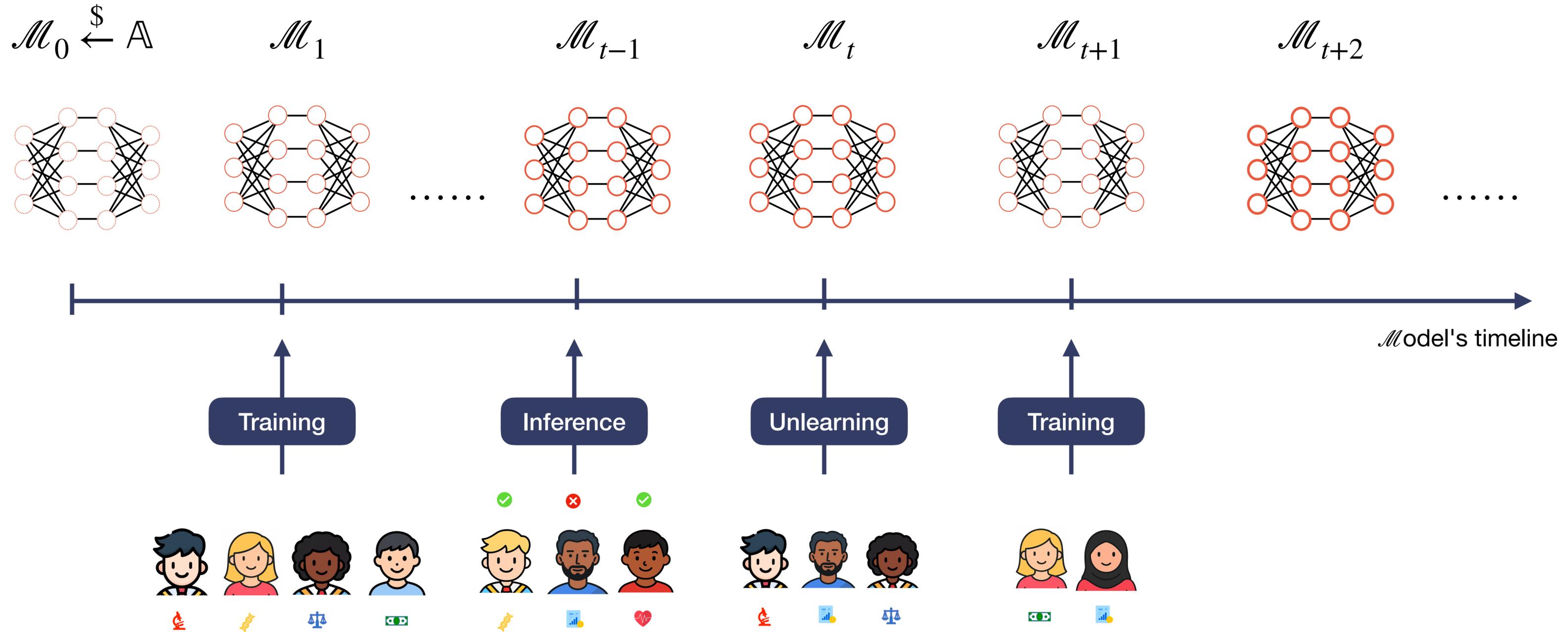
Passive adversary



Different phases in ML



Online Learning



Oblivious computation

Just a definition



```
1  if a > b:  
2      max = a  
3  else:  
4      max = b
```

Non oblivious



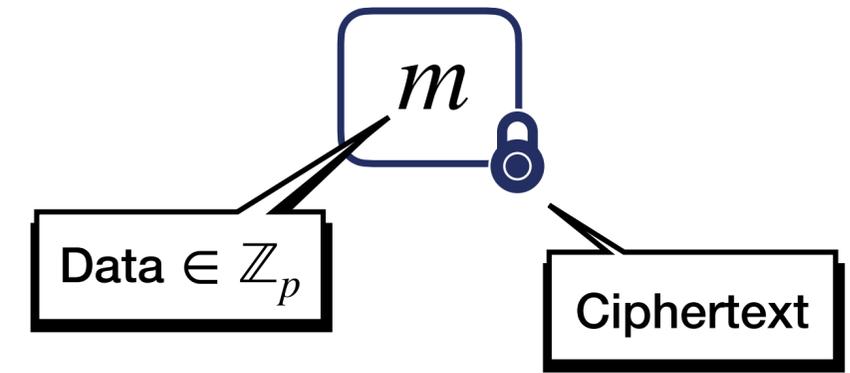
```
1  s = (a > b)  
2  max = a*s + b*(1-s)
```

Oblivious

Oblivious algorithms are algorithms whose **access patterns** (e.g., which memory addresses they touch) and **control flow** (e.g., which branch they take) are **independent of the input data values**.

Oblivious computation

Fully Homomorphic Encryption (FHE)



- Addition
- Multiplication

$$\begin{aligned} \boxed{x} + \boxed{y} &= \boxed{x + y} \\ \boxed{x} \times \boxed{y} &= \boxed{x \times y} \end{aligned}$$

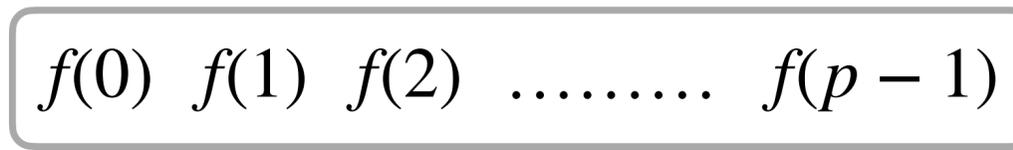
Arithmetic operations

TFHE

- Function evaluation
(Functional Bootstrapping)

$$f(\boxed{x}) = \boxed{f(x)}$$

Non arithmetic operations

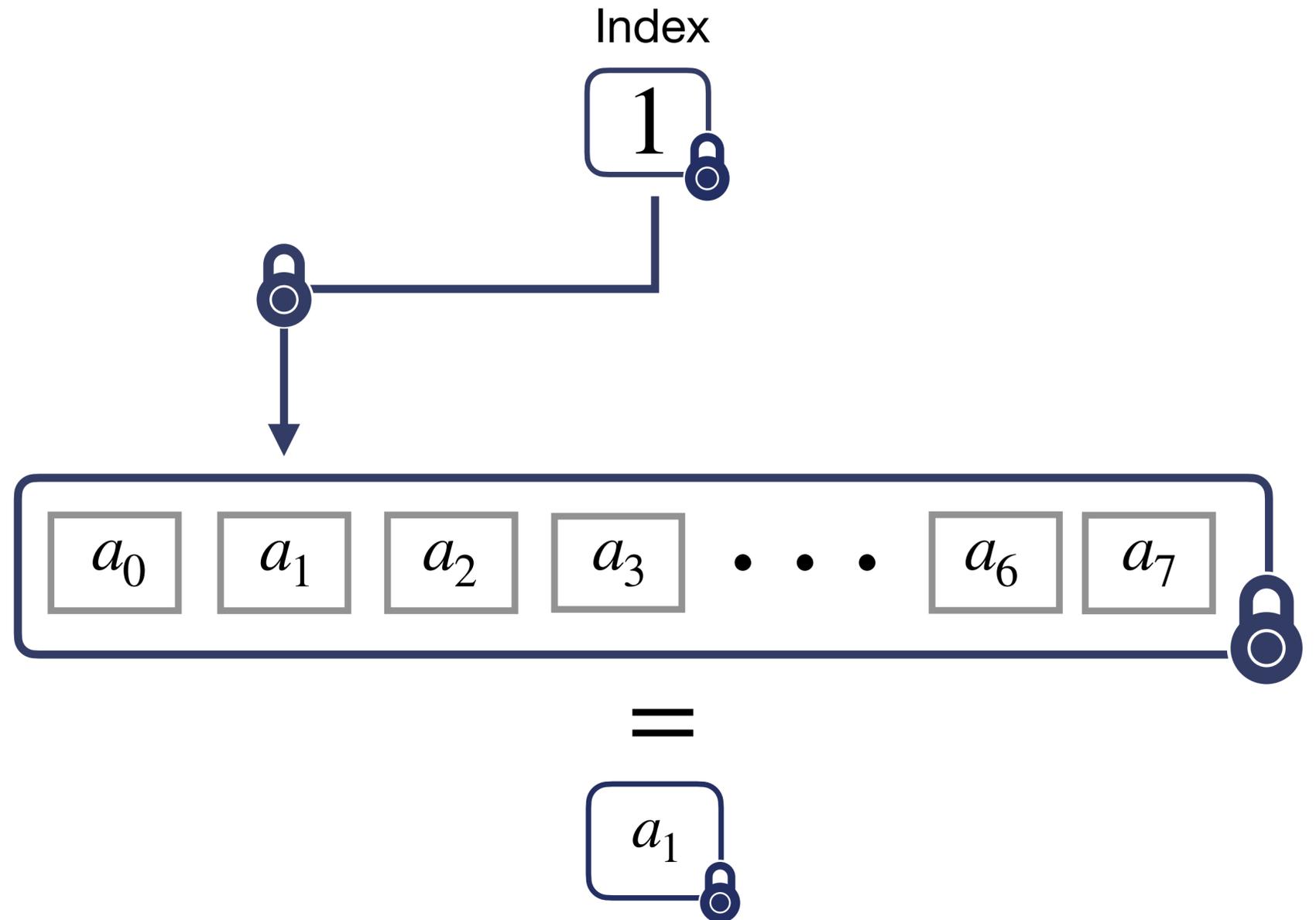


LUT : Look-Up-Table

Oblivious computation

RevoLUT library

Blind Read

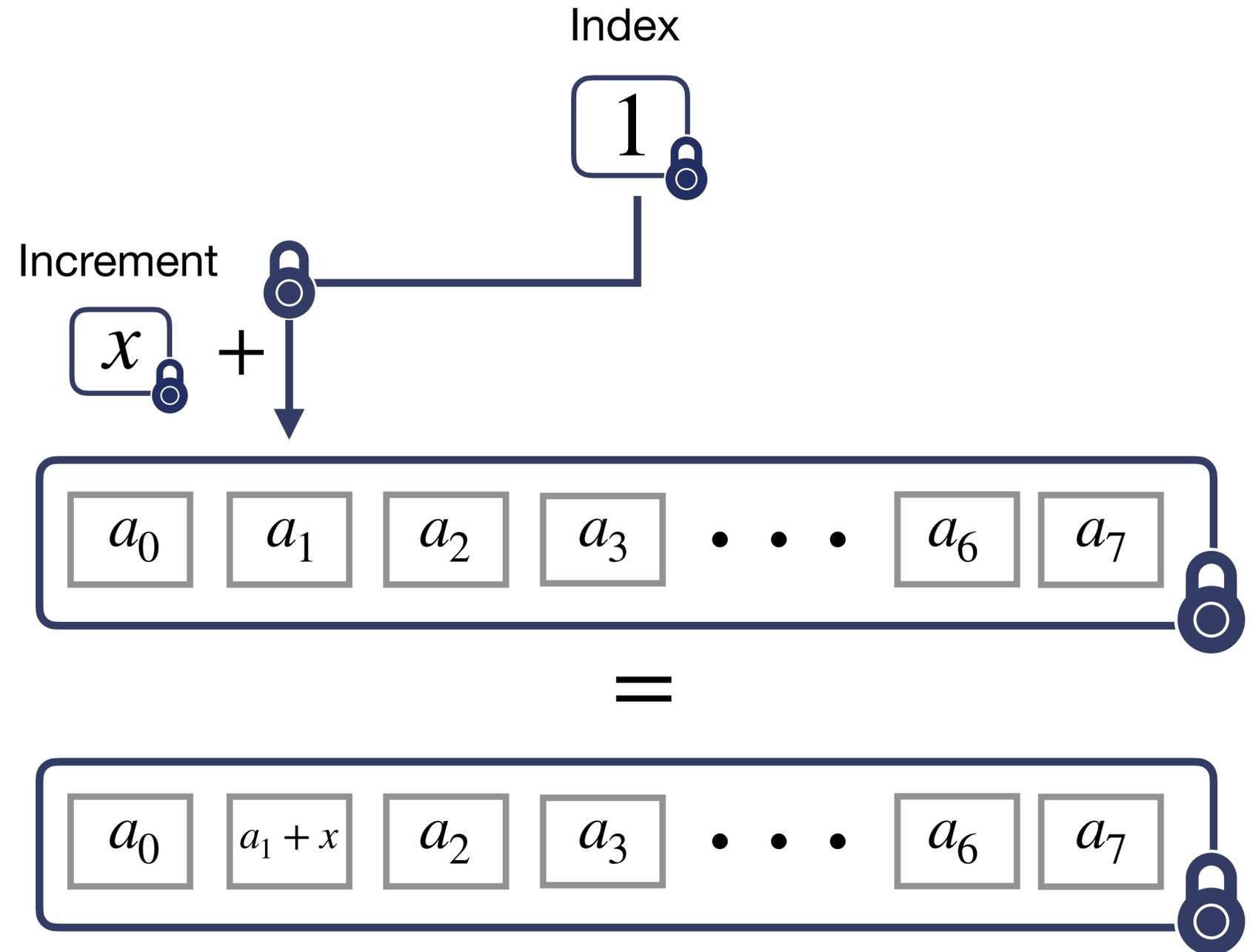


Oblivious computation

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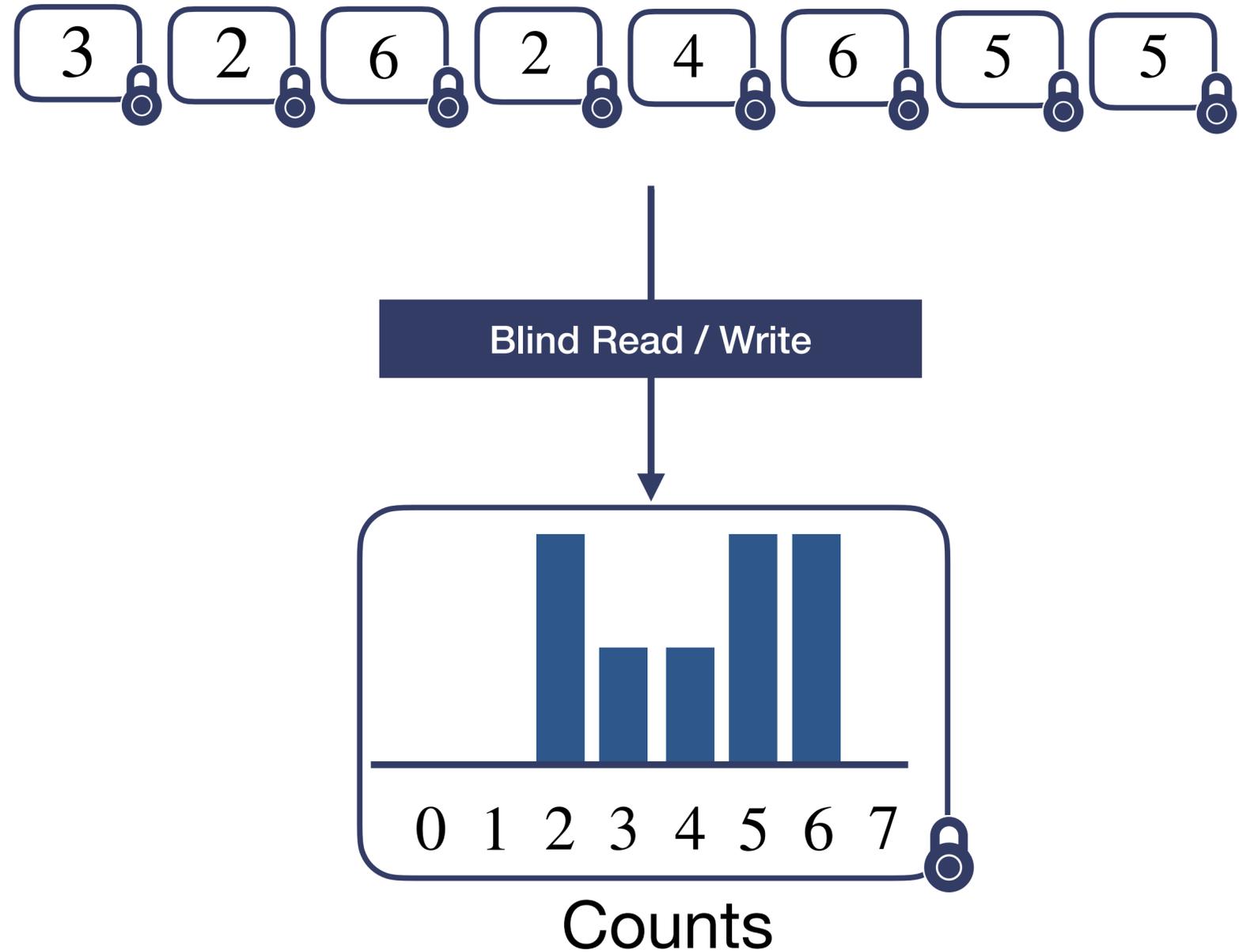
Blind Write



Oblivious computation

RevoLUT library

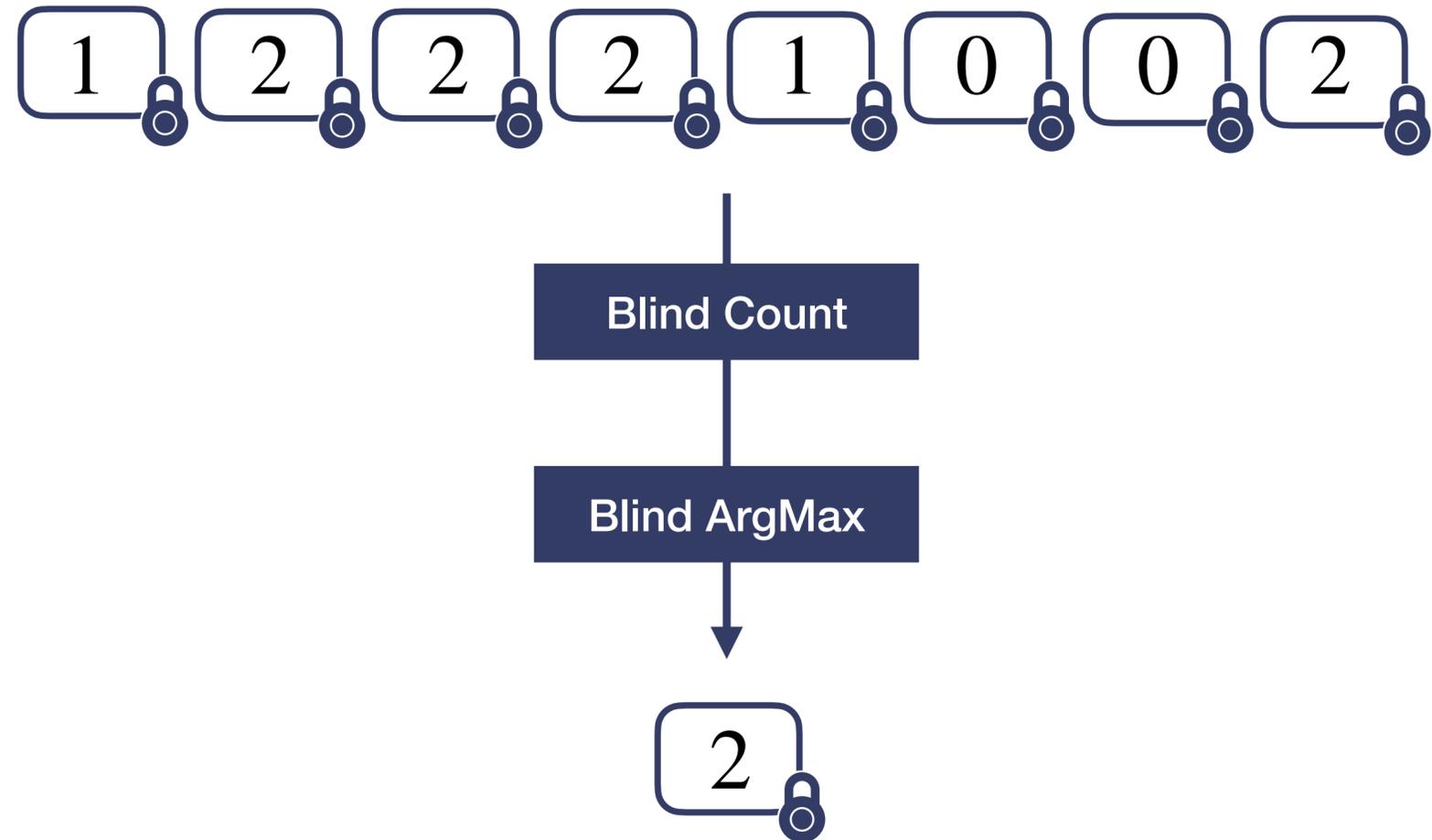
- Blind Read
- Blind Write
- Blind Count



Oblivious computation

RevoLUT library

- Blind Read
- Blind Write
- Blind Count
- Blind Majority

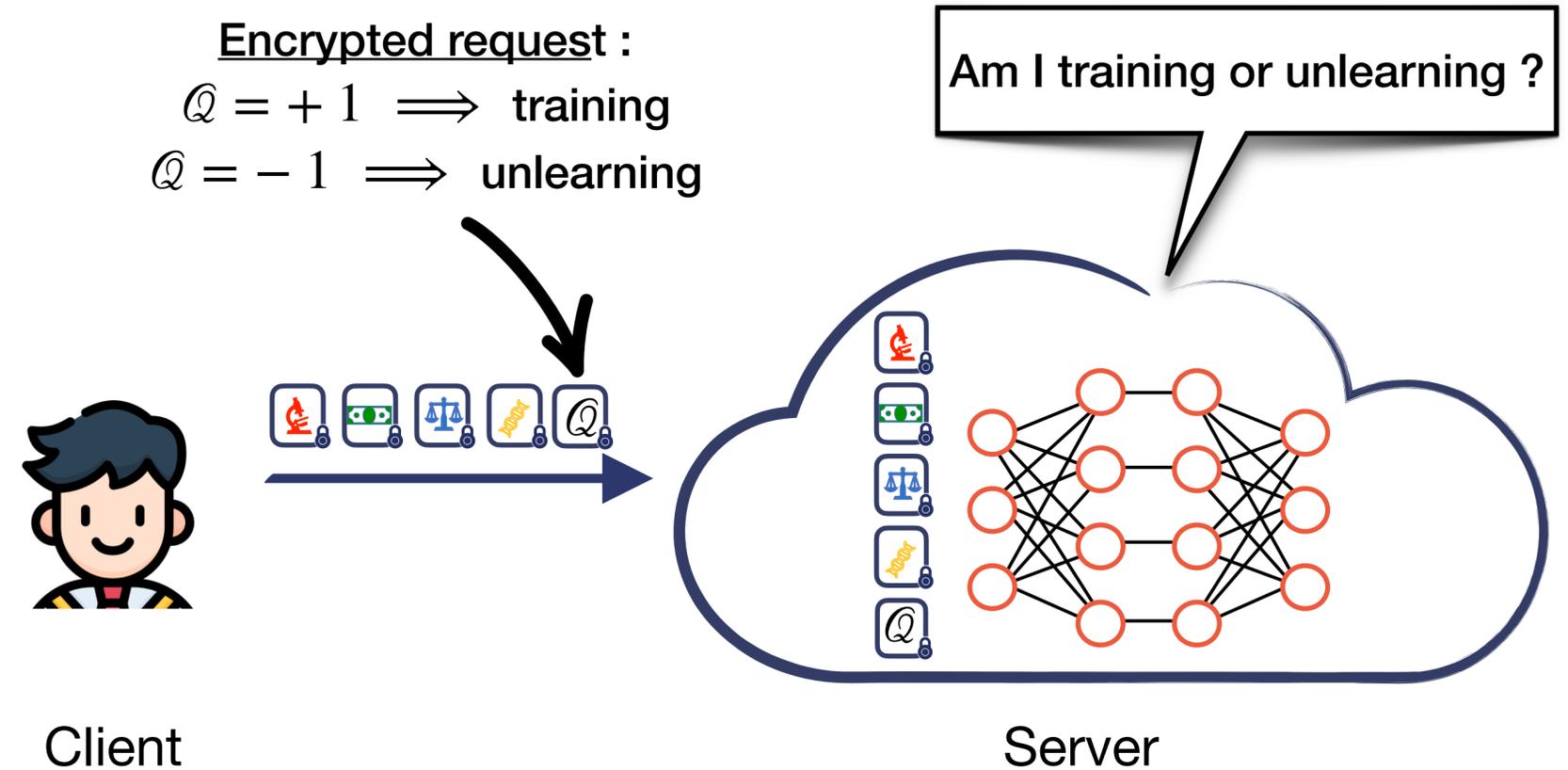


Oblivious unlearning

Goal : **Hiding unlearning requests** from the server

Why ?

- To protect **users privacy**
- To enforce the **right to be forgotten**



Home > News

Google refusing to comply with "right to be forgotten" delisting decision

OTTAWA — The federal privacy commissioner says individuals have the right to have some information delisted from search engine results, but Google is refusing to comply.

Anja Karadeglija, The Canadian Press
Aug 27, 2025 2:47 PM



Extremely Randomized Tree (ERT)

θ : Threshold

I : Feature index

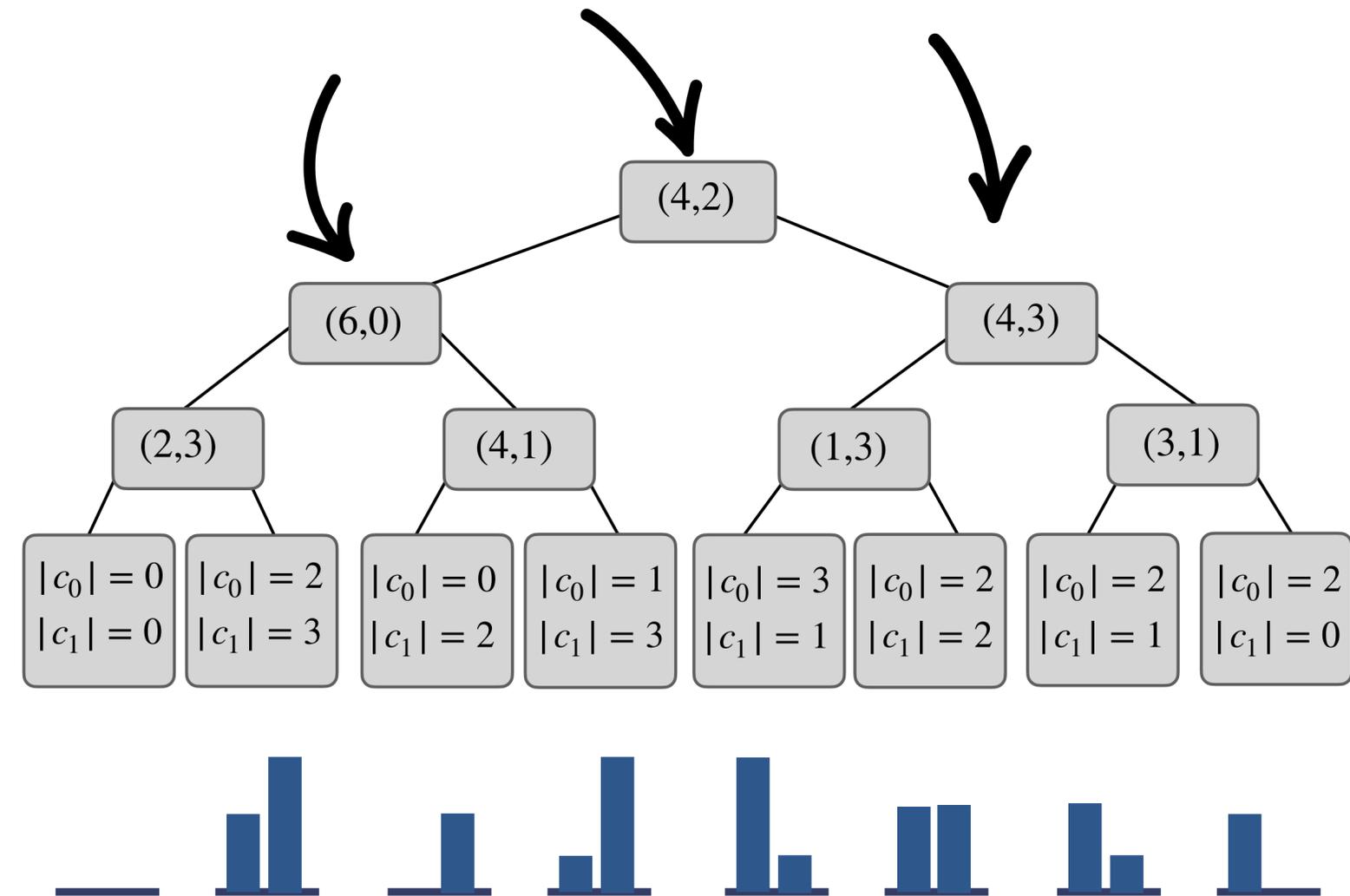
Let $S = \{(X_j, y_j)\}_{j=1}^n$ be the training set where $X_j \in \mathbb{R}^l$ and $y_j \in \{c_0, \dots, c_{\ell-1}\}$.

Two steps to build an ERT :

- 1 Build the internal nodes : randomized splits
- 2 Count class occurrences : accumulating class counts in leaves

Each leaves stores the number of samples from each class c_i that reach it

Splits (θ, I) are selected among k random generated candidates



Extremely Randomized Tree (ERT)

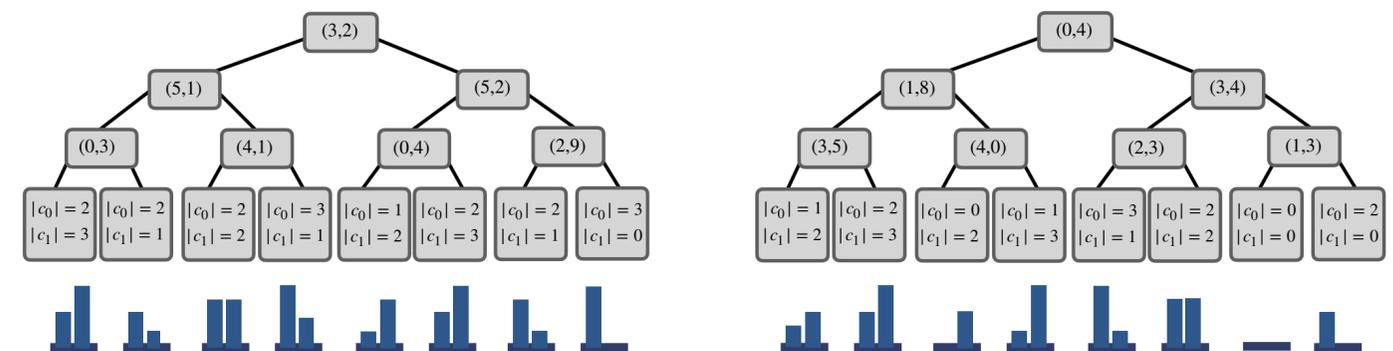
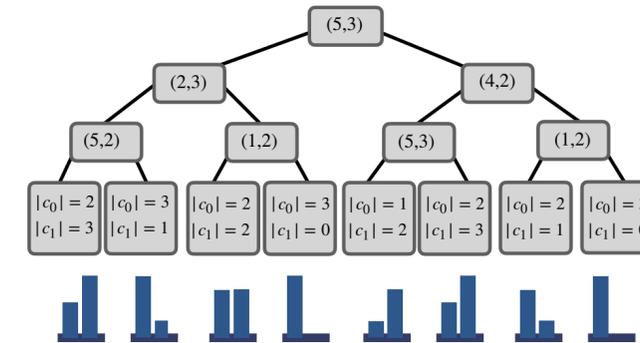
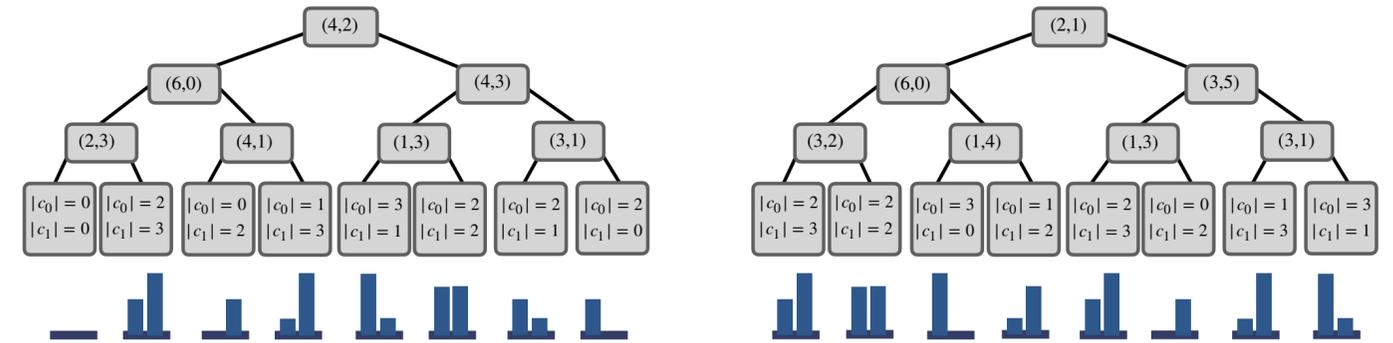
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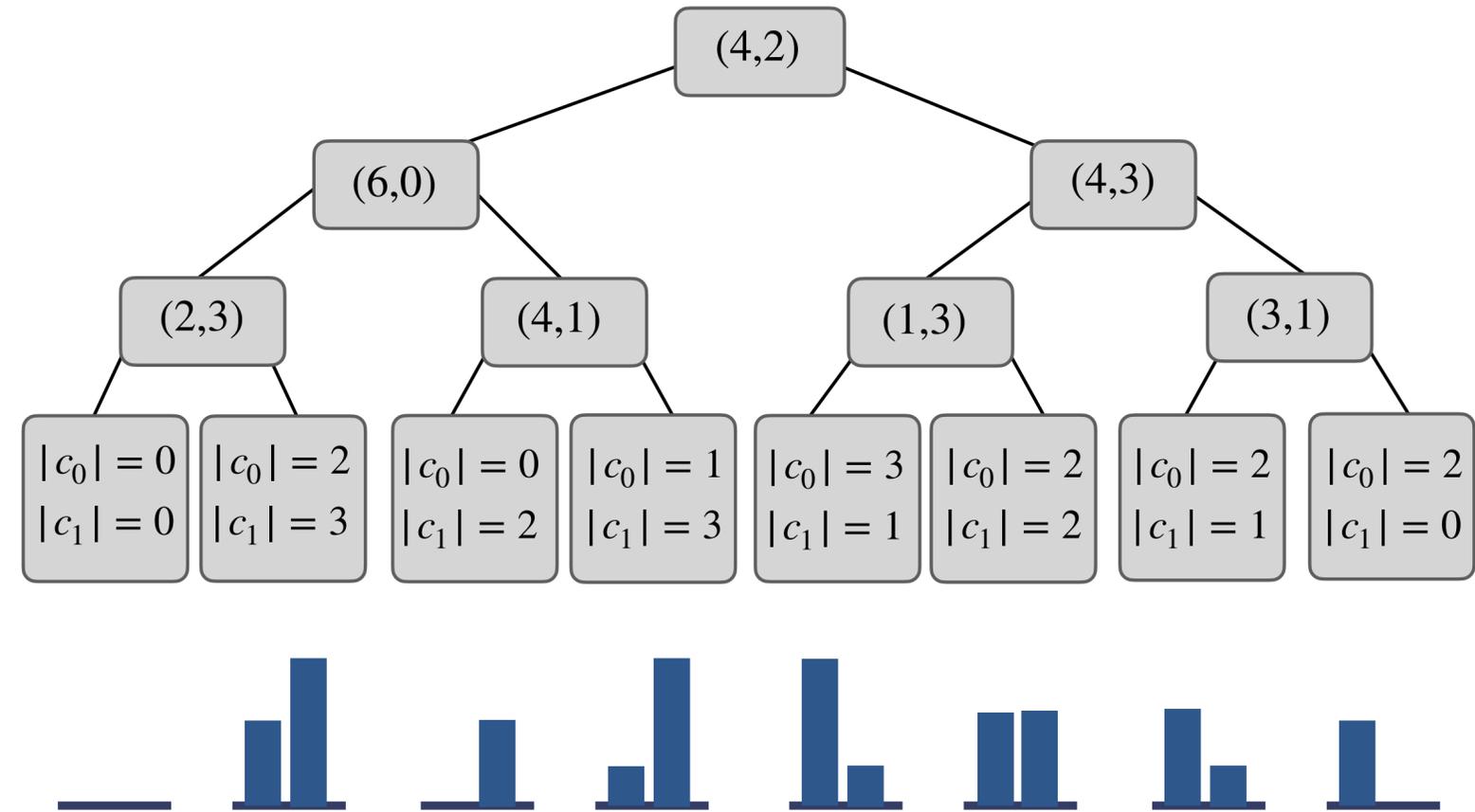


How to run ERTs on encrypted data ?

N : TFHE parameter

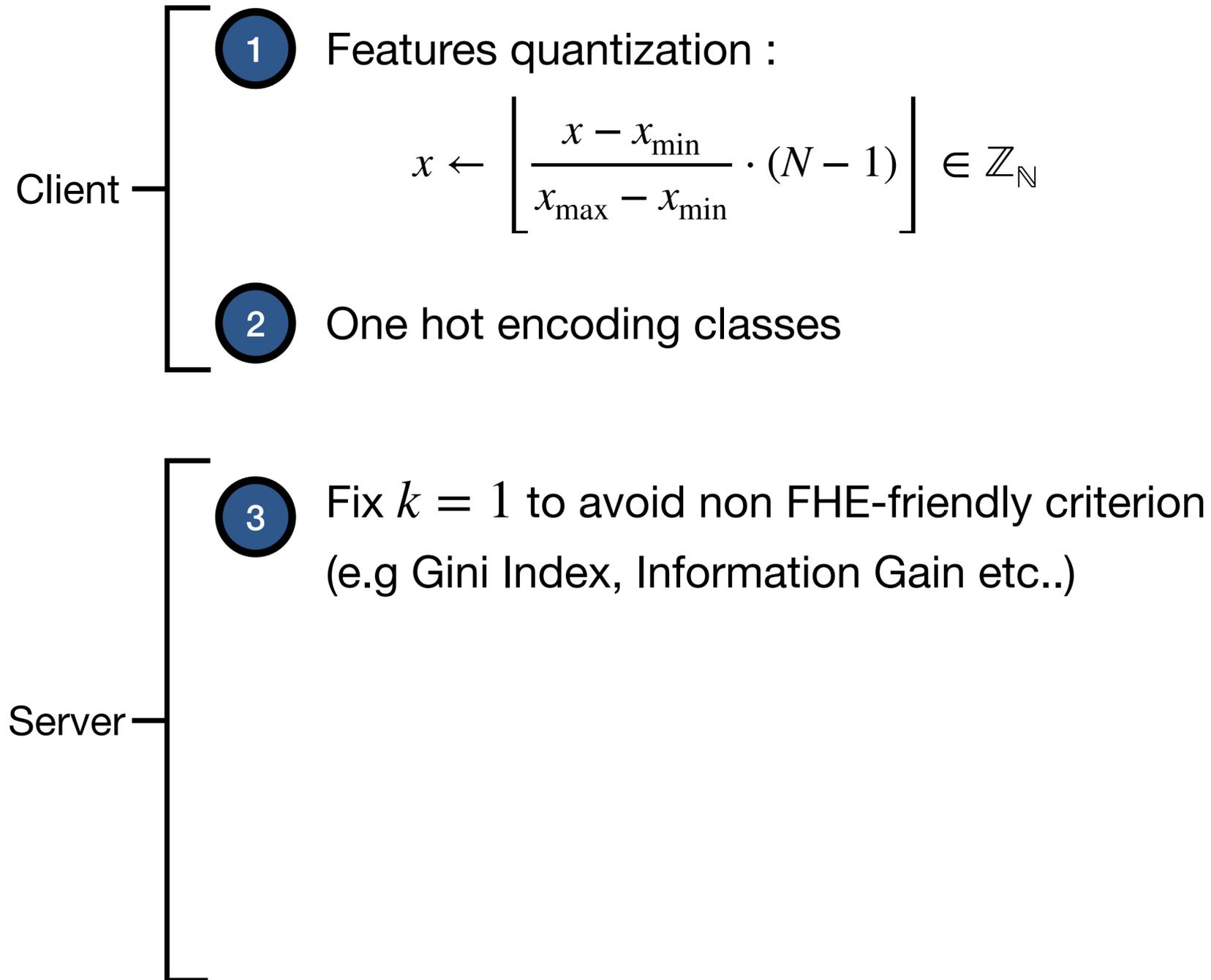
- Client
- 1 Features quantization :

$$x \leftarrow \left\lfloor \frac{x - x_{\min}}{x_{\max} - x_{\min}} \cdot (N - 1) \right\rfloor \in \mathbb{Z}_N$$
 - 2 One hot encoding classes

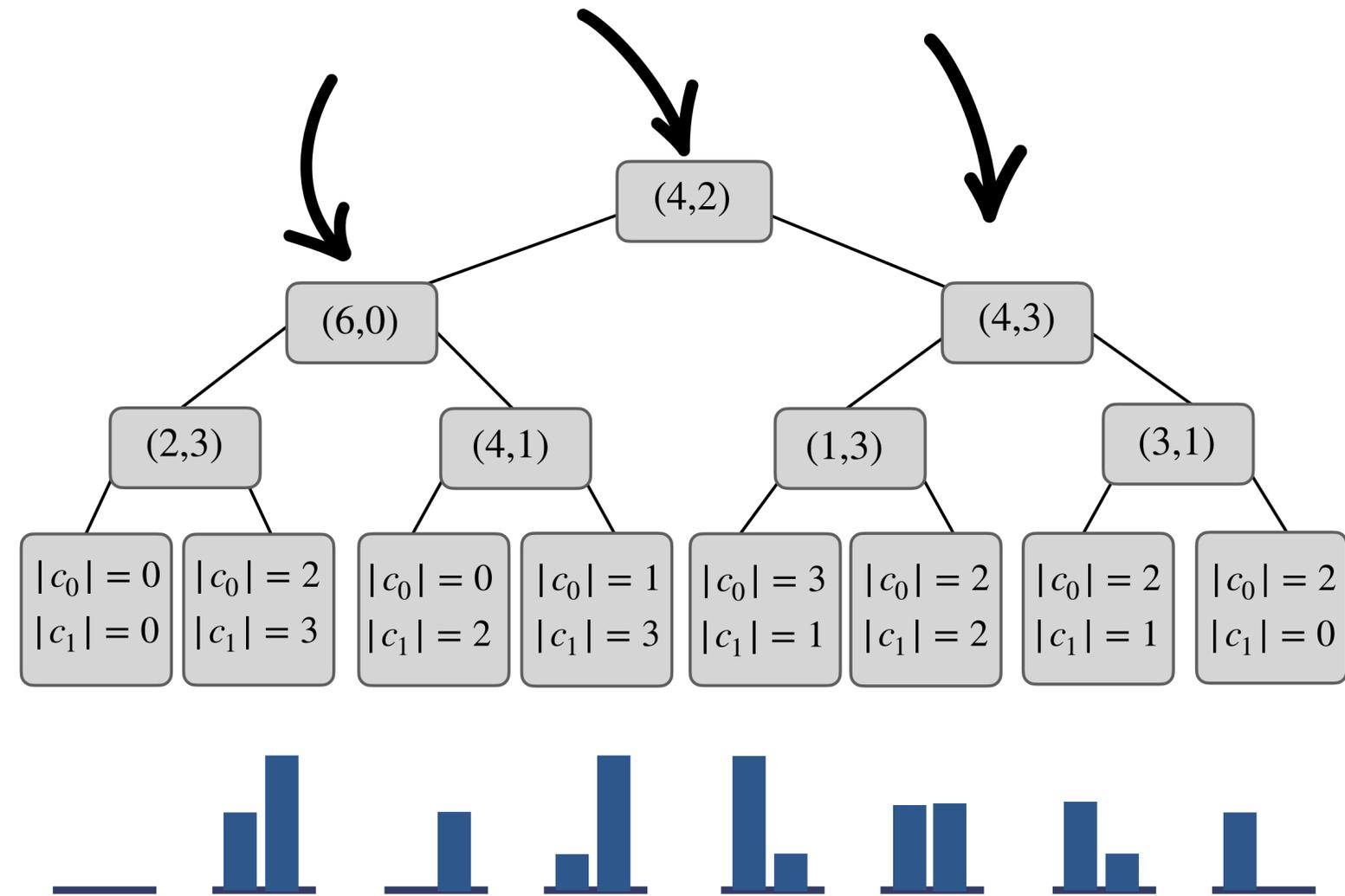


How to run ERTs on encrypted data ?

N : TFHE parameter



Splits (θ, I) are sampled randomly from $\mathbb{Z}_N \times \mathbb{Z}_N$



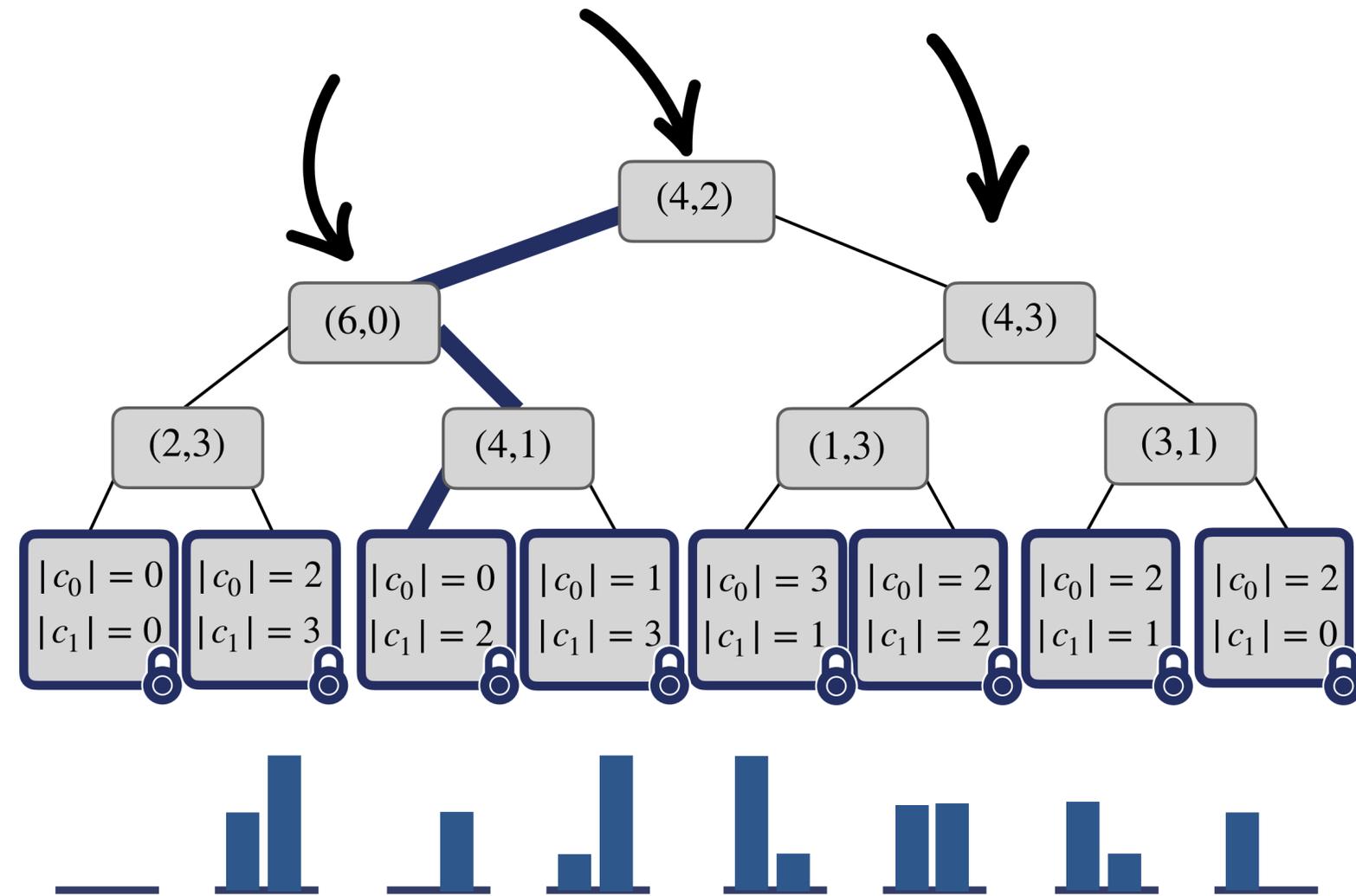
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 - One hot encoding classes
- Server
- Fix $k = 1$ to avoid non FHE-friendly criterion (e.g Gini Index, Information Gain etc..)
 - The **traversal process** and the **leaves updates** are **oblivious**

Splits (θ, I) are sampled randomly from $\mathbb{Z}_N \times \mathbb{Z}_N$



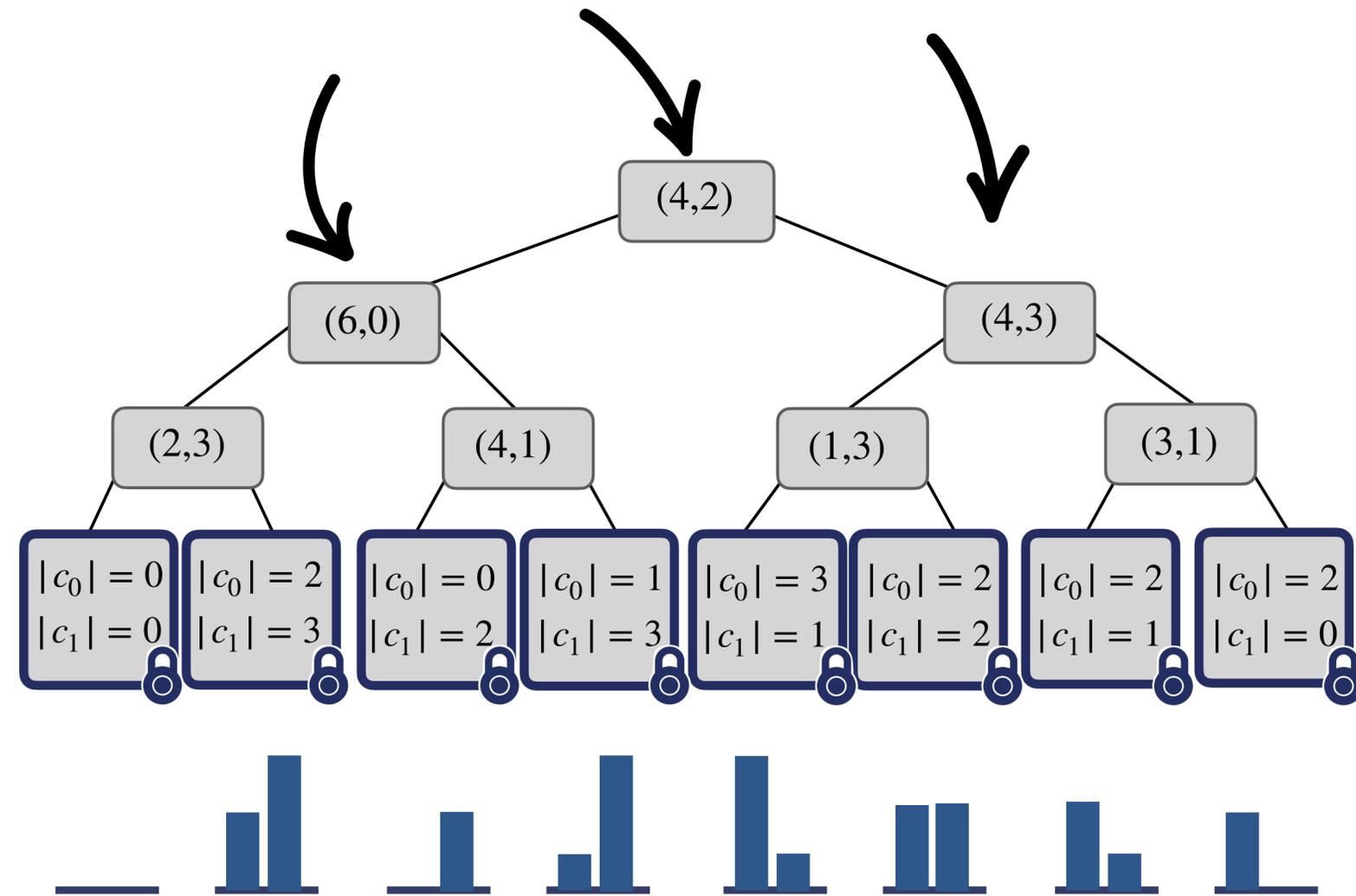
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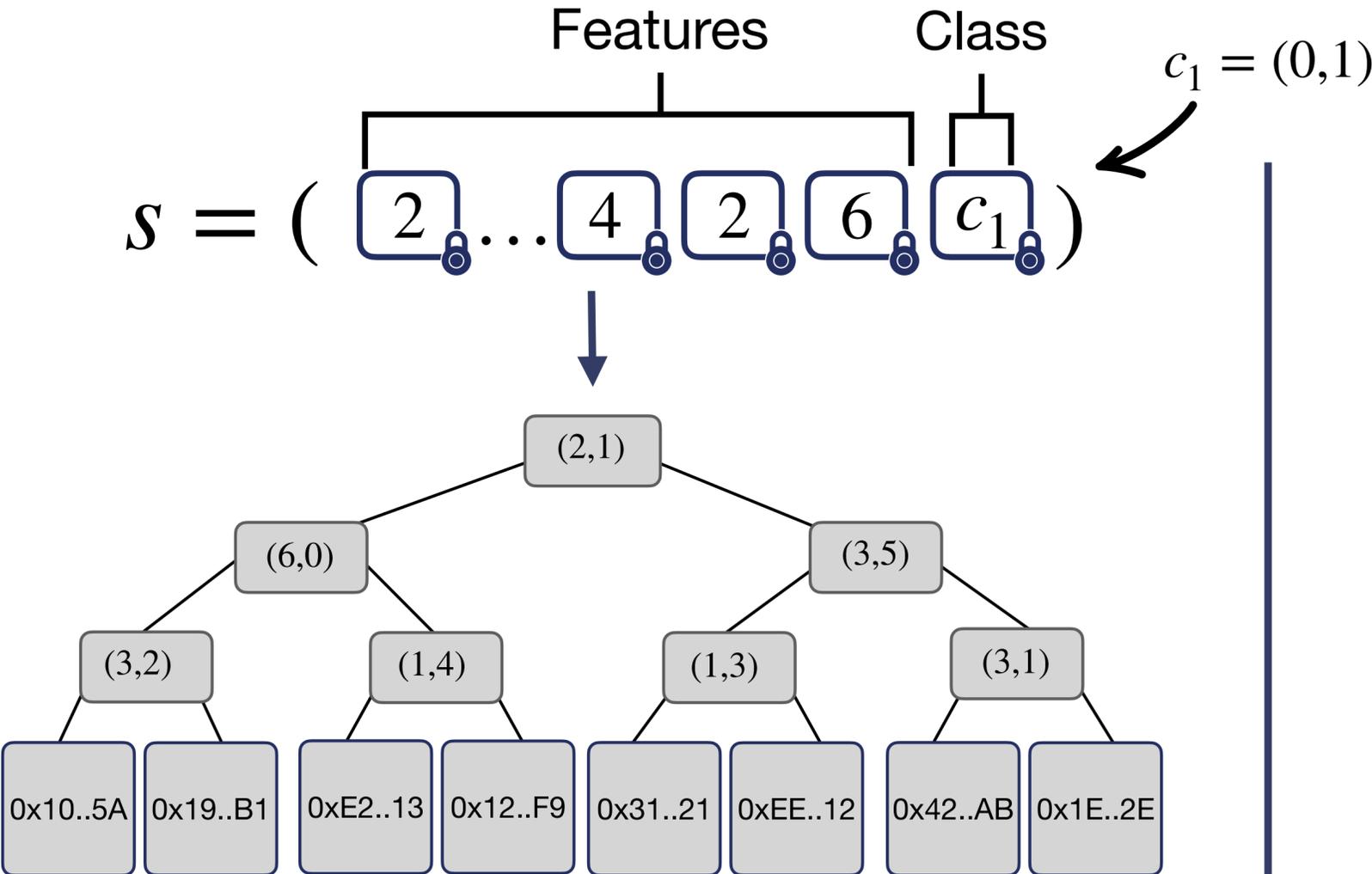
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 - One hot encoding classes
- Server
- Fix $k = 1$ to avoid non FHE-friendly criterion (e.g Gini Index, Information Gain etc..)
 - The **traversal process** and the **leaves updates** are **oblivious**
 - Internal nodes remains **public**
 - Leaves become **private**

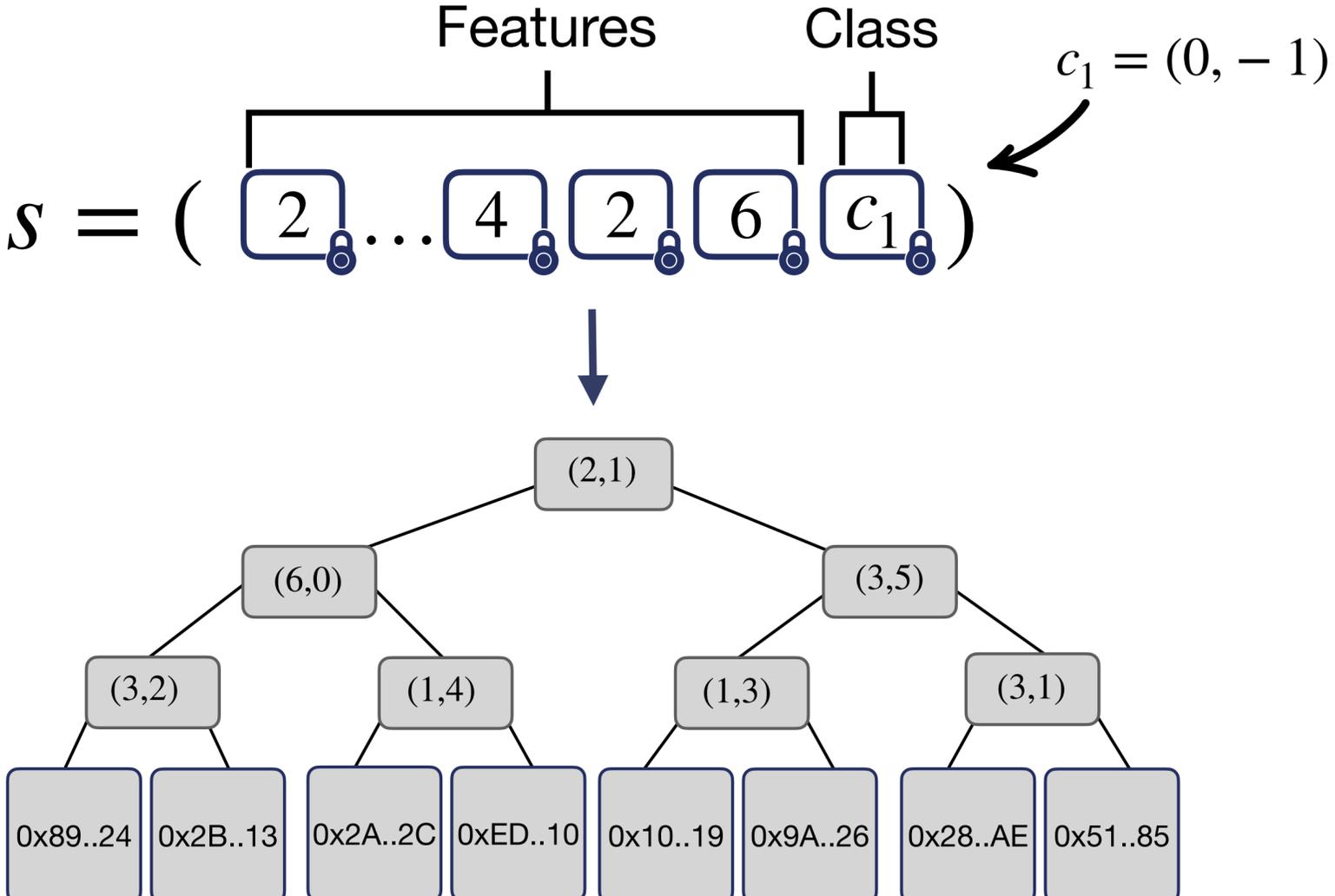
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Server's View



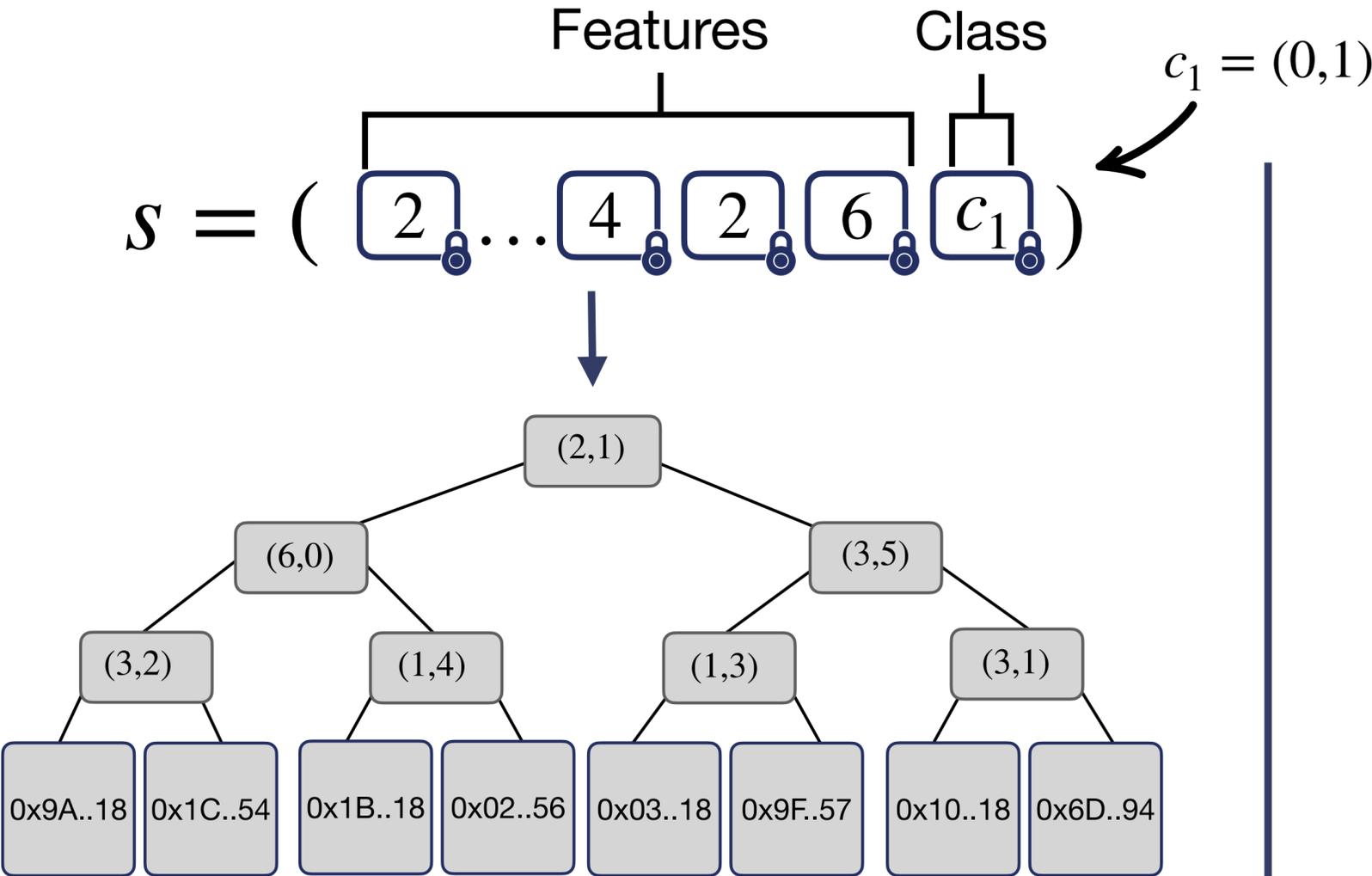
Training



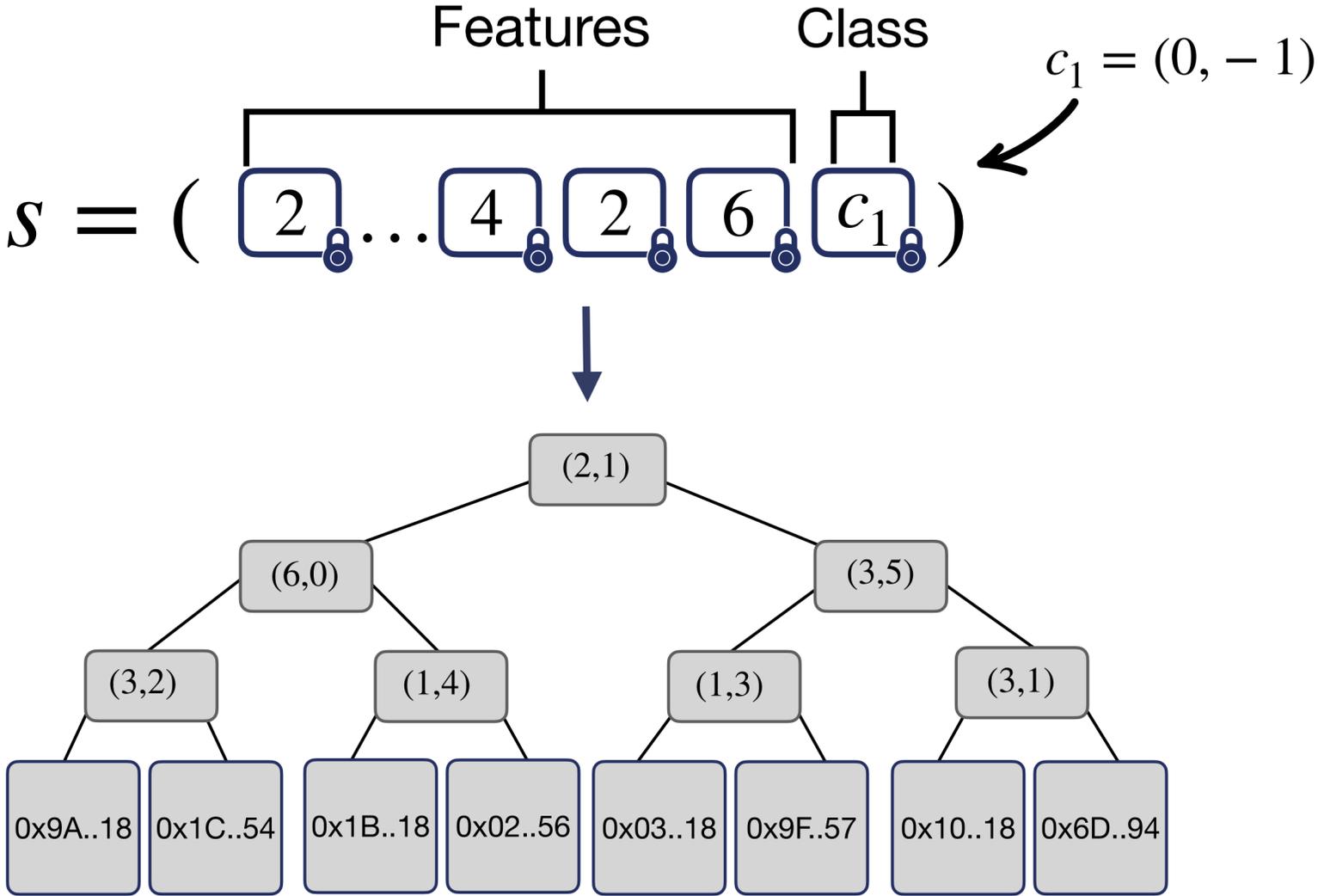
Unlearning

Server's View

Obliviousness 



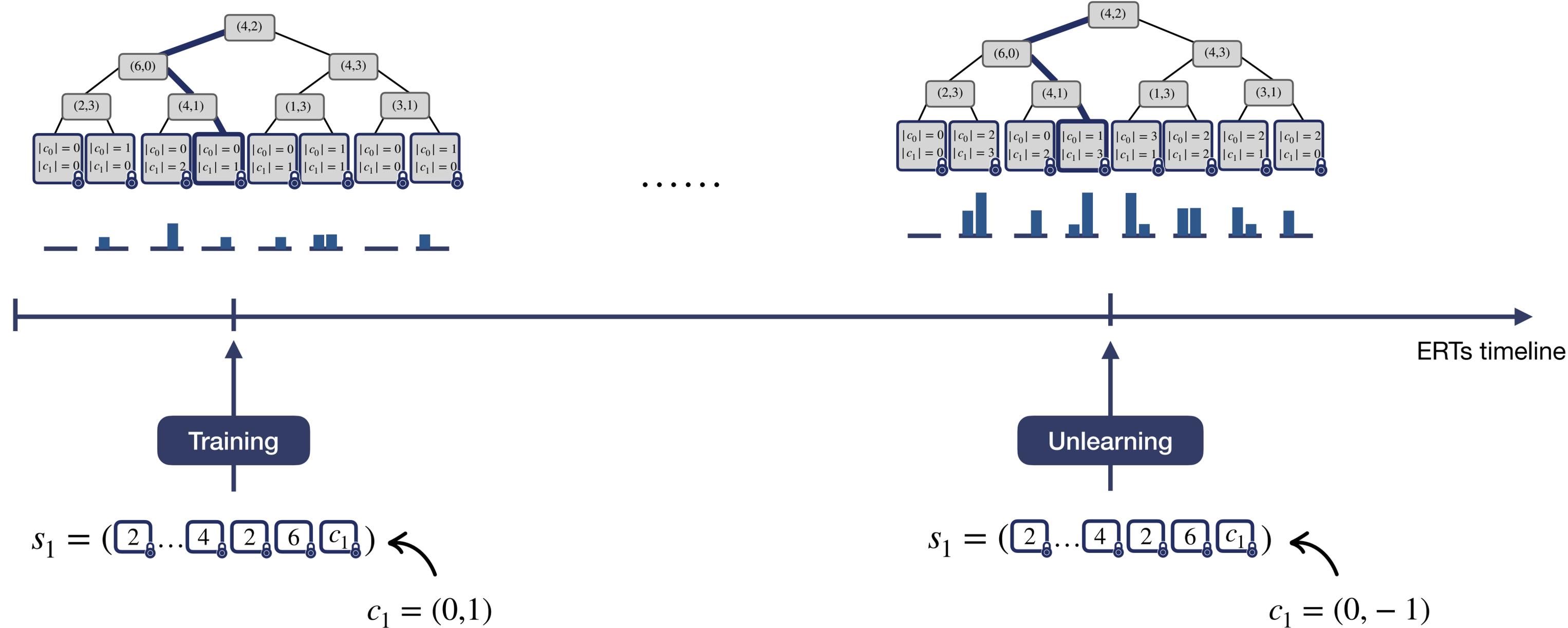
Training



Unlearning

Exact Unlearning

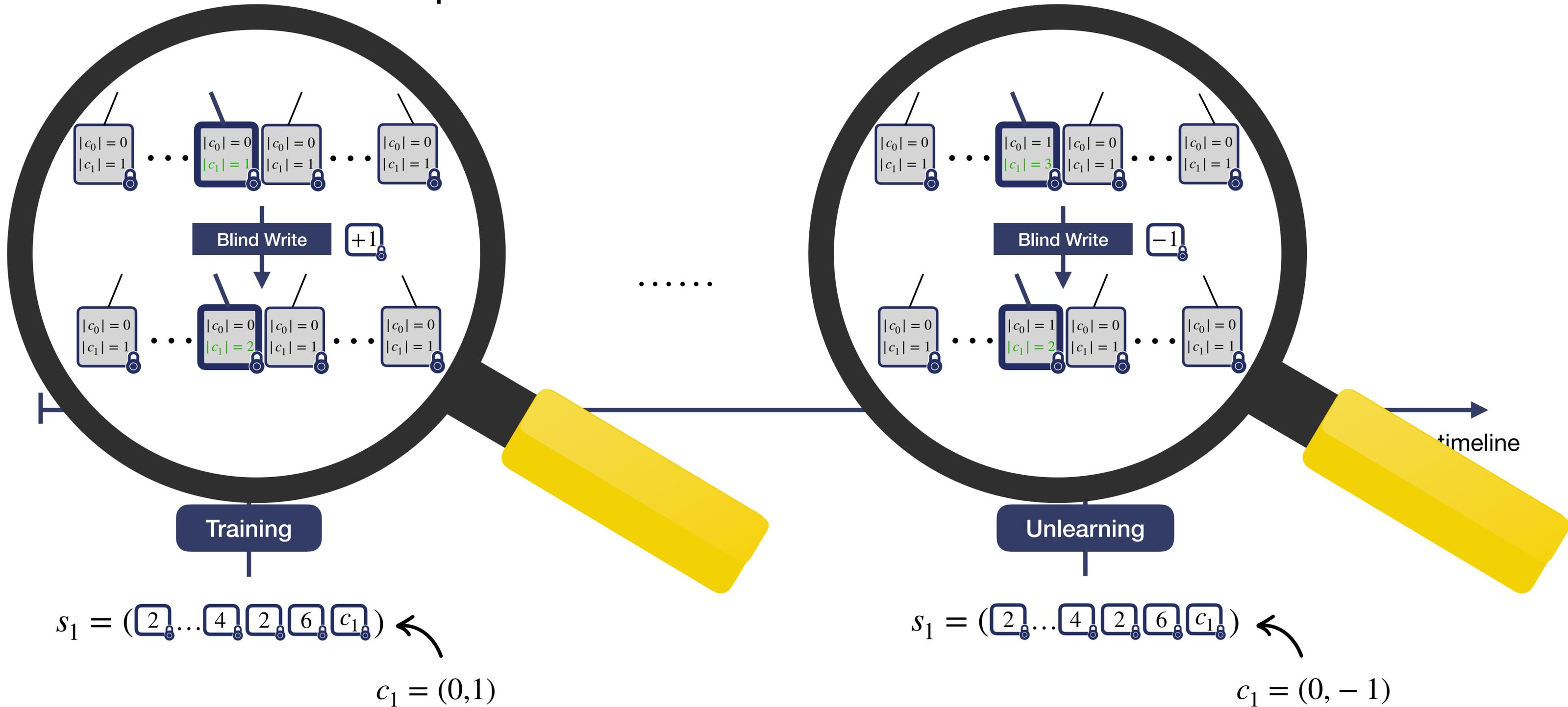
Because the traversal process is **deterministic** :



Exact Unlearning

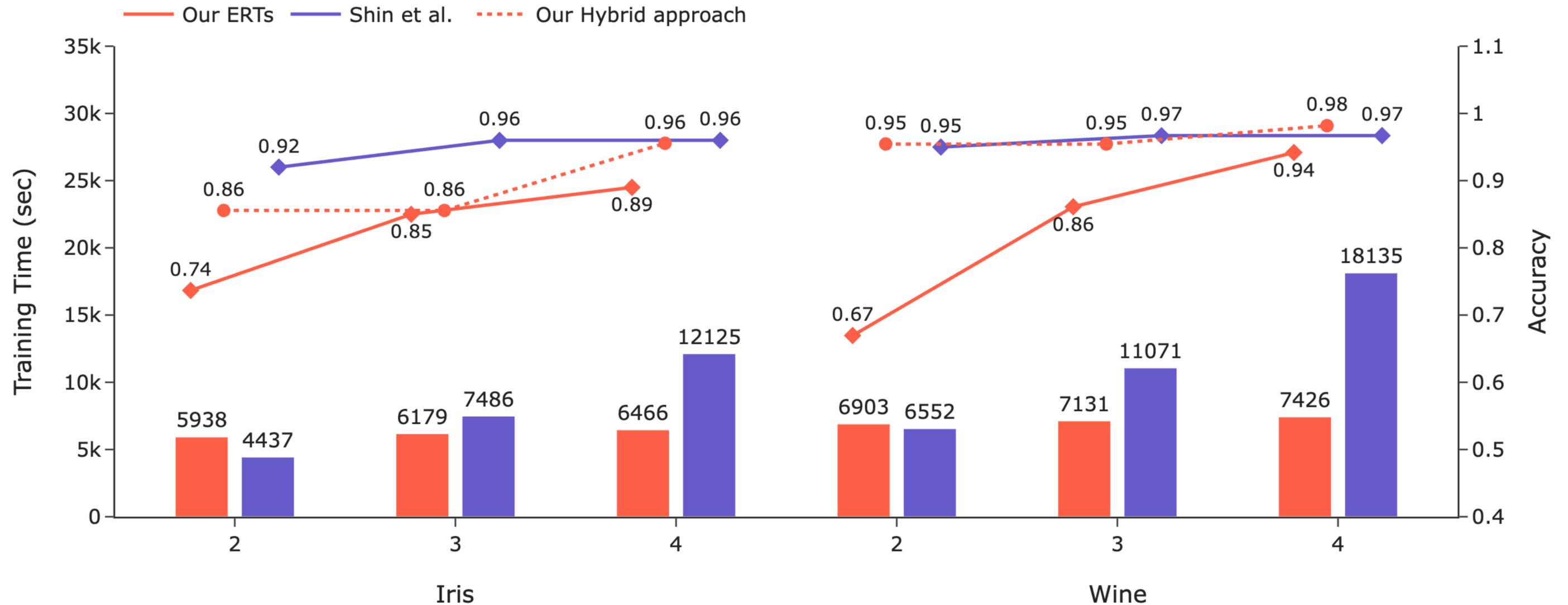
Correctness 

Because the traversal process is **deterministic** :

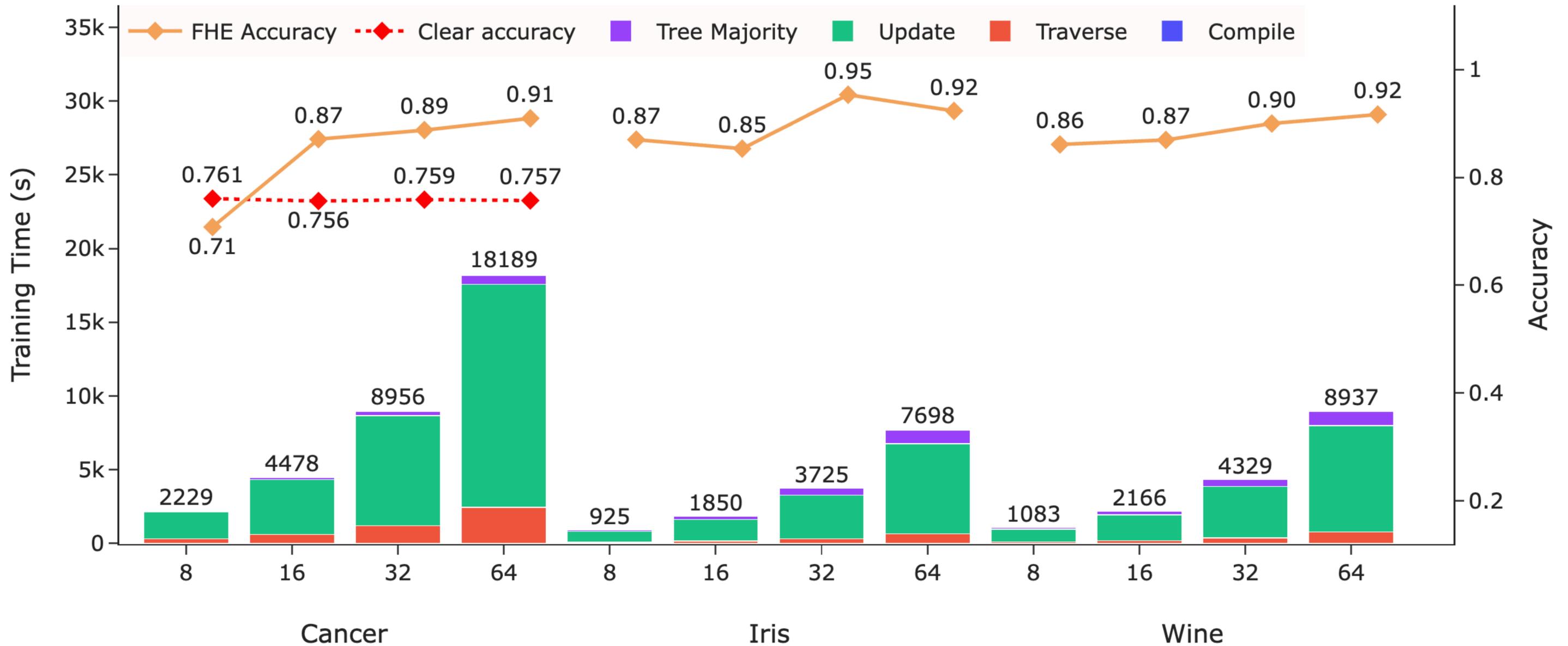


Experimental results

Comparison with **Random Forest** using **FHE** :



Experimental results



Key Takeaways

- **Oblivious computation** enables compliance
- Extremely Randomized Trees (ERTs) are **simple** and **FHE-friendly**
- Unlearning is **indistinguishable** from training
- No accuracy loss on encrypted data



Full paper : ia.cr/2025/1409



[sofianeazogagh/oblivious_unlearning](https://github.com/sofianeazogagh/oblivious_unlearning)

Thank you !

See you at the poster session



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